

The Art of the Flow

Sergei A. Voloshin



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Flow and:

- Centrality/energy dependence, and ideal fluid
- Constituent Quark Scaling, and deconfinement
- Nonflow/fluctuations, and “ridge”, initial geometry
- azHBT, and proof of collective expansion
- Velocity fields, vorticity, and polarization



Exploring the secrets
of the universe

Art Poskanzer



1 Color by Roberta Weir



Coauthored with Art: 7 phenomenology, PAs: 2 NA49 and 9 STAR

QM '95, NA49 and flow at SPS



Quark Matter '95

Y. Zhang (E877) – technique, first flow measurements at AGS

J-Y. Ollitrault - 'non-flow''

S.Voloshin, Y. Zhang arXiv:hep-ph/9407282v1 12 Jul 1994

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$$v_n = \langle \cos[n(\phi_i - \Psi_{RP})] \rangle$$

Event plane resolution correction made for each harmonic

Unfiltered theory can be compared to experiment!

QM '95, NA49 and flow at SPS

QM '97

Directed and Elliptic Flow in 158 GeV/Nucleon Pb + Pb Collisions

A.M. Poskanzer^a for the NA49 Collaboration

VOLUME 80, NUMBER 19

PHYSICAL REVIEW LETTERS

11 MAY 1998

(Received 10 November 1997)

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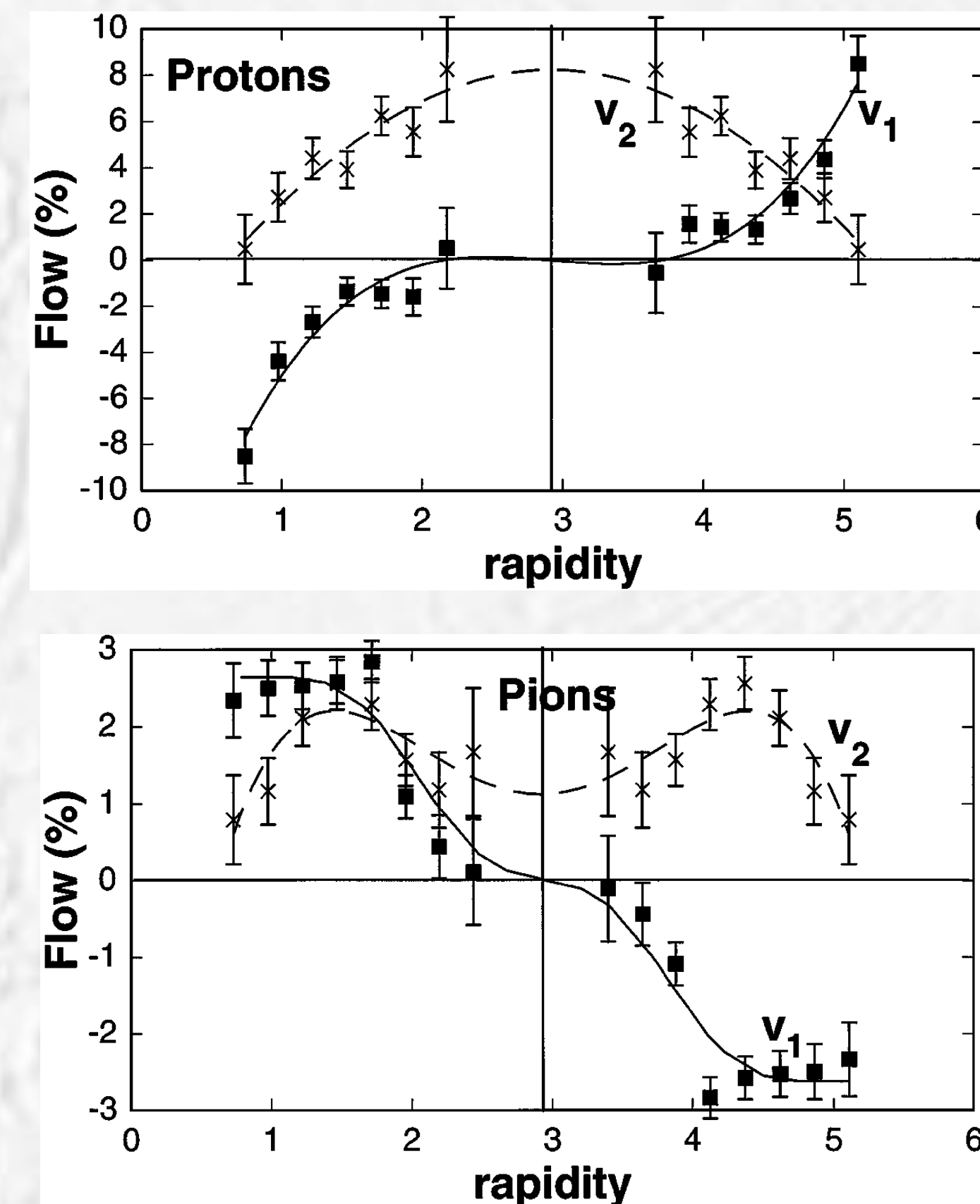


FIG. 2. The rapidity dependence of the directed (v_1) and elliptic (v_2) flow for the protons ($0.6 < p_t < 2.0$ GeV/c) and pions ($0.05 < p_t < 0.35$ GeV/c). The points below midrapidity ($y = 2.92$) have been reflected from the measurements in the forward hemisphere. The curves are to guide the eye.

Flow “method paper”

PHYSICAL REVIEW C

VOLUME 58, NUMBER 3

SEPTEMBER 1998

Methods for analyzing anisotropic flow in relativistic nuclear collisions

A. M. Poskanzer¹ and S. A. Voloshin^{2,*}

¹*Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, California 94720*

²*Physikalisches Institut der Universität Heidelberg, Heidelberg, Germany*

(Received 20 May 1998)

The strategy and techniques for analyzing anisotropic flow (directed, elliptic, etc.) in relativistic nuclear collisions are presented. The emphasis is on the use of the Fourier expansion of azimuthal distributions. We present formulas relevant for this approach, and in particular, show how the event multiplicity enters into the event plane resolution. We also discuss the role of nonflow correlations and a method for introducing flow into a simulation. [S0556-2813(98)04109-0]

Physical Review C 50th Anniversary Milestones



Citations: [Google Scholar/inSPIRE 2157/1410](#)

Flow proponent

Art: Flow proponent, advocate, supporter

Promoted and developed flow methods, codes, analyses, helped to test ALICE codes...

Was happy to see how flow draws attention at the conferences

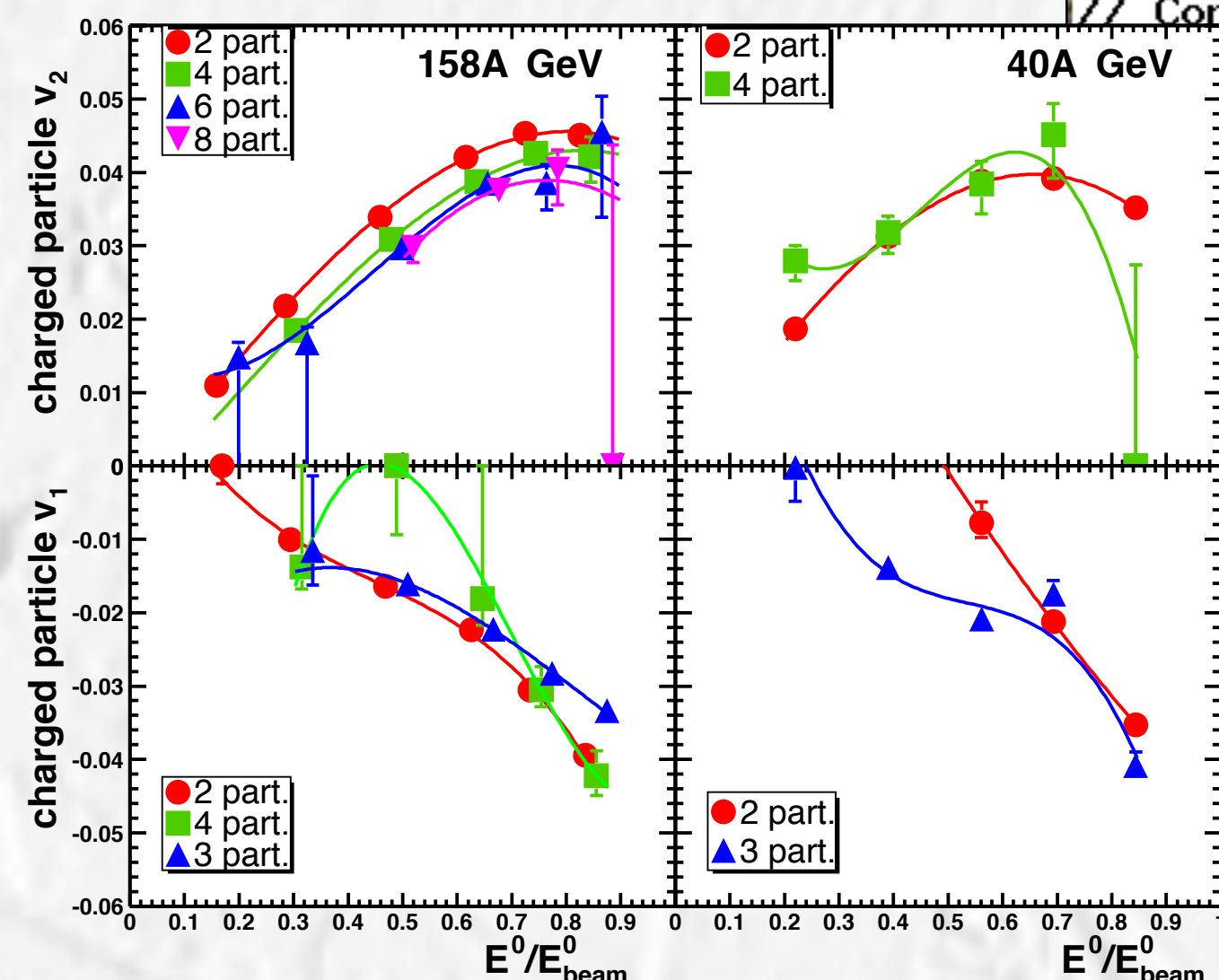
Notations, $v_2\{EP\}$
 FlowStyle in ROOT
 FlowEvent
 “little” q flow vector
 v_2^2/v_4 physics

```

////////////////////////////////////
//
// $Id: StFlowEvent.cxx,v 1.7 2000/06/01 18:26:35 posk Exp $
//
// Author: Raimond Snellings and Art Poskanzer
////////////////////////////////////
//
// Description: A subset of StEvent
//
////////////////////////////////////
//
// $Log: StFlowEvent.cxx,v $
// Revision 1.7 2000/06/01 18:26:35 posk
// Increased precision of Track integer data members.
//
// Revision 1.6 2000/05/20 00:55:13 posk
// Condensed flownanoevent.root somewhat.
    
```

DIRECTED AND ELLIPTIC FLOW OF CHARGED PIONS ...

PHYSICAL REVIEW C 68, 034903 (2003)



```

Revision 1.5 2000/05/16 20:59:29 posk
oshin's flownanoevent.root added.

Revision 1.4 2000/05/12 22:42:04 snelling
itions for persistency and minor fix
    
```

```

////////////////////////////////////
//
// $Id: StFlowNanoEvent.cxx,v 1.6 2000/05/26 21:29:30 posk Exp $
//
// Author: Sergei Voloshin and Raimond Snellings, March 2000
//
// Description: A persistent Flow nano DST
//
// The StFlowNanoEvent class has a simple event structure:
//   TClonesArray *fTracks;
//
//   Int_t          mNtrack;           // track number
//   Int_t          mEventID;         // event ID
//   UInt_t         mOrigMult;        // number of StEvent tracks
//   UInt_t         mCentrality;      // centrality bin
//   StThreeVectorF mVertexPos;      // primary vertex position
//
// The StFlowNanoEvent data member fTracks is a pointer to a TClonesArray.
// It is an array of a variable number of tracks per event.
// Each element of the array is an object of class StFlowTrack
//
////////////////////////////////////
//
// $Log: StFlowNanoEvent.cxx,v $
// Revision 1.6 2000/05/26 21:29:30 posk
// Protected Track data members from overflow.
    
```

FIG. 21. (Color online) Weighted flow $\langle w_n e^{in(\phi - \Phi_{RP})} \rangle / \sqrt{\langle w_n^2 \rangle}$, Eq. (13), with $w_1 = y$ in the center of mass frame and $w_2 = p_t$, from the

Elliptic flow centrality/energy dependence

The physics of the centrality dependence of elliptic flow

S.A. Voloshin ^{a,b}, A.M. Poskanzer ^a

^a Nuclear Science Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA

^b Department of Physics and Astronomy, Wayne State University, Detroit, MI 48201, USA

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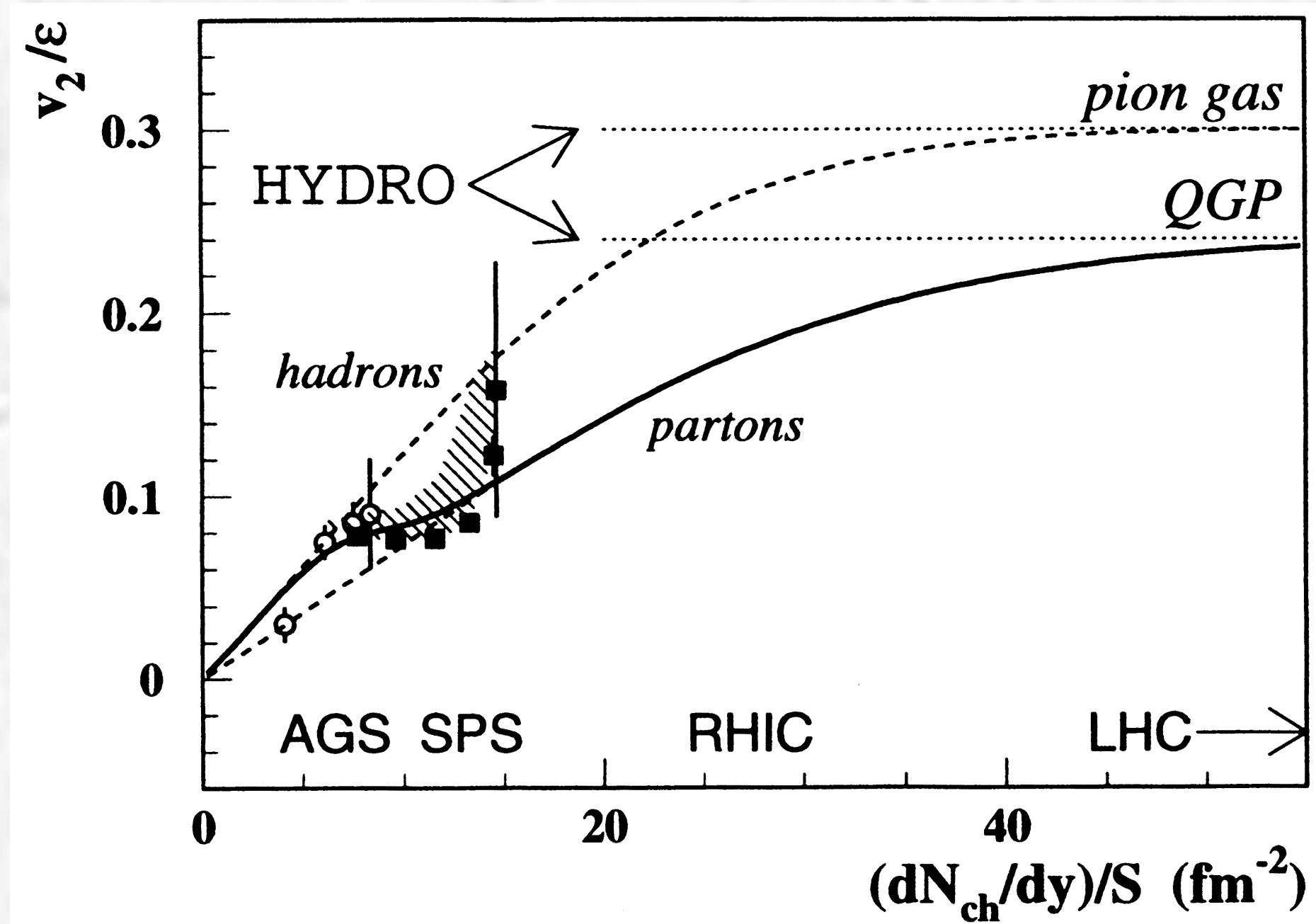


Fig. 3. Elliptic flow divided by the initial space elliptic anisotropy at the AGS (open circles) and the SPS (filled squares). The shaded area shows the uncertainty in the SPS experimental data due to the uncertainty in the centrality determination. See text and footnote for the description of the curves and hydro limits.

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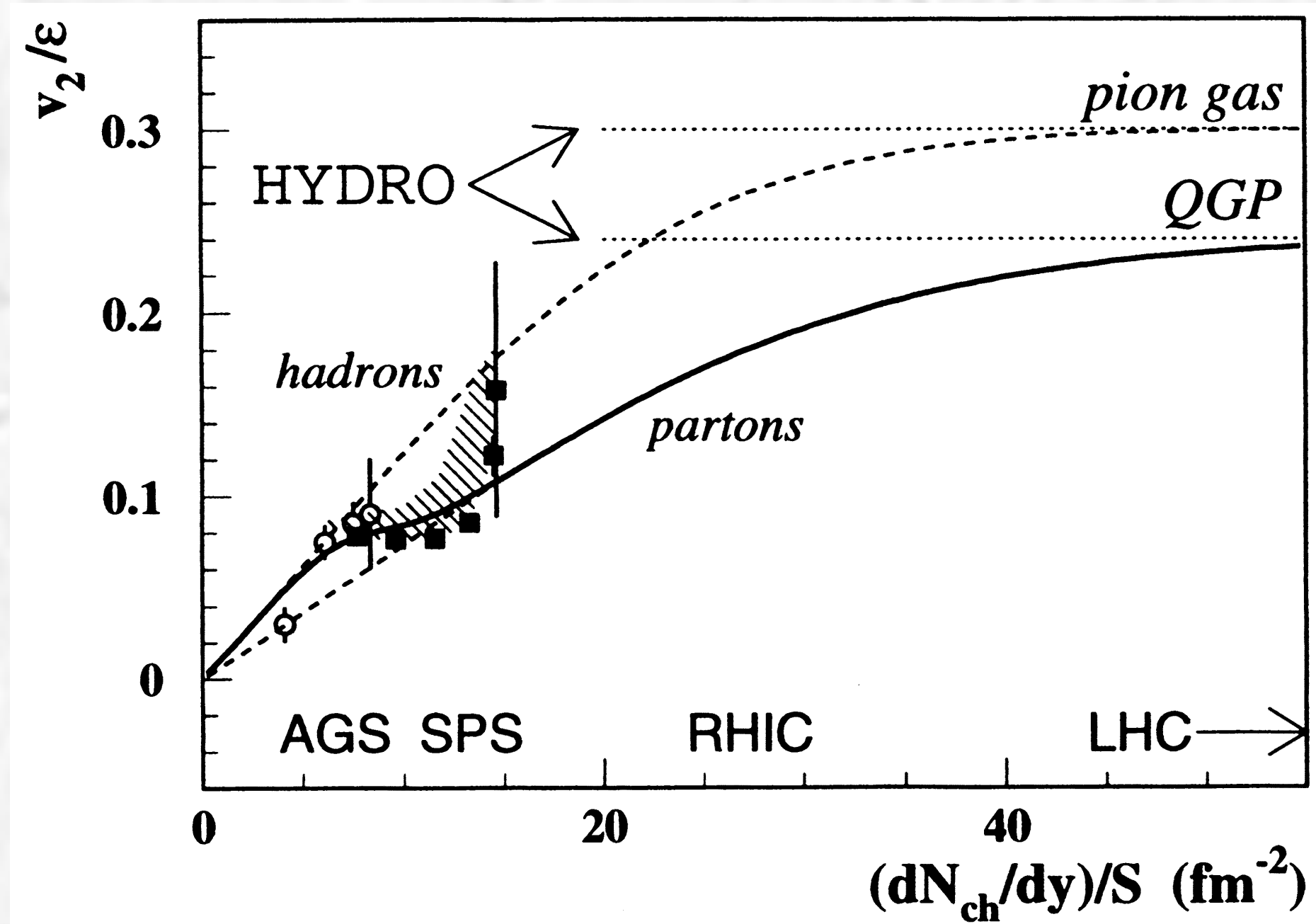
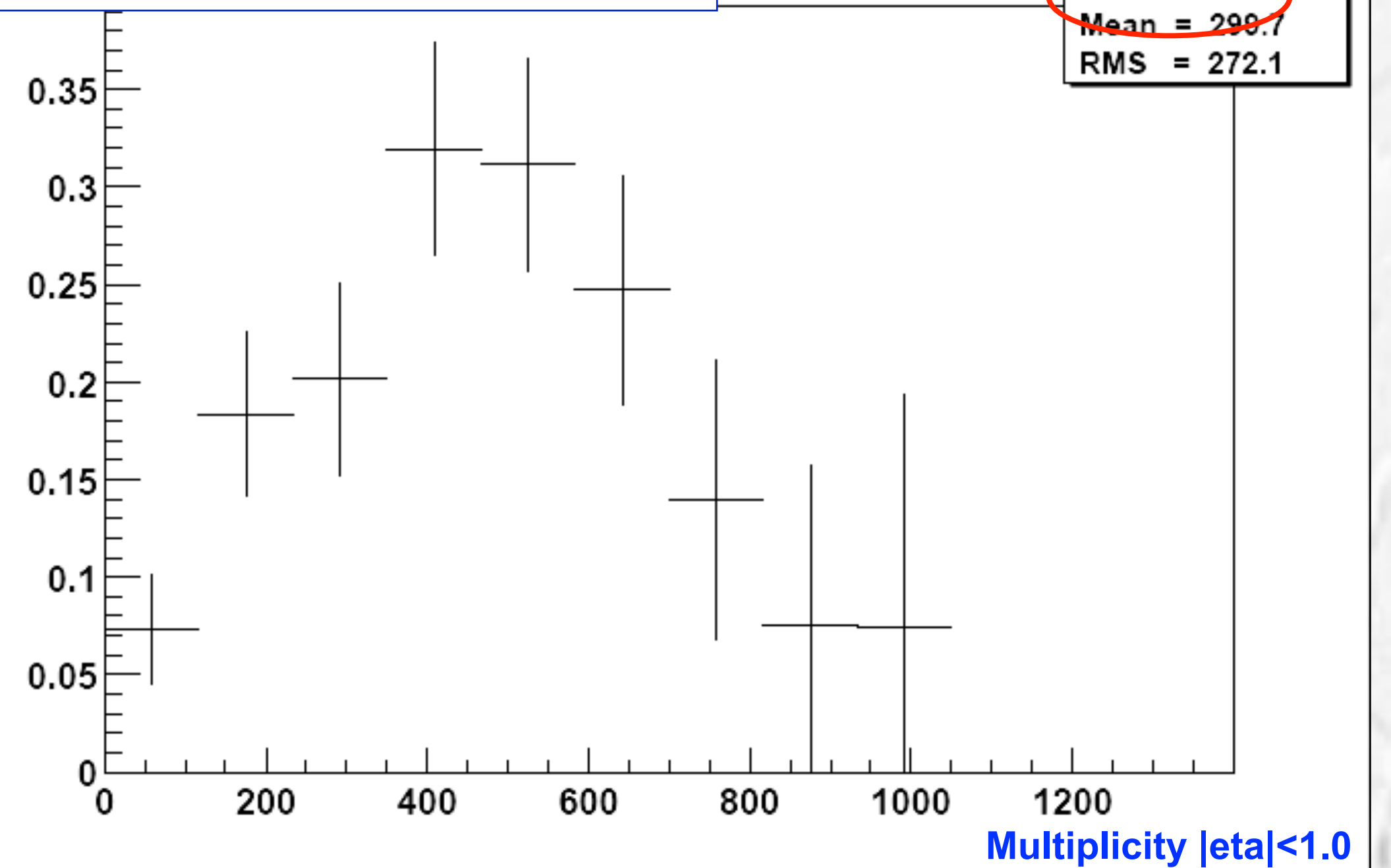


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2-particle azimuthal correlations

$$N \langle \cos(2\phi_i - 2\phi_j) \rangle \approx N v_2^2$$

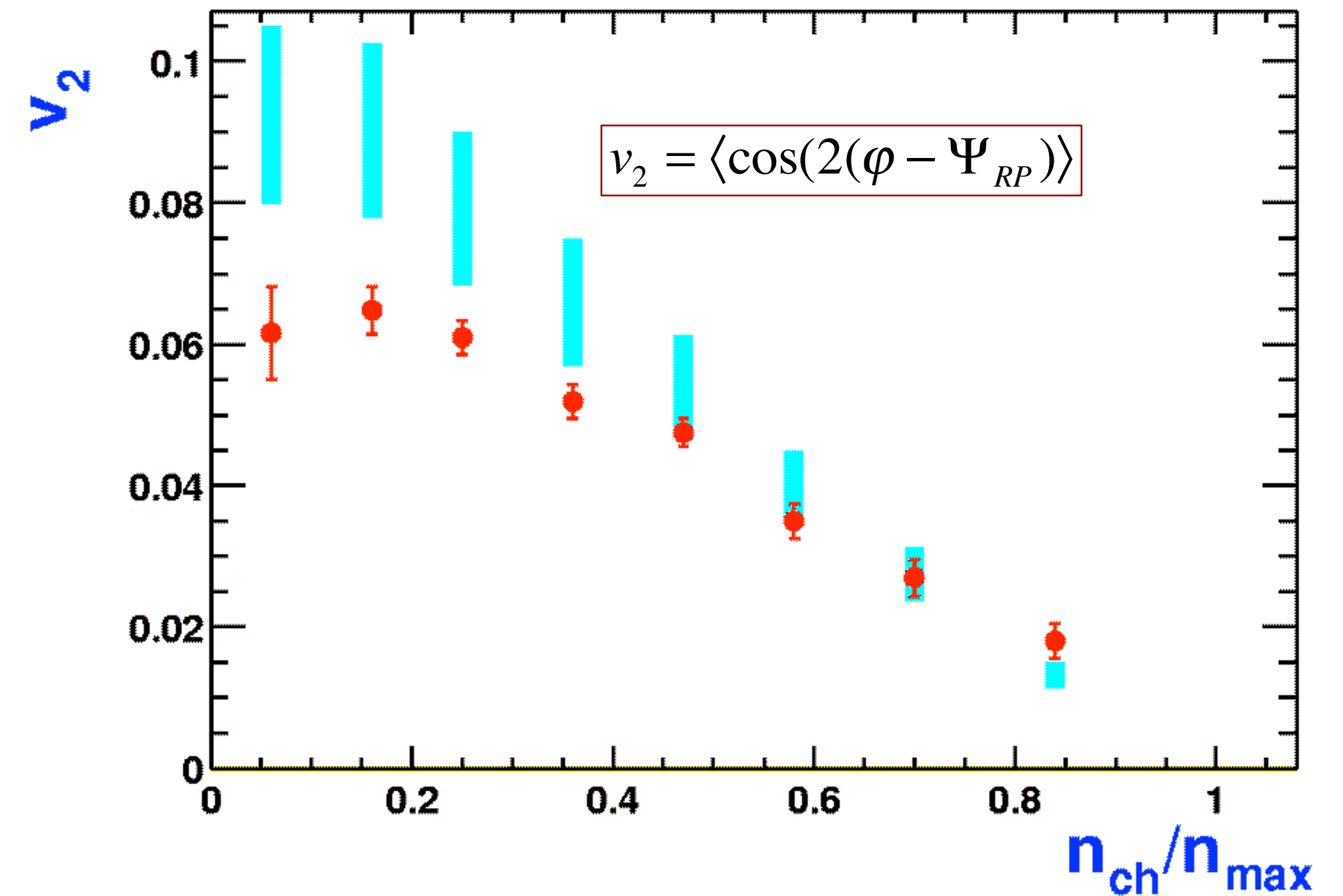


Results from data taken during the first three hours of RHIC operation

First observation of elliptic flow at RHIC (STAR)



STAR Collaboration , PRL, 86 (2000) 402



For the first time in Heavy-Ion Collisions the flow measurements are in **quantitative** agreement with hydrodynamic model predictions up to mid-central collisions
Dense and (likely) thermalized matter

Elliptic flow centrality/energy dependence

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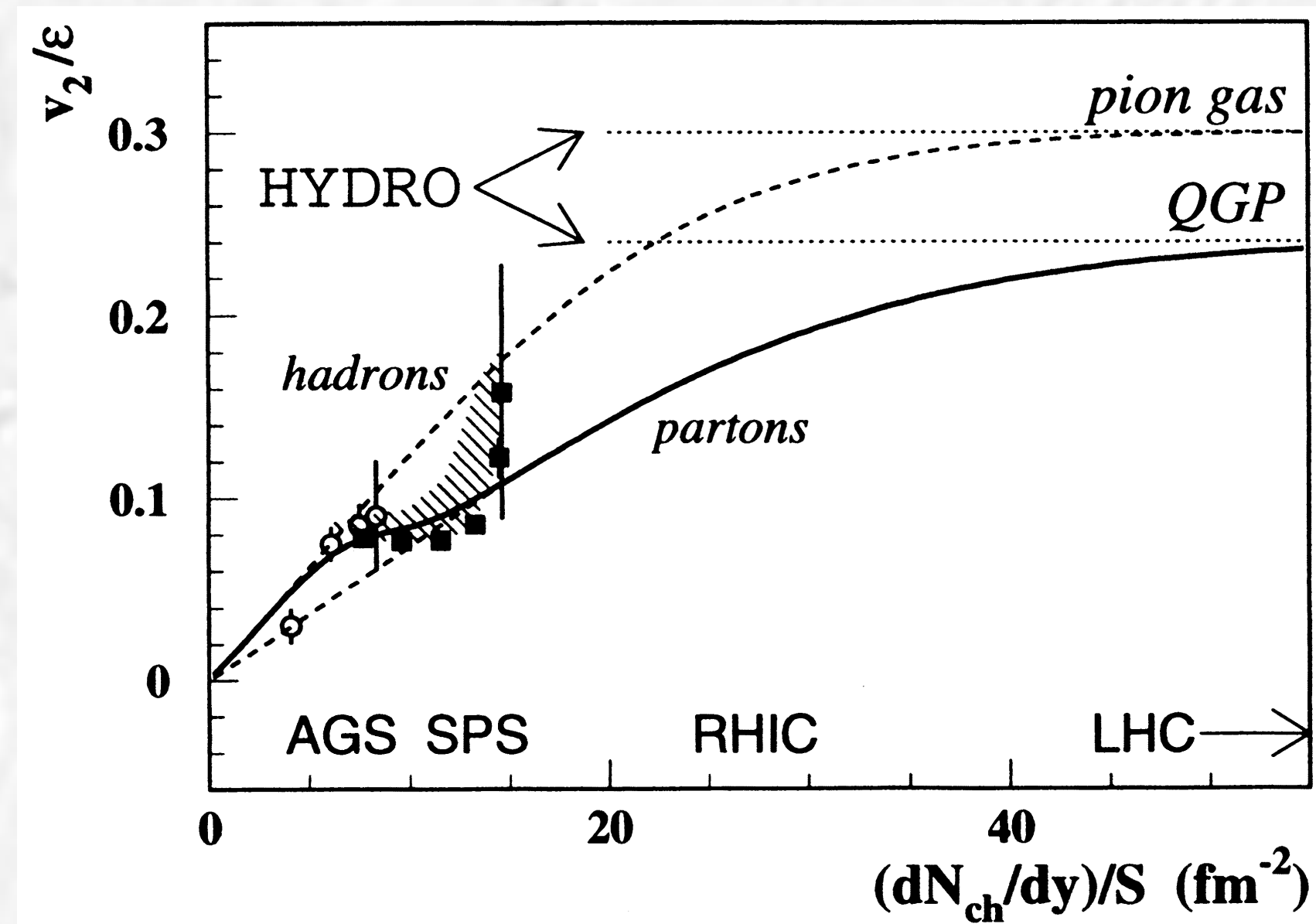
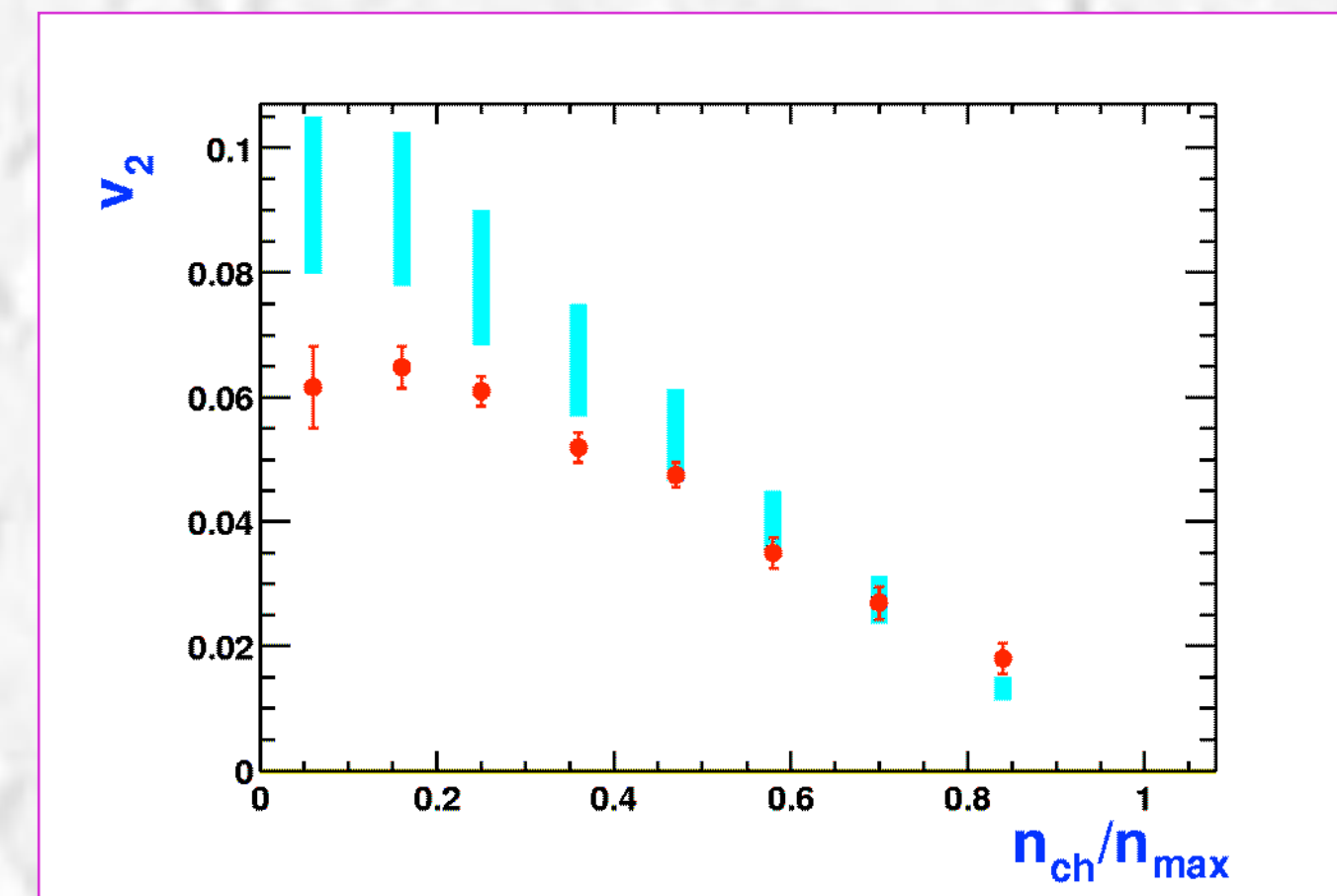


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PHYSICAL REVIEW C **68**, 034903 (2003)

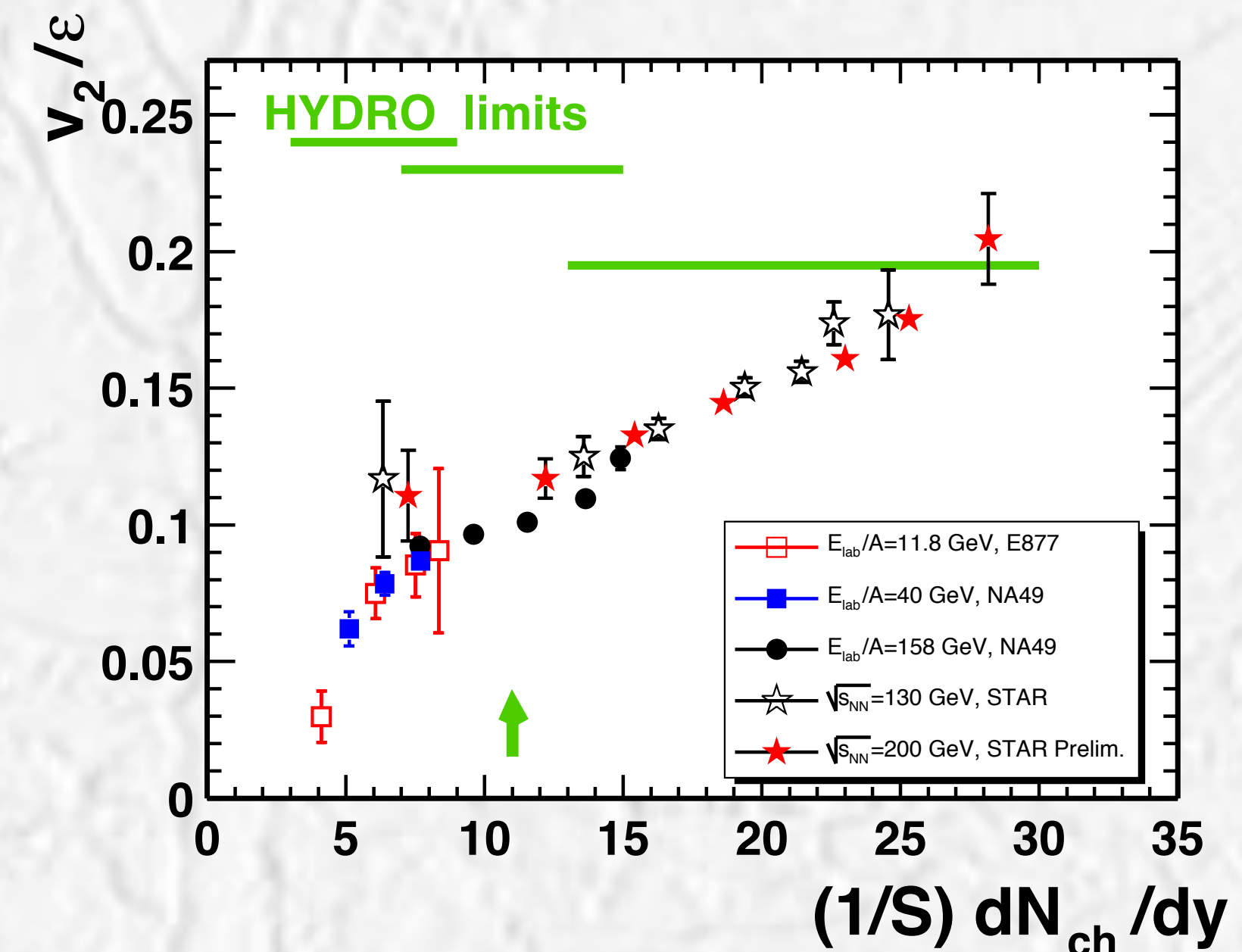


FIG. 25. (Color online) v_2/ϵ as a function of particle density. The v_2 values are for near midrapidity ($0 < y < 0.6$ for 40A GeV and $0 < y < 0.8$ for 158A GeV). The results of NA49 pion v_2 are compared to charged particle v_2 measured by E877 and STAR. The meaning of the horizontal lines (hydro limits) and of the arrow will be discussed in Sec. VI.

QGP - The Perfect fluid

Universe May Have Begun as Liquid, Not Gas

Associated Press
Tuesday, April 19, 2005; Page A05

The Washington Post

New results from a particle collider suggest that the universe behaved like a liquid in its earliest moments, not the fiery gas that was thought to have pervaded the early universe.

Early Universe was a liquid

Quark-gluon blob surprises particle physicists.

by Mark Peplow
news@nature.com

nature

The Universe consisted of a perfect liquid in its first moments, according to new results from an atom-smashing experiment.

New State of Matter Is 'Nearly Perfect' Liquid

Physicists working at Brookhaven National Laboratory announced today that they have created what appears to be a new state of matter out of the building blocks of atomic nuclei, quarks and gluons. The researchers unveiled their findings—which could provide new insight into the composition of the universe just moments after the big bang—today in Florida at a meeting of the American Physical Society.

SCIENTIFIC AMERICAN

There are four collaborations, dubbed BRAHMS, PHENIX, PHOBOS and STAR, working at Brookhaven's Relativistic Heavy Ion Collider (RHIC). All of them study what happens when two interacting beams of gold ions smash into one another at great velocities, resulting in thousands of subatomic collisions every second. When the researchers analyzed the patterns of the atoms' trajectories after these collisions, they



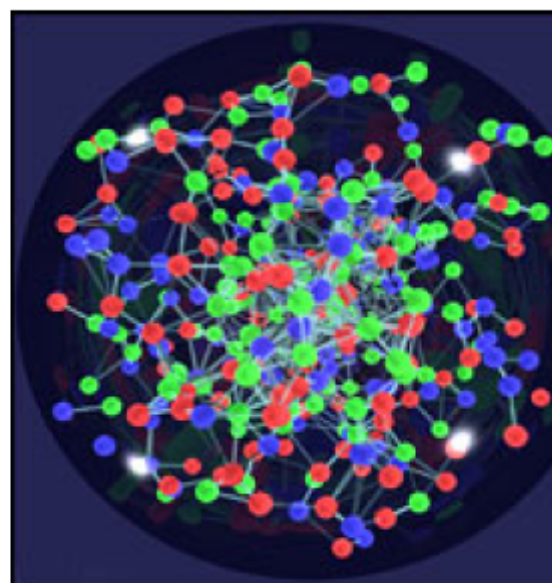
Image: BNL

Early Universe was 'liquid-like'

Physicists say they have created a new state of hot, dense matter by crashing together the nuclei of gold atoms.

BBC NEWS

The high-energy collisions prised open the nuclei to reveal their most basic particles, known as quarks and gluons.



The impression is of matter that is more strongly interacting than predicted.

The researchers, at the US Brookhaven National Laboratory, say these particles were seen to behave as an almost perfect "liquid".

SCIENTIFIC AMERICAN

MAY 2006
WWW.SCIAM.COM

Quark Soup

PHYSICISTS RE-CREATE THE LIQUID STUFF OF THE EARLIEST UNIVERSE



社会 asahi.com トップ > 社会 > その他・話題

宇宙の始まりはしづく? 「クォークは液体」と発表

2005年04月18日23時34分

宇宙誕生の大爆発「ビッグバン」直後に相当する超高温・高密度の状態を再現する実験をしてきた日米などの国際チームは18日、物質を形づくる究極の基本粒子クォークは超高温でバラバラになるが、気体のように自由に飛び回るのでなく、しづくのような液体状態にあったと考えられる、と発表。宇宙や物質のなりたちを説明する。

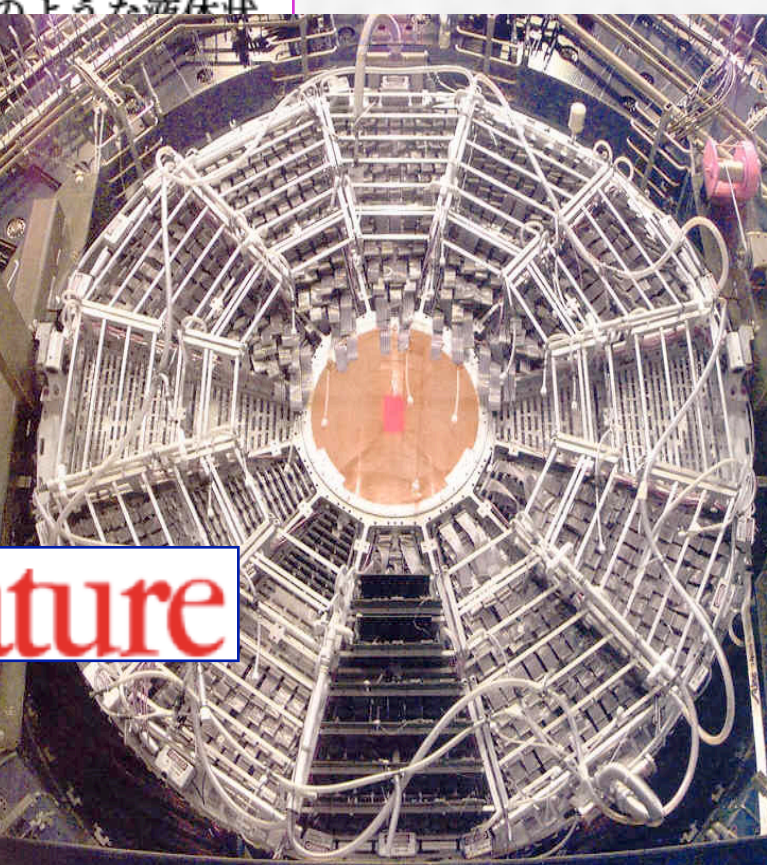
基本粒子クォークとそれらをく

What's in a name?

Physicists agree that experiments at the Brookhaven atom collider have created

a new form of matter. But theorists and experimentalists are still arguing about what to call it. Geoff Brumfiel investigates.

nature



Early Universe Went With the Flow

Posted April 18, 2005 5:57PM

Between 2000 and 2003 the lab's Relativistic Heavy Ion Collider repeatedly smashed the nuclei of gold atoms together with such force that their energy briefly generated trillion-degree temperatures. Physicists think of the collider as a time machine, because those extreme temperature conditions last prevailed in the universe less than 100 millionths of a second after the big bang.



Early Universe Liquid-Like

Aronson, associate director for high energy nuclear physics at Brookhaven National Laboratory, which is located on Long Island at 65 miles east of New York city. Between 2000 and 2003 the lab's Relativistic Heavy Ion Collider, known as RHIC, repeatedly smashed the nuclei of

gold atoms together with such force that their energy briefly generated trillion-degree temperatures. Physicists think of the collider as a time machine, because those extreme temperature conditions last prevailed in the universe less than 100 millionths of a second after the big bang. Everything was so hot then that quarks and gluons, which are now almost inextricably bound into the protons and neutrons inside atomic nuclei, were thought to have flown around like BBs in a blender. But by reproducing the conditions of the early universe, RHIC has shown that unconstrained quarks and gluons don't fly away in all

directions so much as squirt out in streams. "The matter that we've formed behaves like a very nearly perfect liquid," Aronson said. When physicists talk about a perfect liquid, they don't mean the best glass of champagne they ever tasted. The word "perfect" refers to the liquid's viscosity, a friction-like property that

affects a fluid's flow and the way it reacts to objects that move through it. High viscosity means a fluid flows slowly. Theoretical physicists have recently proposed that material swallowed

and what goes on when two gold nuclei collide at RHIC.

concept of the early universe, the new discovery offers opportunities to

Society. "There are a lot of exciting questions," said

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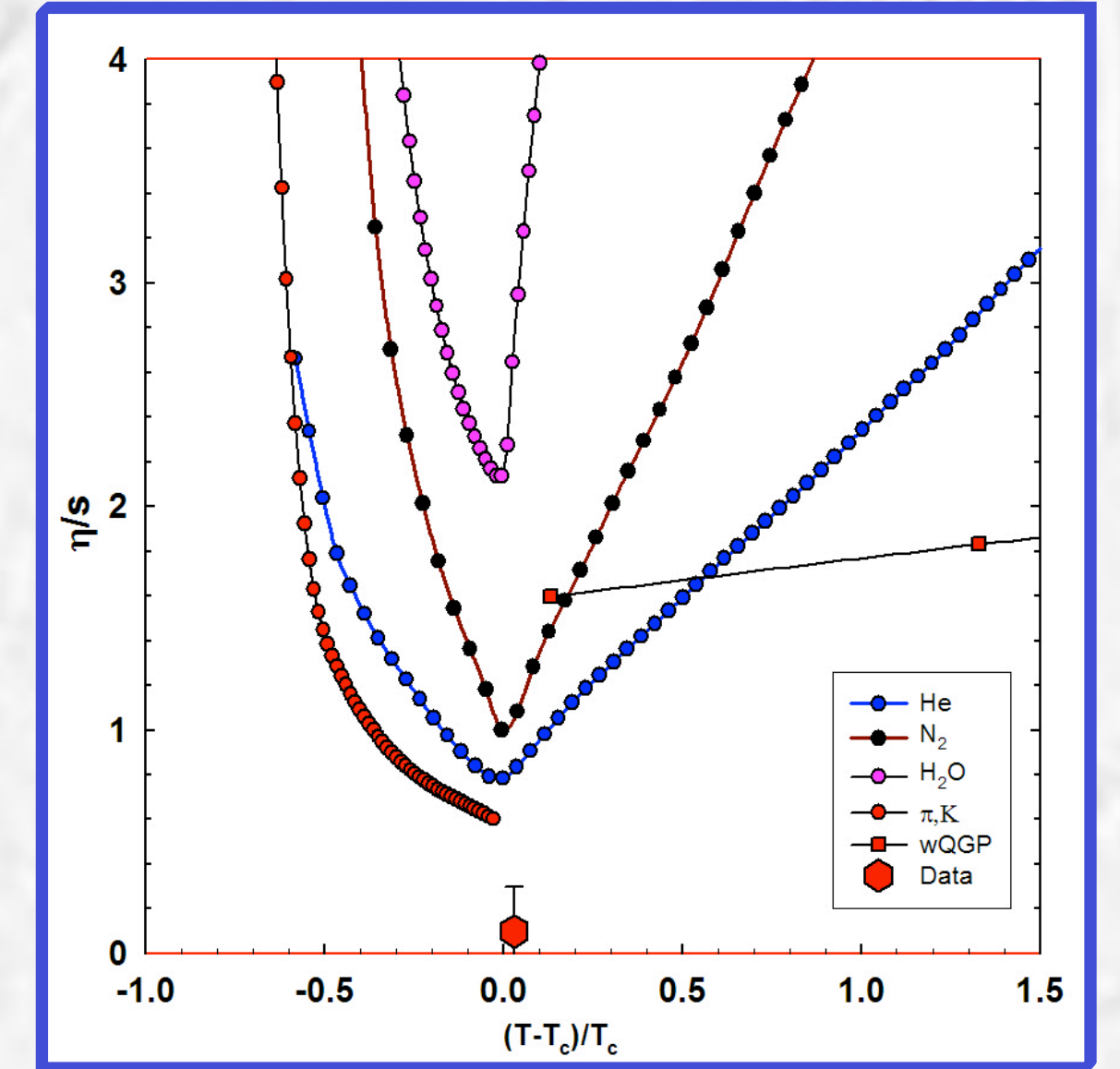
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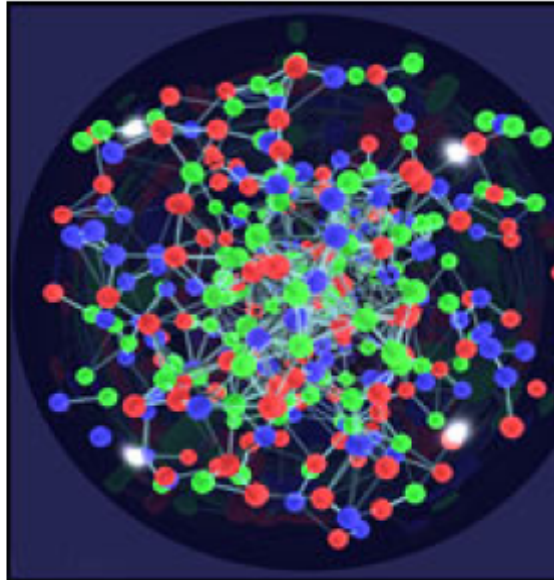


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Science

Iran Daily April 20, 2005 4

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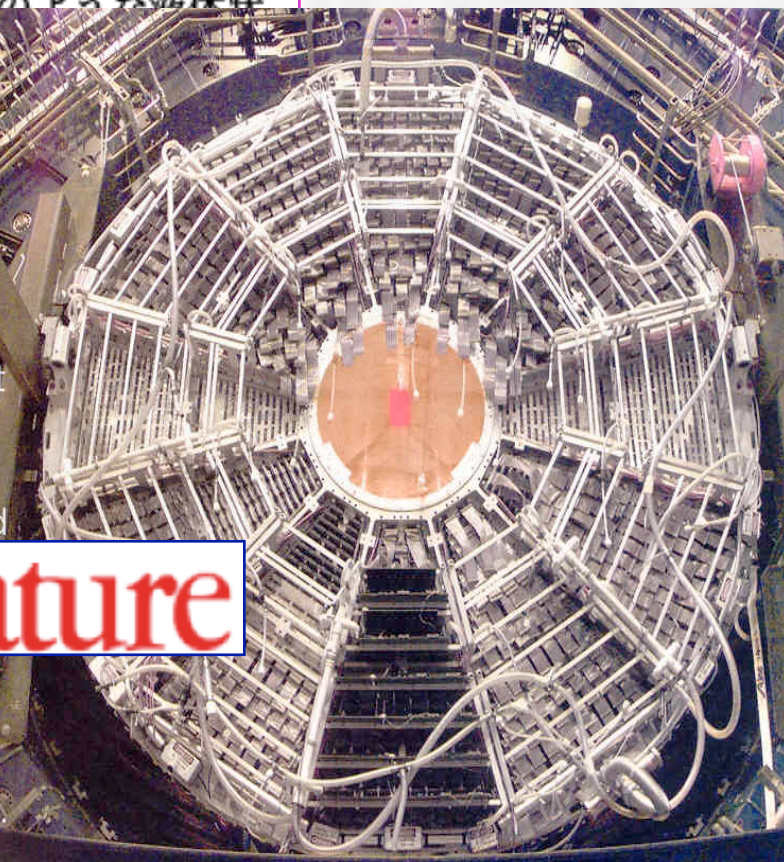
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nature



low, December 8-9, 2022

S.A. Voloshin

WAYNE STATE UNIVERSITY

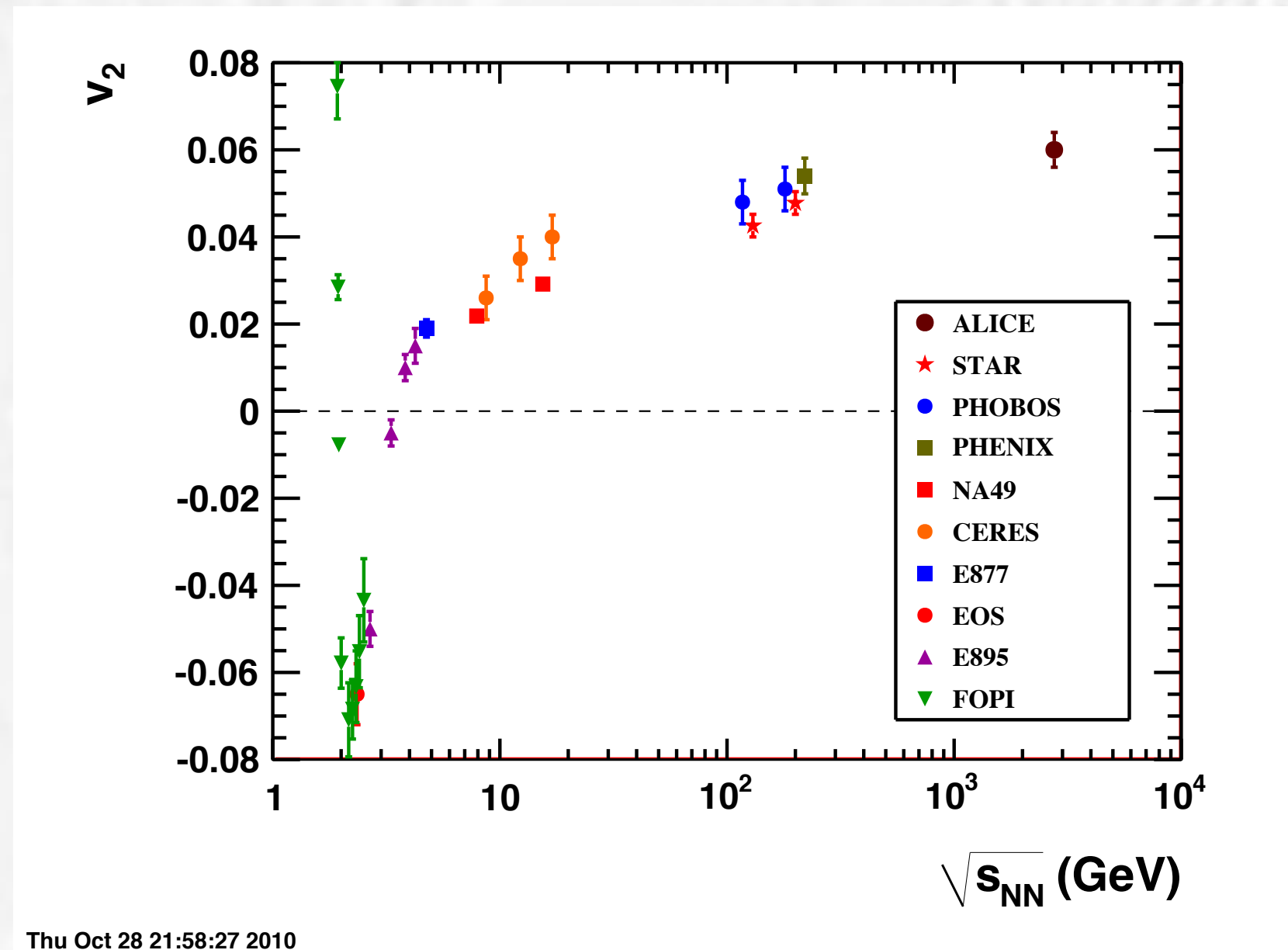
Energy dependence: AGS-SPS-RHIC-LHC

version 7, November 7, 2010. Text: [new](#), [old](#), [questions](#)

Elliptic flow of charged particles in Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV

de M. Michel Nostradamus

We report the first measurement of charged particle elliptic flow in Pb+Pb collisions at $\sqrt{s_{NN}} = 2.76$ TeV with the ALICE detector at the CERN Large Hadron Collider. The measurement is performed in the central pseudorapidity region ($|\eta| < 0.8$) and transverse momentum range $0.25 < p_t < 5$ GeV/c. The elliptic flow signal, v_2 , averaged over transverse momentum and pseudorapidity, reaches values of **0.085** for relatively peripheral collisions (40–50% most central). The differential elliptic flow $v_2(p_t)$ reaches a maximum of **0.25** around $p_t = 3$ GeV/c. Compared to RHIC Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV, the elliptic flow increases by about **15%** in agreement with hydrodynamical model predictions.



Thu Oct 28 21:58:27 2010

FIG. 4. Integrated elliptic flow in Pb+Pb 20–30% centrality collisions at 2.76 TeV compared with results from lower energies taken at similar centralities. The compilation is taken from [26].

Energy dependence: AGS-SPS-RHIC-LHC

version 7, November 7, 2010. Text: [new](#), [old](#), [questions](#)

PRL 105, 252302 (2010)

Selected for a [Viewpoint in Physics](#)
PHYSICAL REVIEW LETTERS

week ending
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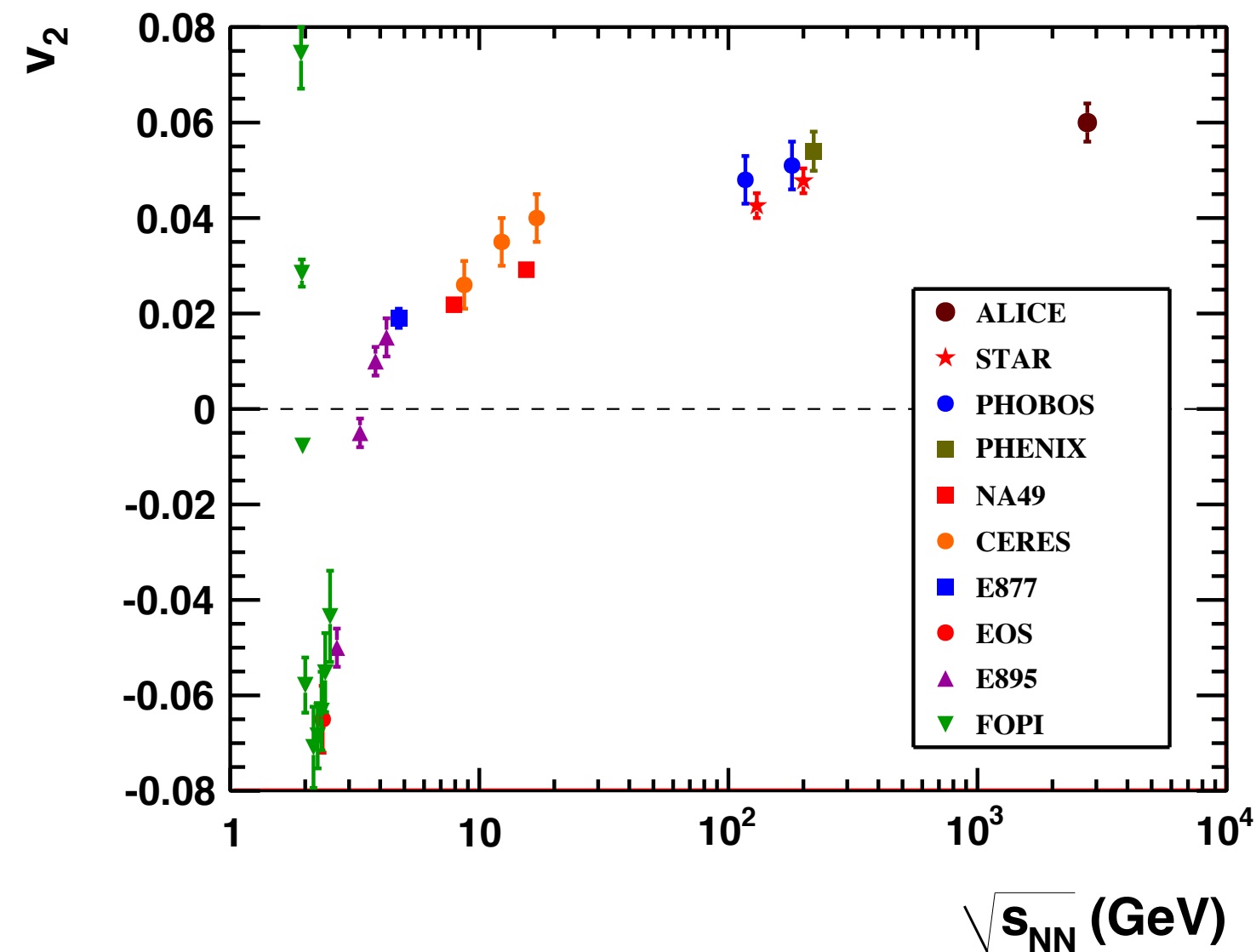
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DOI: [10.1103/PhysRevLett.105.252302](https://doi.org/10.1103/PhysRevLett.105.252302)

PACS numbers: 25.75.Ld, 25.75.Gz, 25.75.Nq



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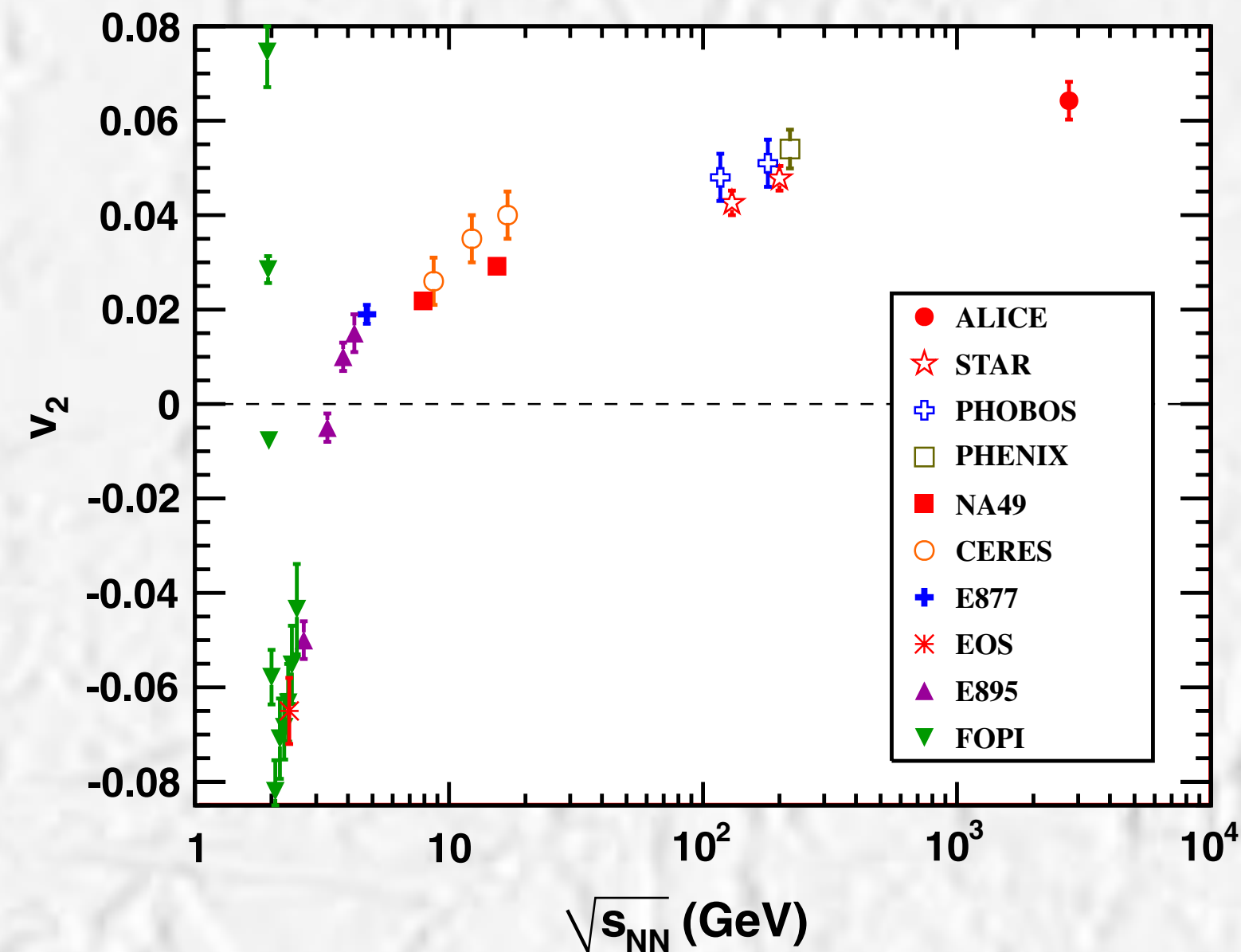


FIG. 4 (color online). Integrated elliptic flow at 2.76 TeV in Pb-Pb 20%–30% centrality class compared with results from lower energies taken at similar centralities [40,43].

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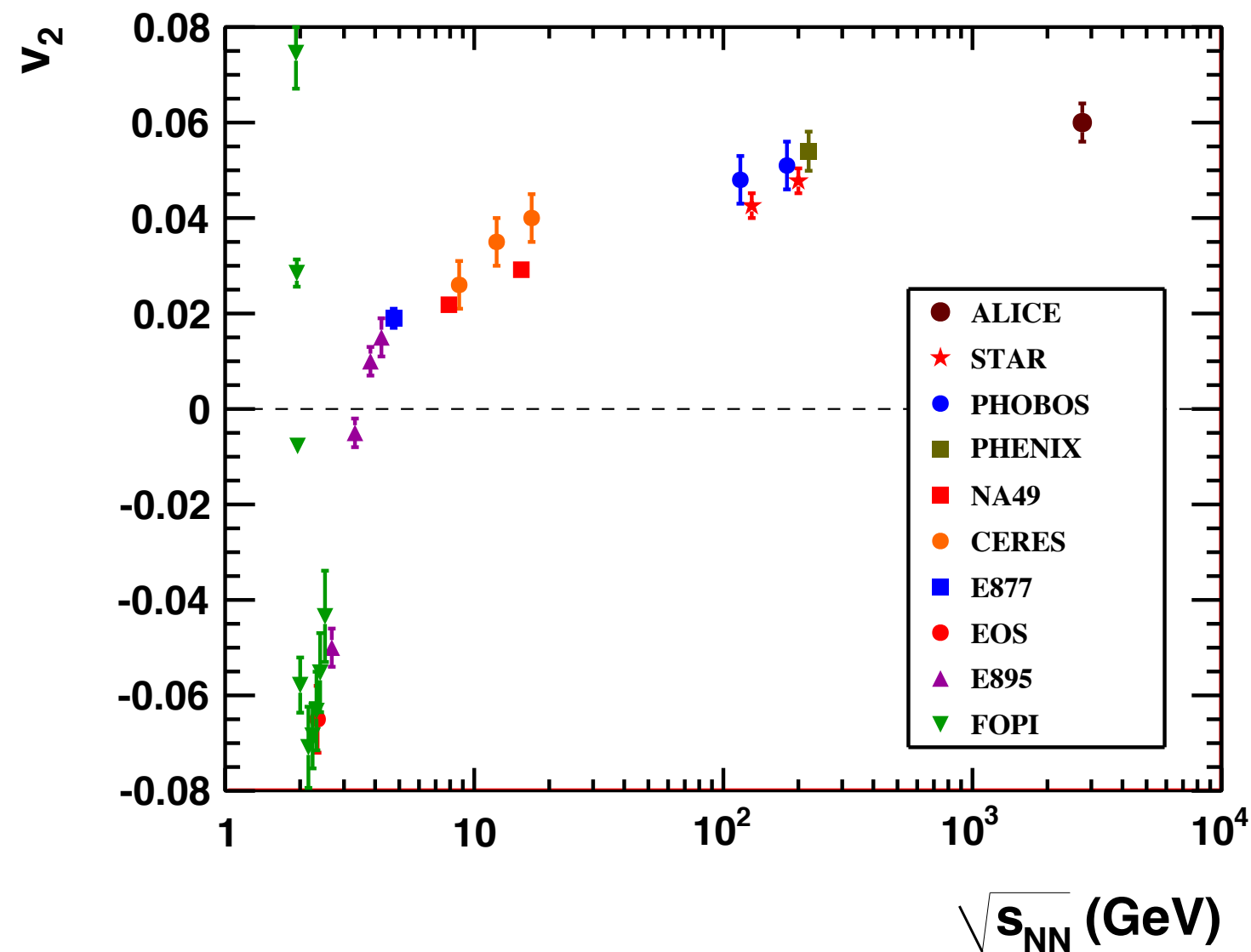
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Thu Oct 28 21:58:27 2010

FIG. 4. Integrated elliptic flow in Pb+Pb 20–30% centrality collisions at 2.76 TeV compared with results from lower energies taken at similar centralities. The compilation is taken from [26].

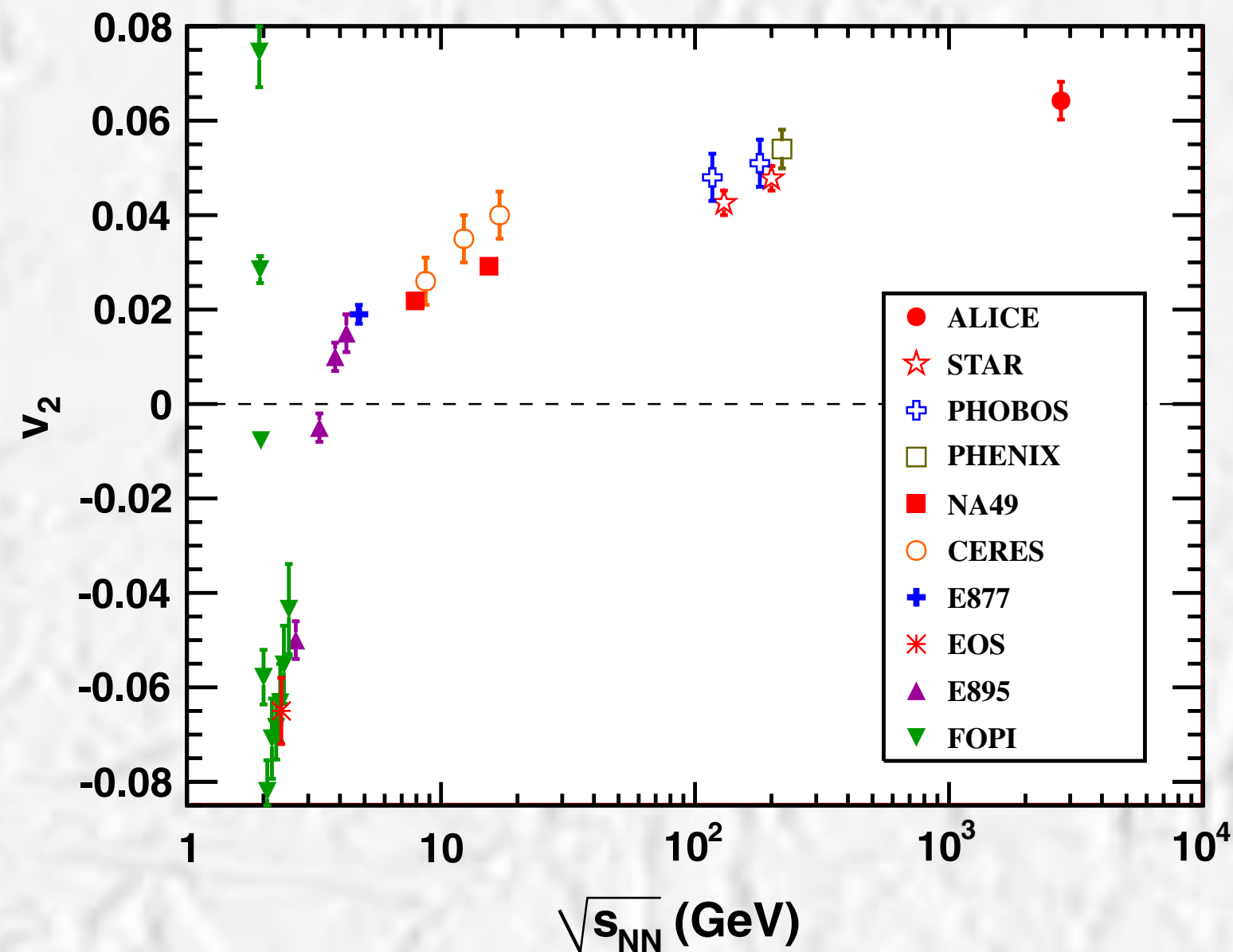
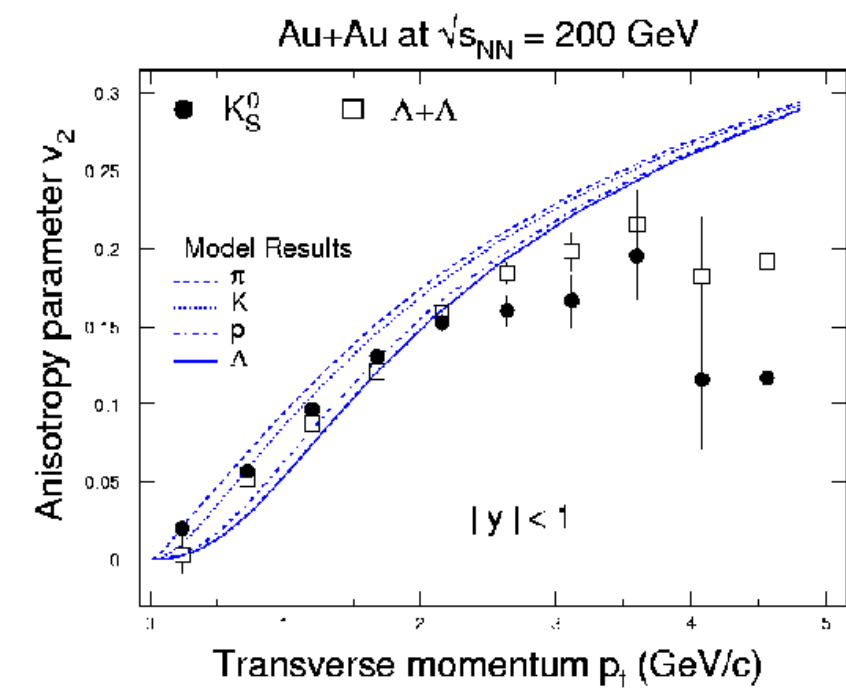
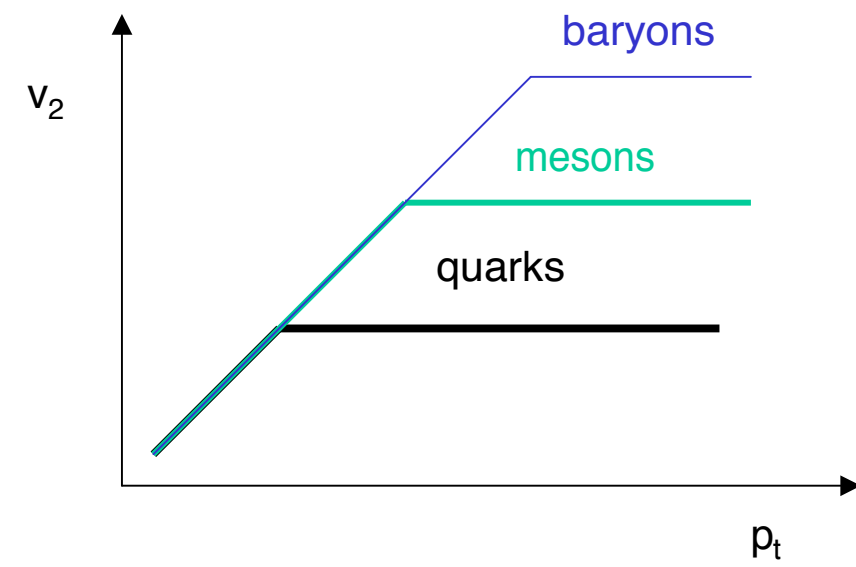


FIG. 4 (color online). Integrated elliptic flow at 2.76 TeV in Pb-Pb 20%–30% centrality class compared with results from lower energies taken at similar centralities [40,43].

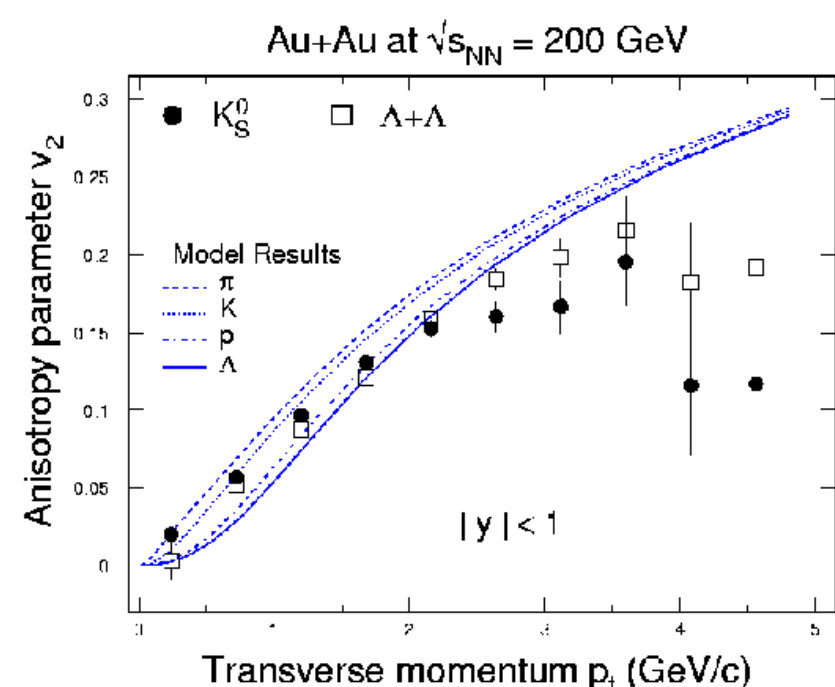
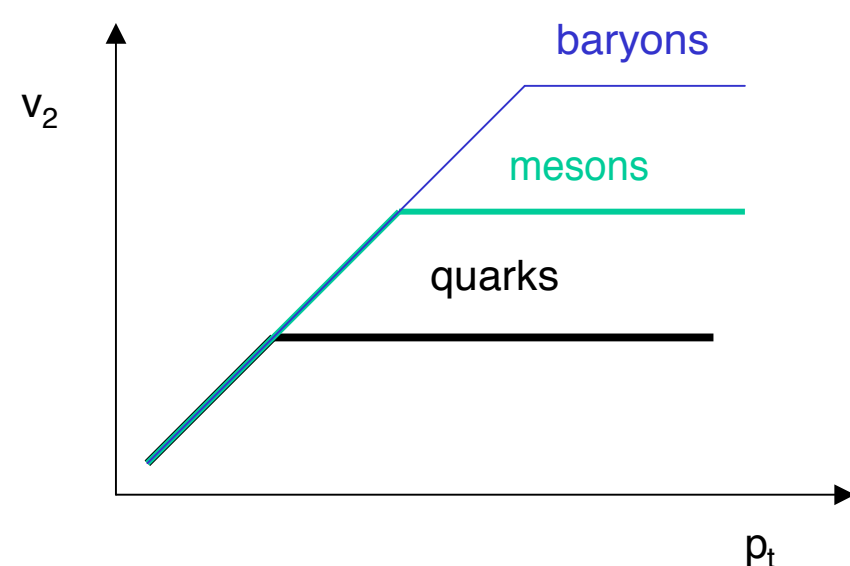
Constituent quark scaling

Quark coalescence?



Constituent quark scaling

Quark coalescence?



STAR Analysis meeting - 15

May 3 - 5, 2002

S.A. Voloshin



Constituent quark model + coalescence

coalescence

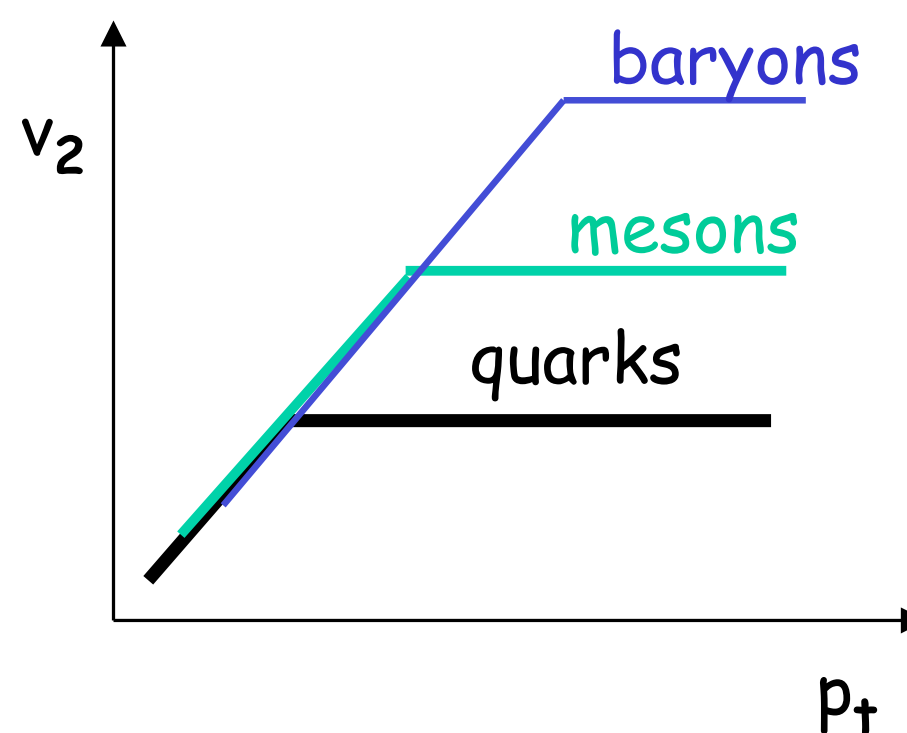
Low p_T quarks

fragmentation

High p_T quarks



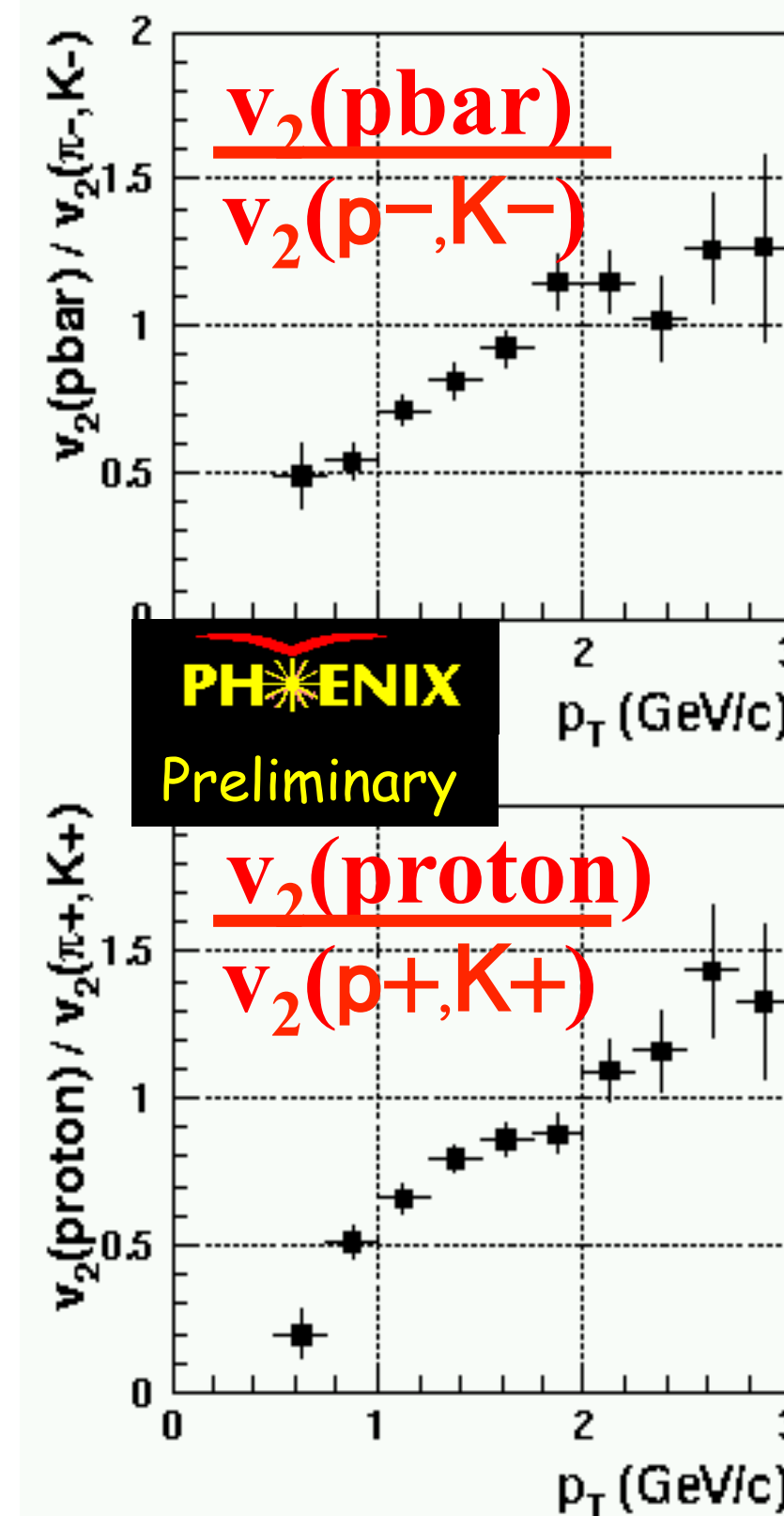
Coalescence in the intermediate region (rare products):



$$\frac{d^3 n_M}{d^3 p_M} \propto \left[\frac{d^3 n_q}{d^3 p_q} (p_q \approx p_M / 2) \right]^2$$

Side-notes:

- a) more particles produced via coalescence vs parton fragmentation \rightarrow larger mean p_T ...
- b) \rightarrow higher baryon/meson ratio

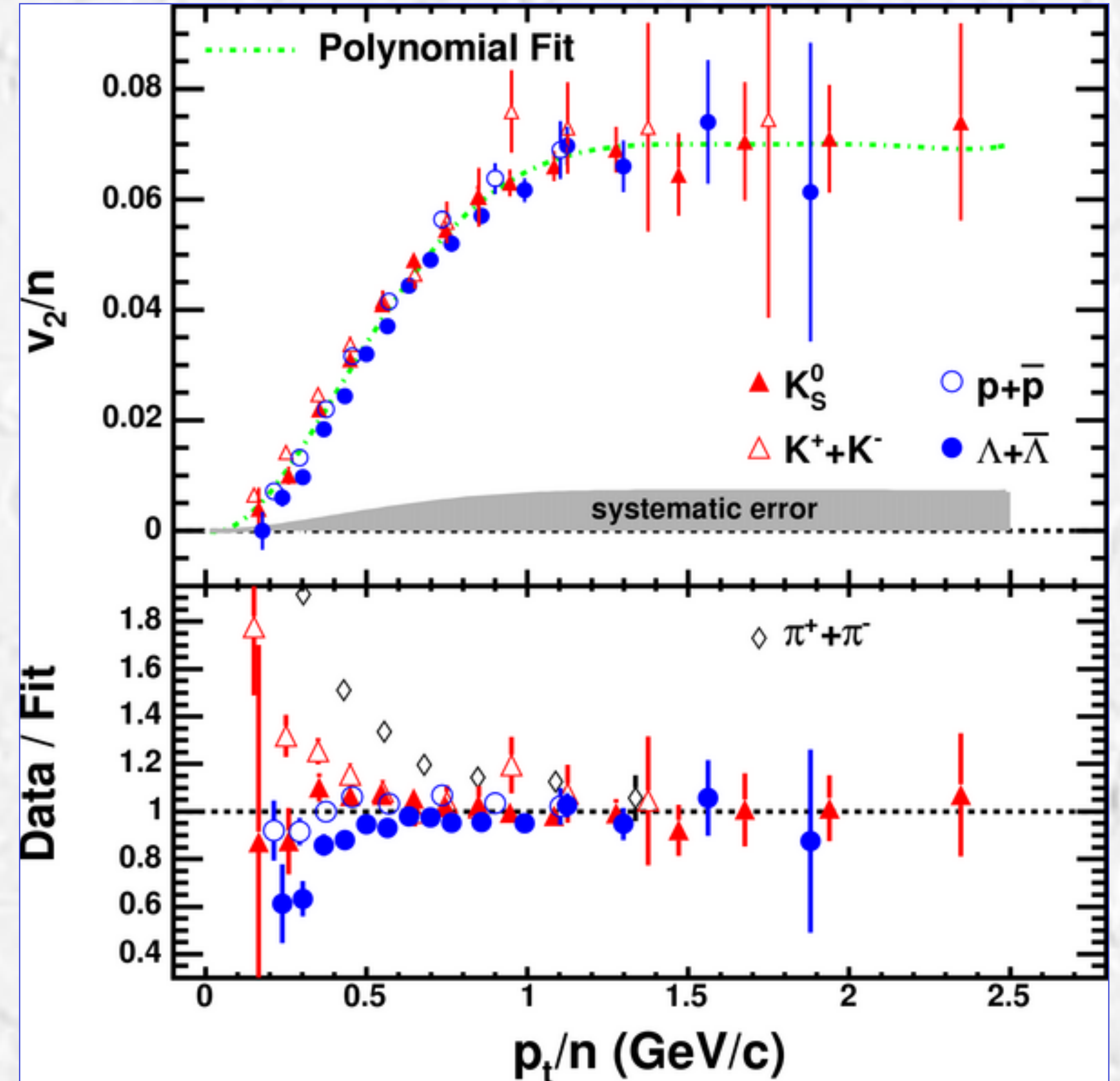
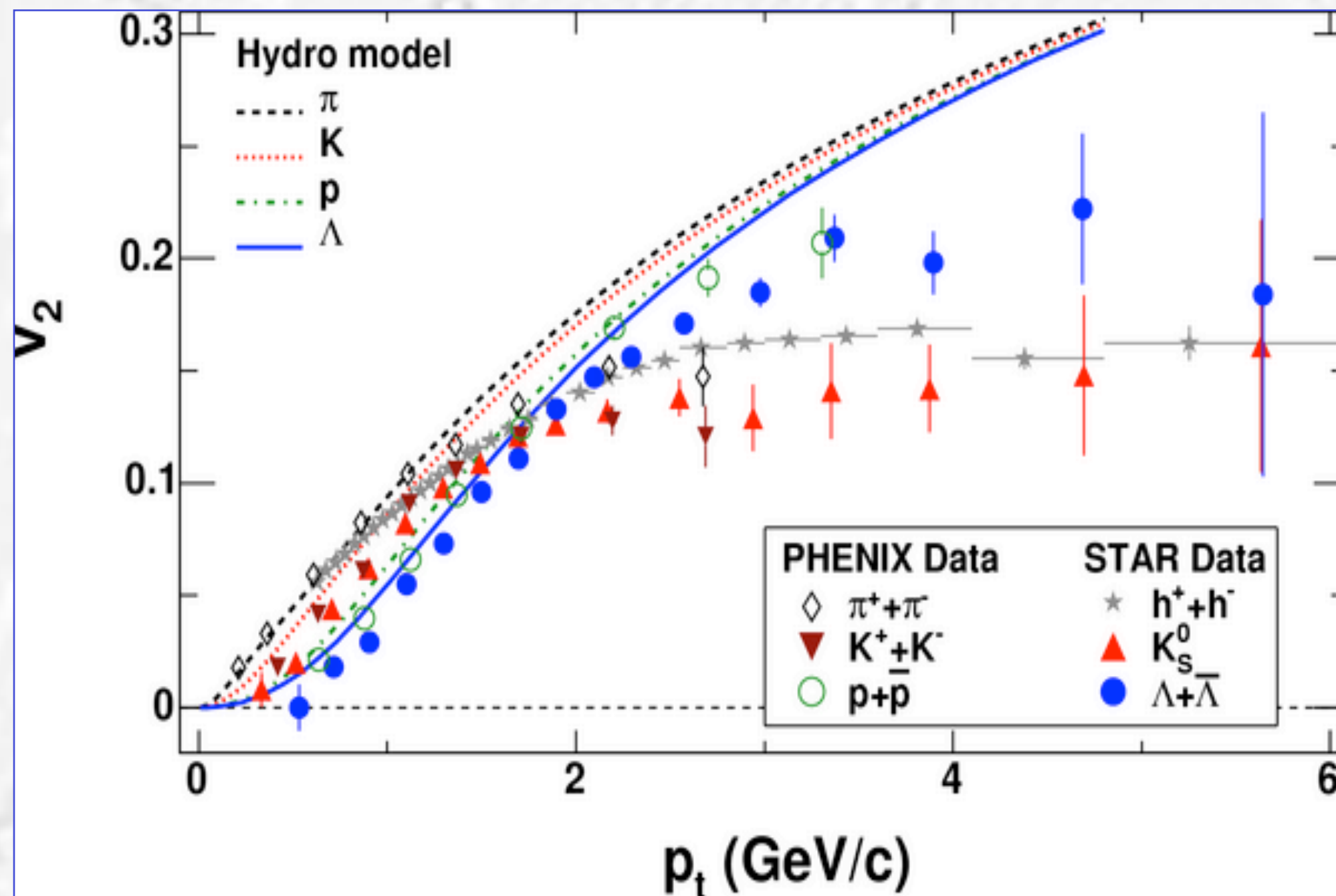
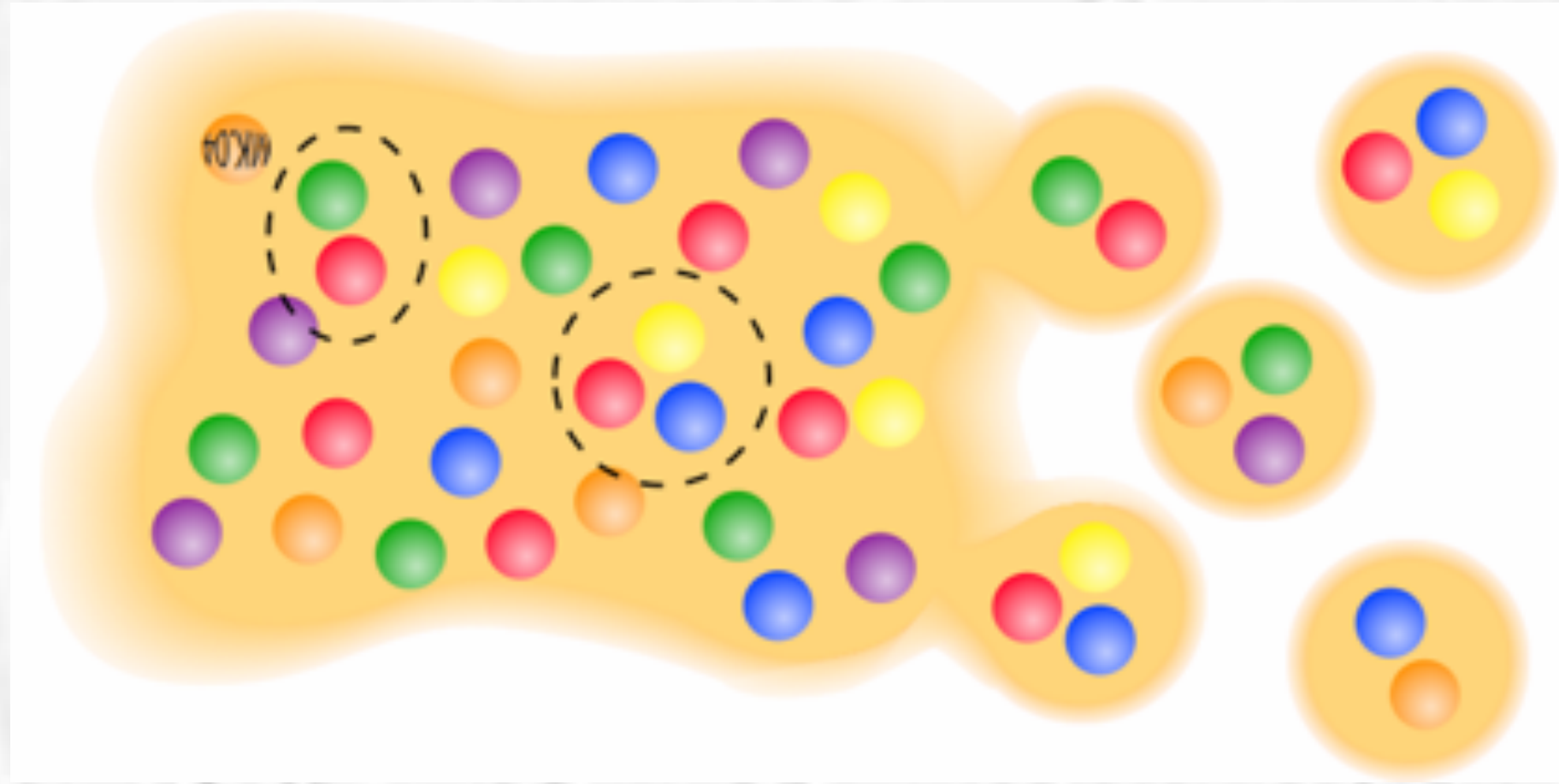


- What is the centrality dependence of the effect?

Quarks flow - deconfinement

STAR PRL 92(2004)052302

STAR, Phys Rev C (72), 014904 (2005)



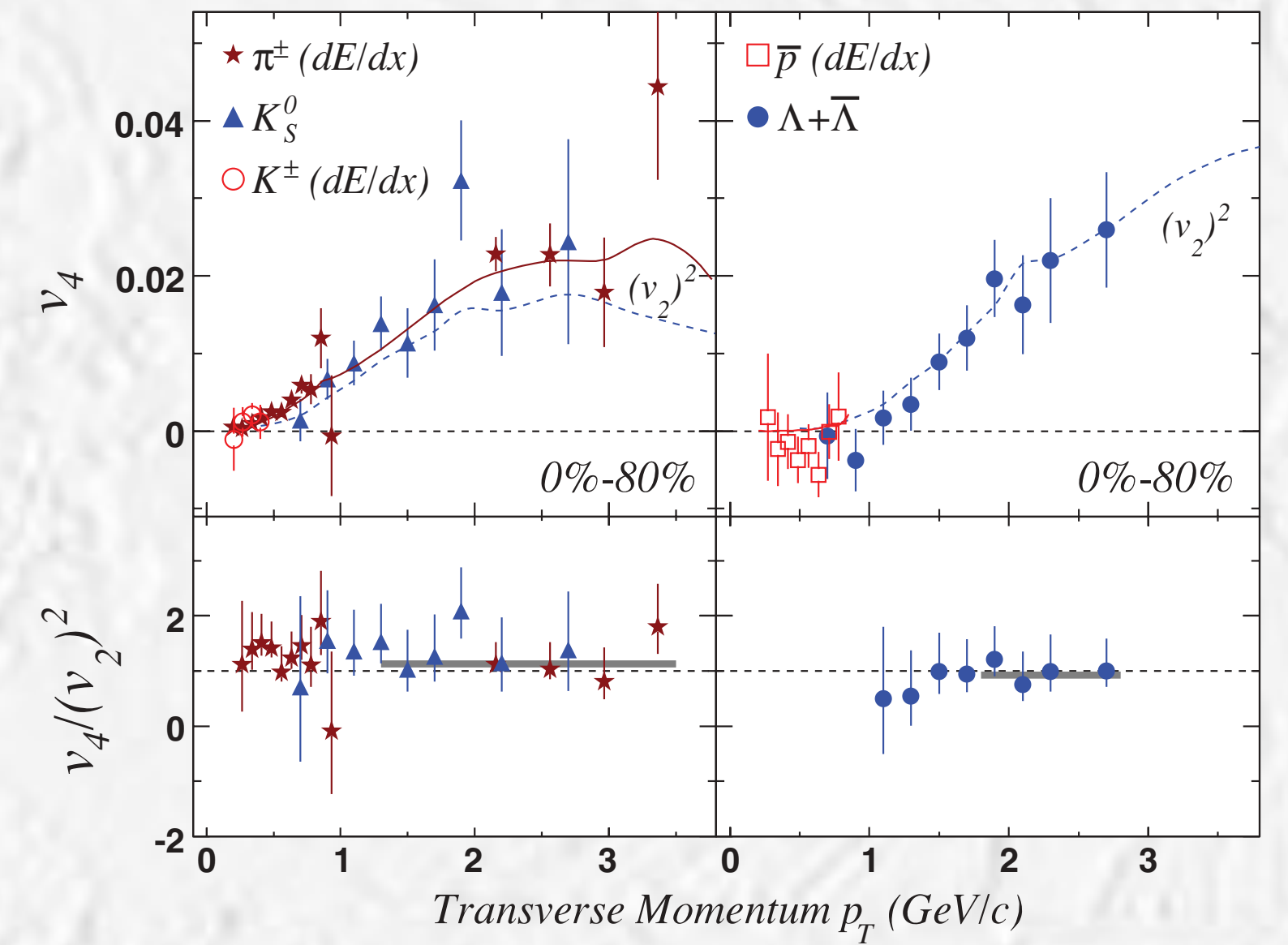
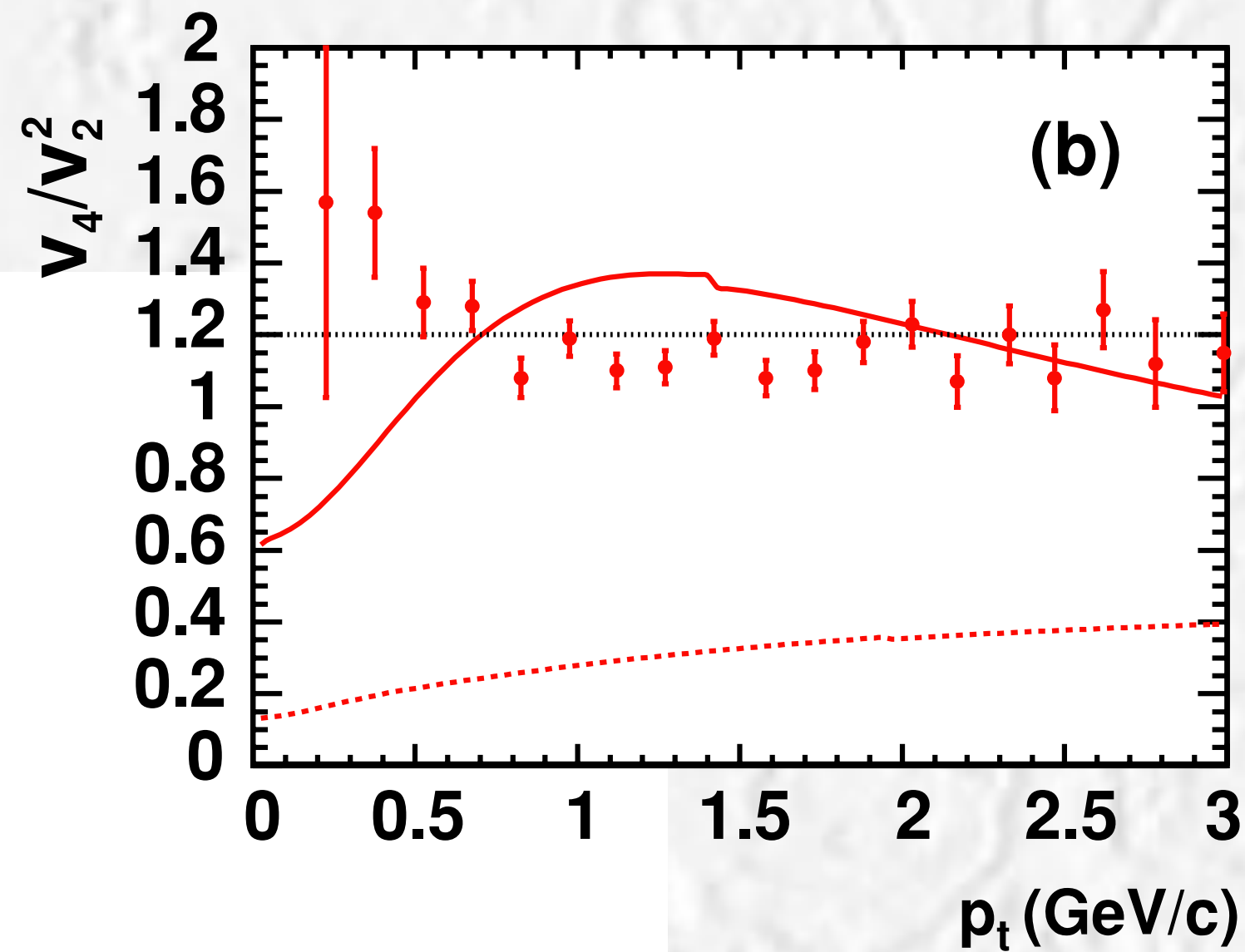
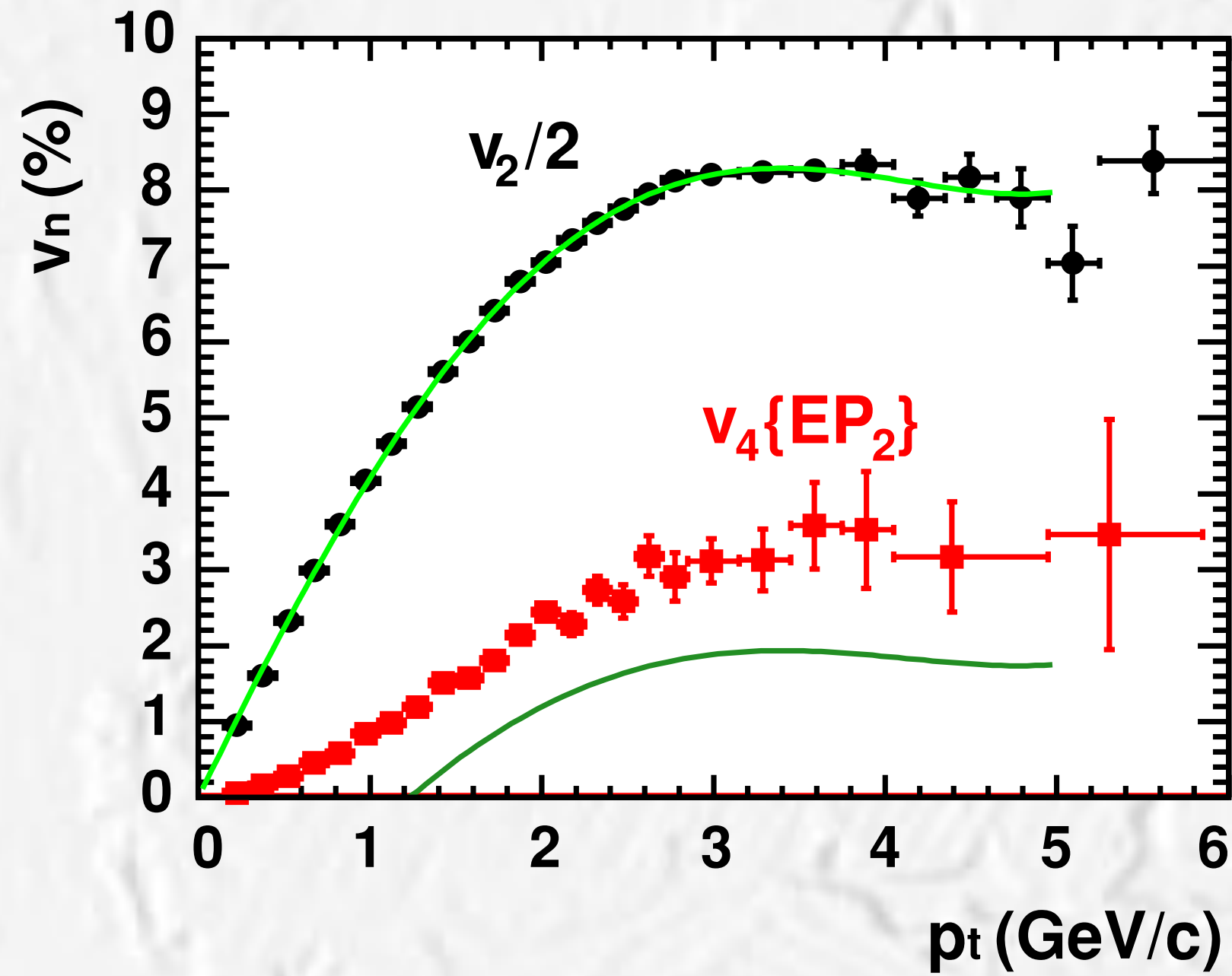
v_2 and v_4

PHYSICAL REVIEW C 75, 054906 (2007)

PHYSICAL REVIEW C 72, 014904 (2005)

Mass, quark-number, and $\sqrt{s_{NN}}$ dependence of the second and fourth flow harmonics in ultrarelativistic nucleus-nucleus collisions

Azimuthal anisotropy in Au+Au collisions at $\sqrt{s_{NN}} = 200$ GeV



Physical Review C 50th Anniversary Milestones



NCQ scaling in nonlinear flow modes



PUBLISHED FOR SISSA BY SPRINGER

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ACCEPTED: June 7, 2020

PUBLISHED: June 24, 2020

Non-linear flow modes of identified particles in Pb-Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV



ALICE
The ALICE collaboration

$$V_n = v_n e^{in\Psi_n}$$

$$V_4 = V_4^L + V_4^{NL} = V_4^L + \chi_{4,22} (V_2)^2,$$

Does the ratio of baryon and meson flow in nonlinear modes equals to the square or first power of that in linear parts?

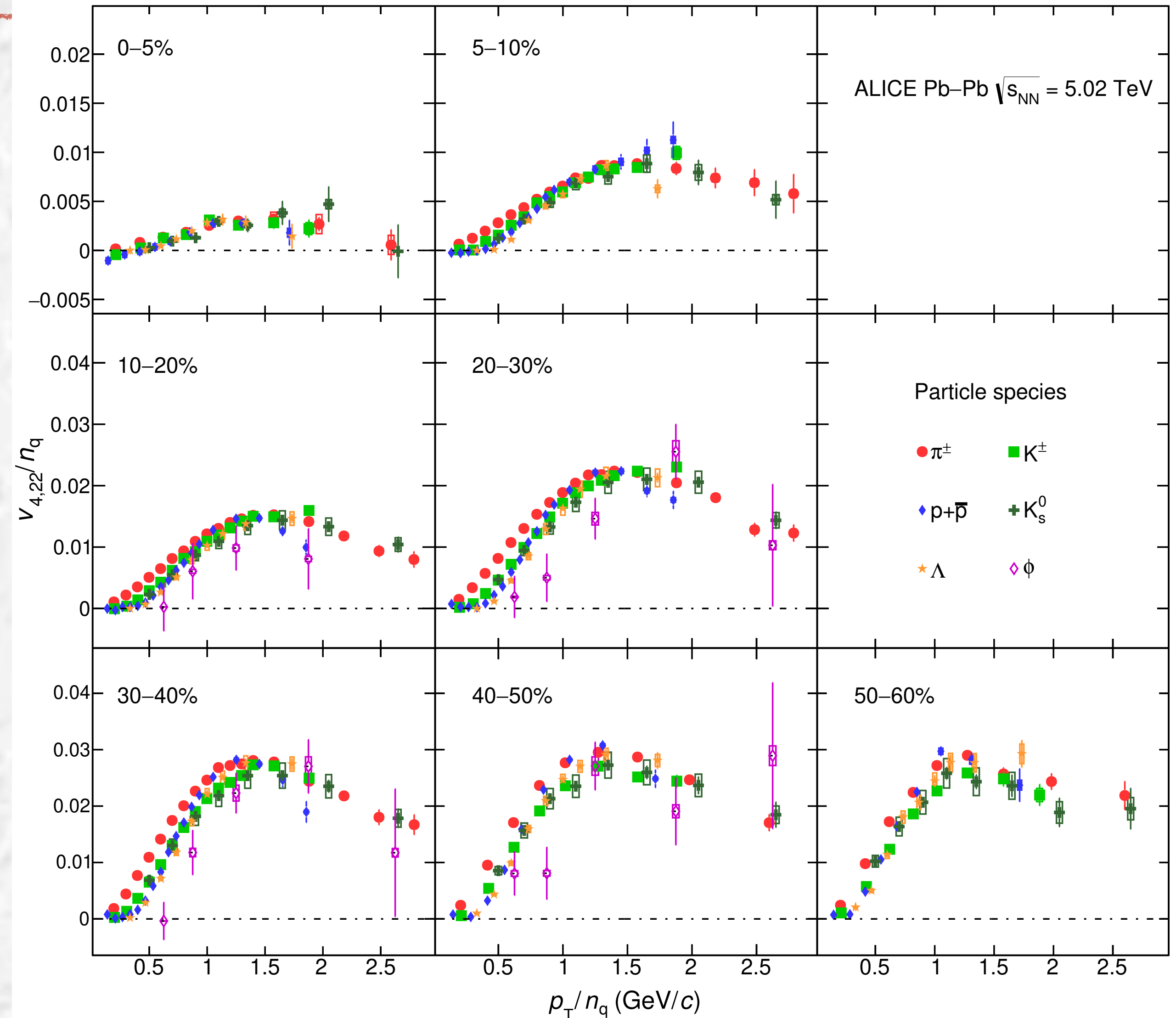


Figure 10. The p_T/n_q -dependence of $v_{4,22}/n_q$ for different particle species grouped into different centrality intervals of Pb-Pb collisions at $\sqrt{s_{NN}} = 5.02$ TeV. Statistical and systematic uncertainties are shown as bars and boxes, respectively.

Flow and Non-flow

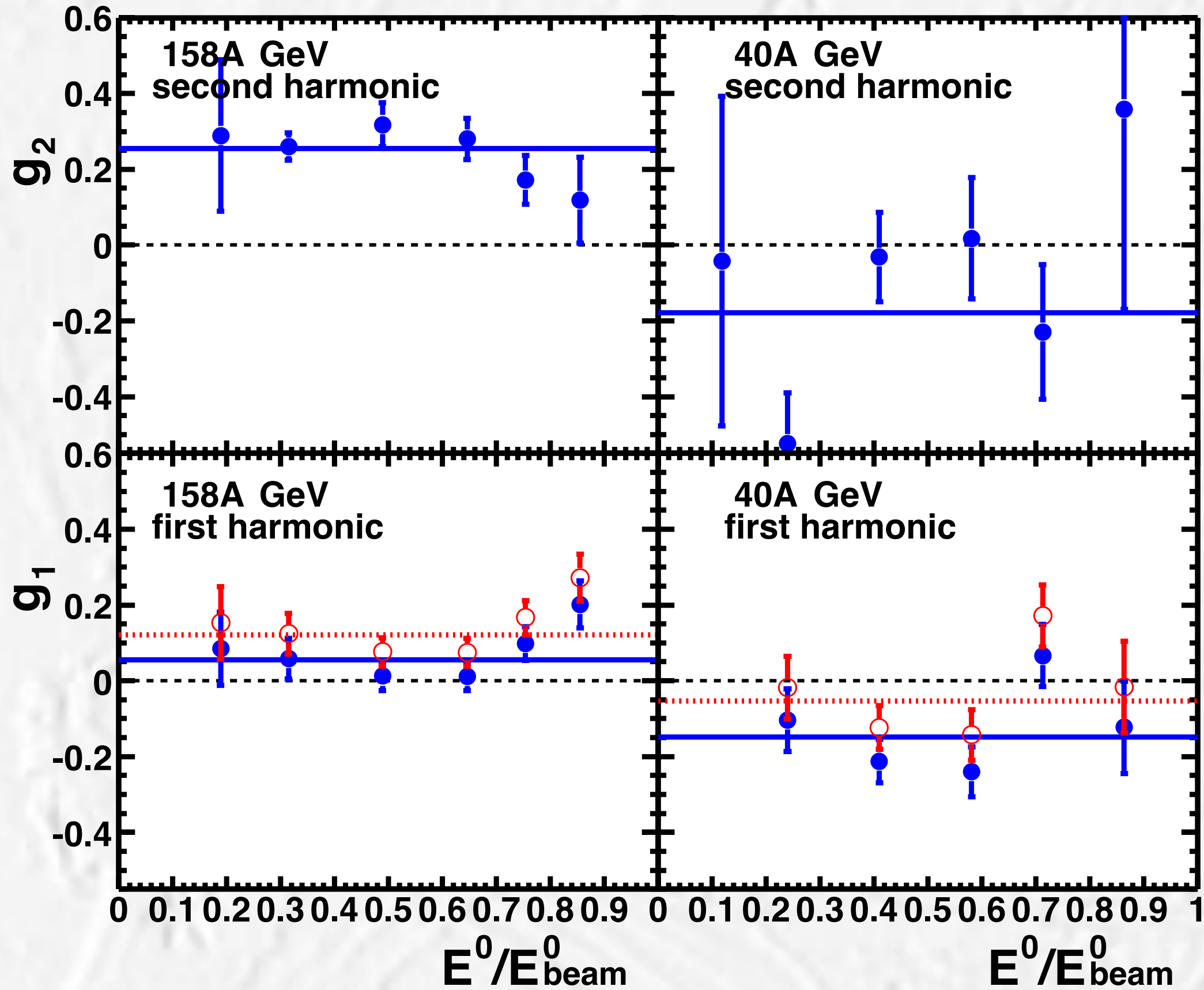


FIG. 22. (Color online) Nonflow azimuthal correlations from Eq. (16), for the first, g_1 , (bottom) and second, g_2 , (top) Fourier harmonics, from 158A GeV (left) and 40A GeV (right) Pb+Pb collisions. For g_1 , the solid points represent all nonflow effects, while the open points are corrected for momentum conservation. The horizontal lines are at the mean values.

\

$$\langle v_2^2 \rangle = \langle v_2 \rangle^2 + \sigma_{v_2}^2 + g_2/N$$

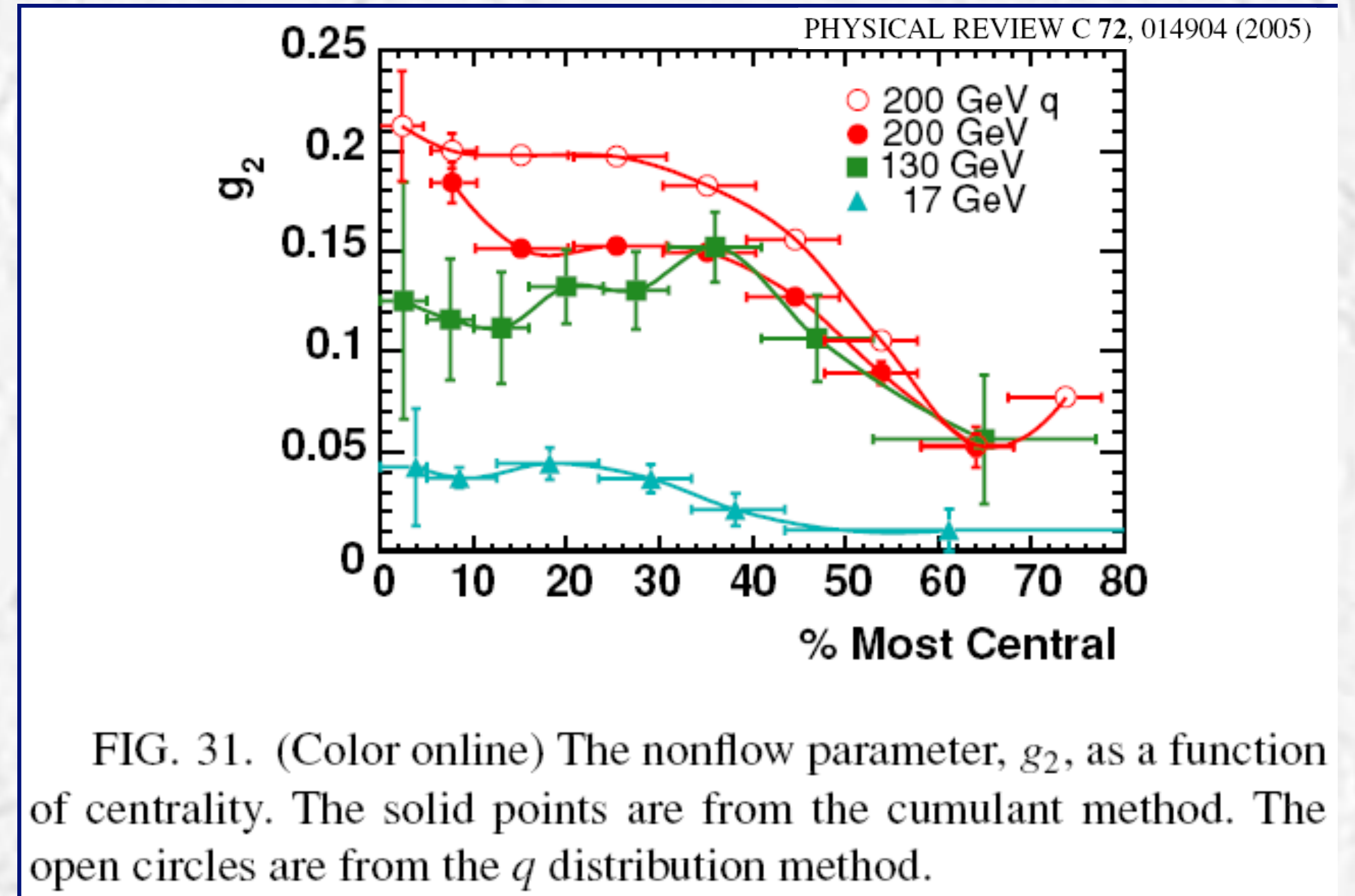
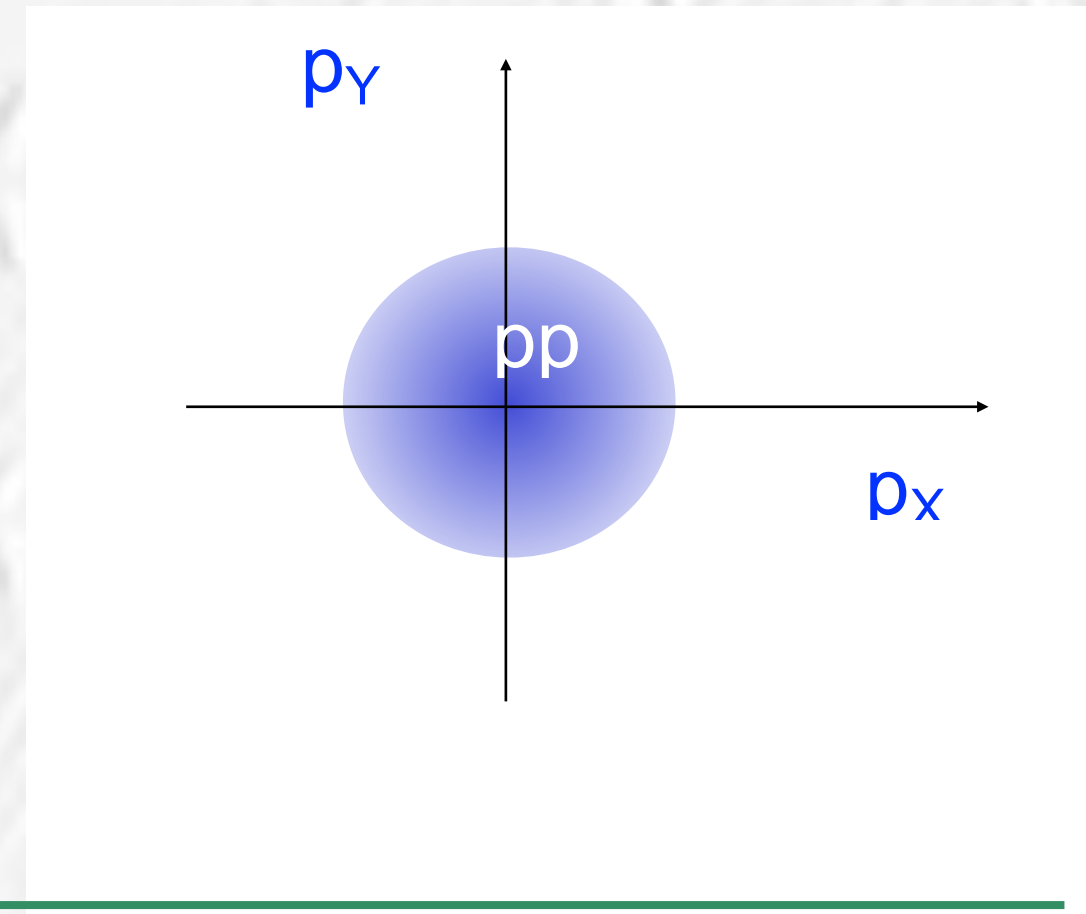
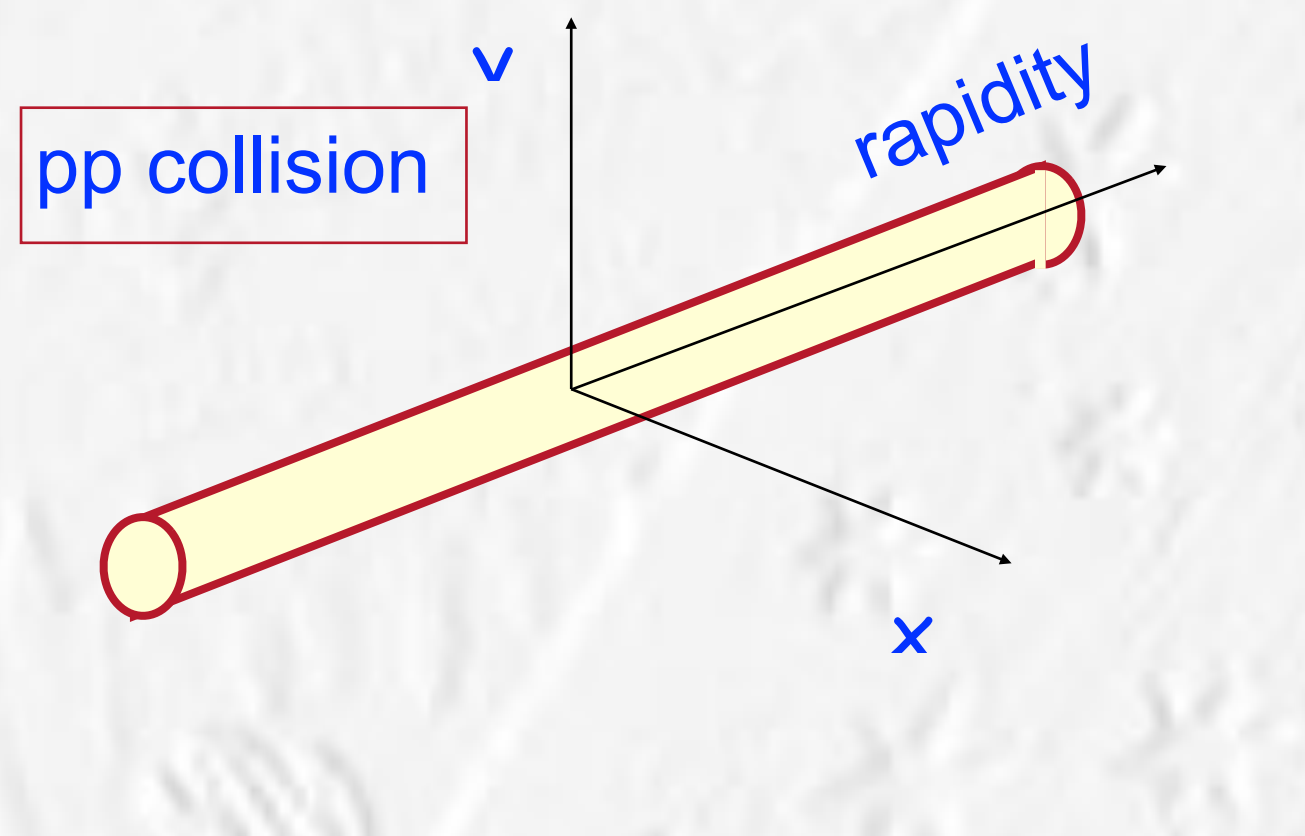


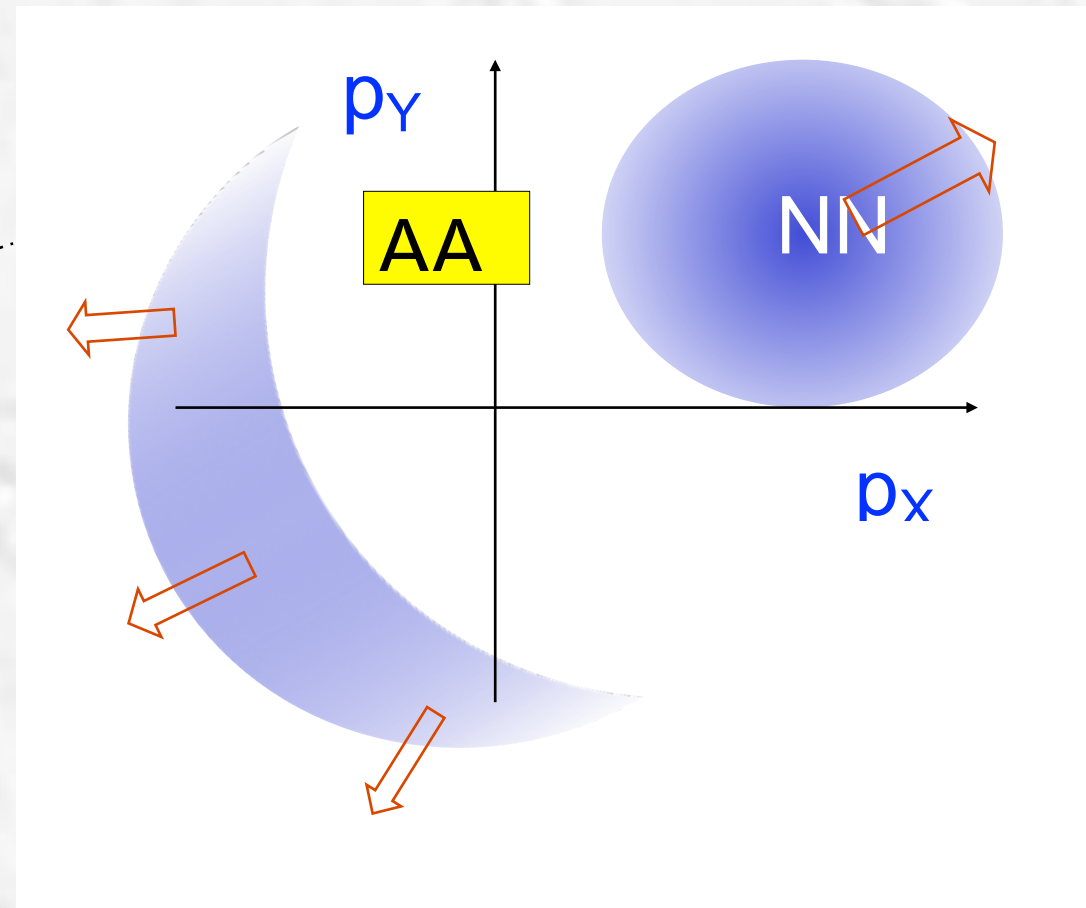
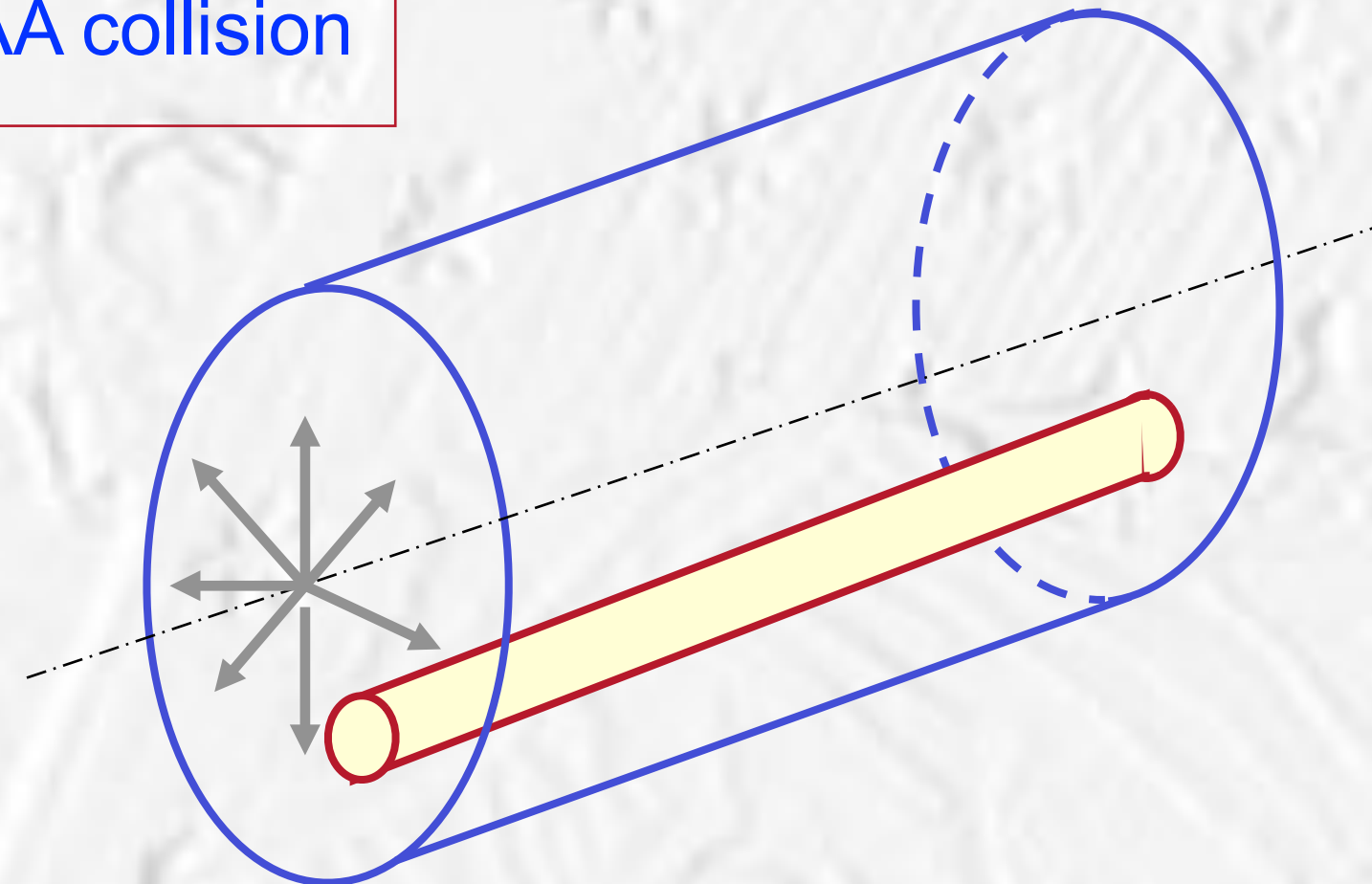
FIG. 31. (Color online) The nonflow parameter, g_2 , as a function of centrality. The solid points are from the cumulant method. The open circles are from the q distribution method.

Radial expansion \rightarrow nonflow

[arXiv:nucl-th/0312065]

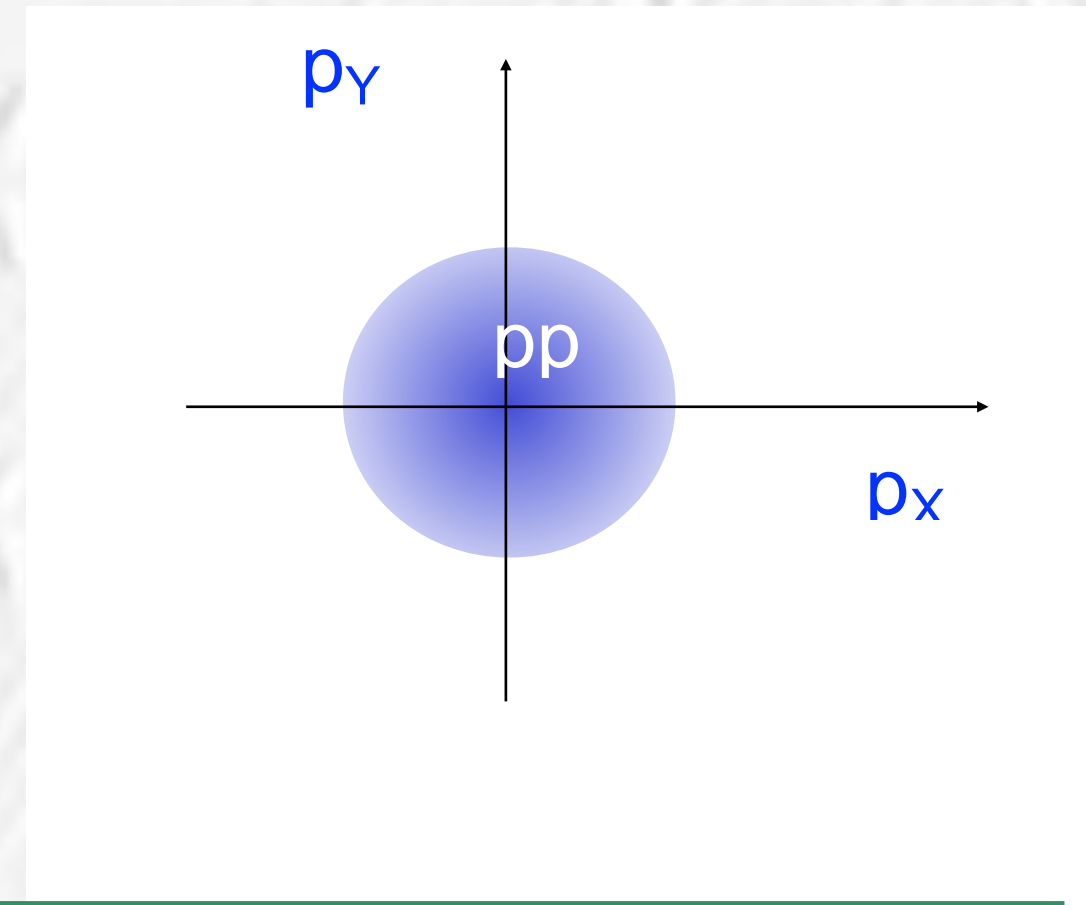
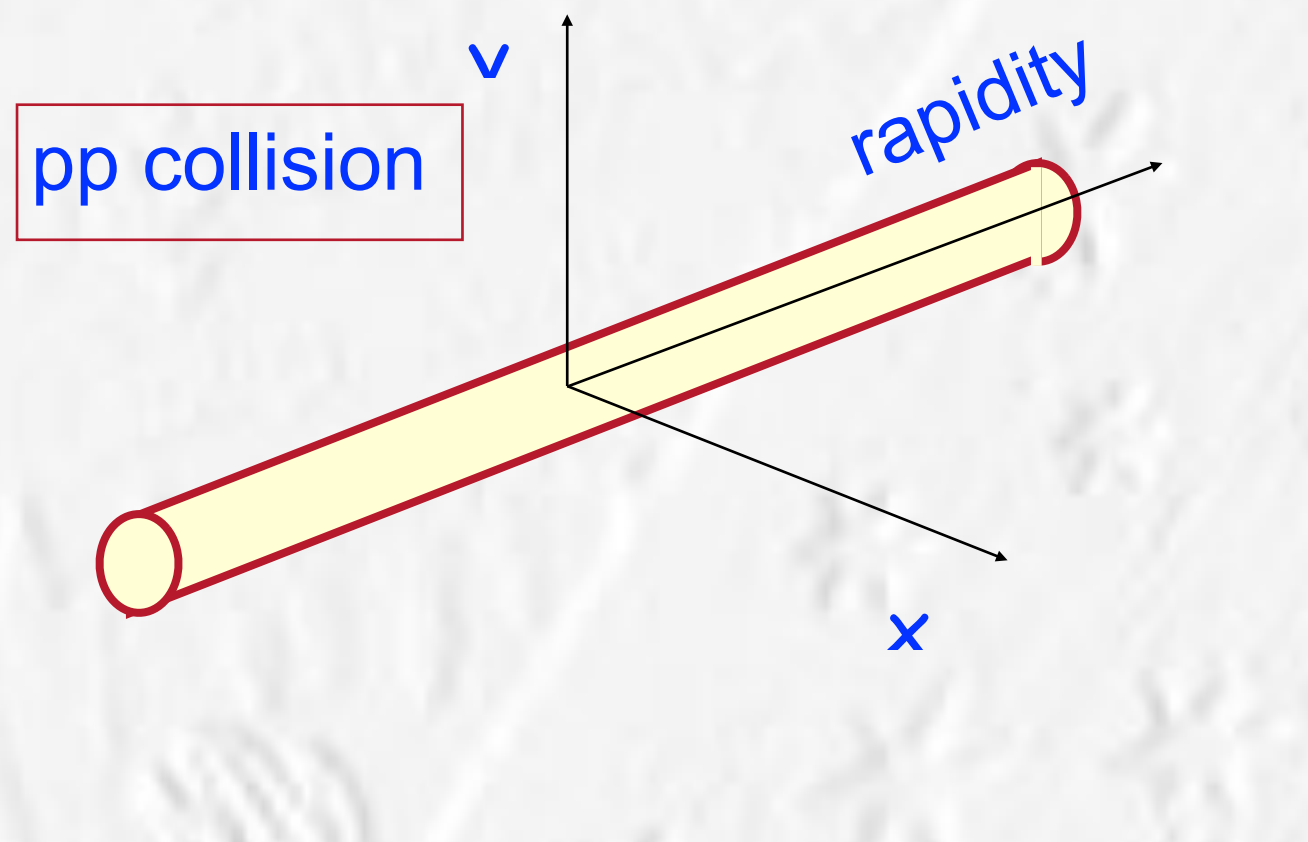


AA collision

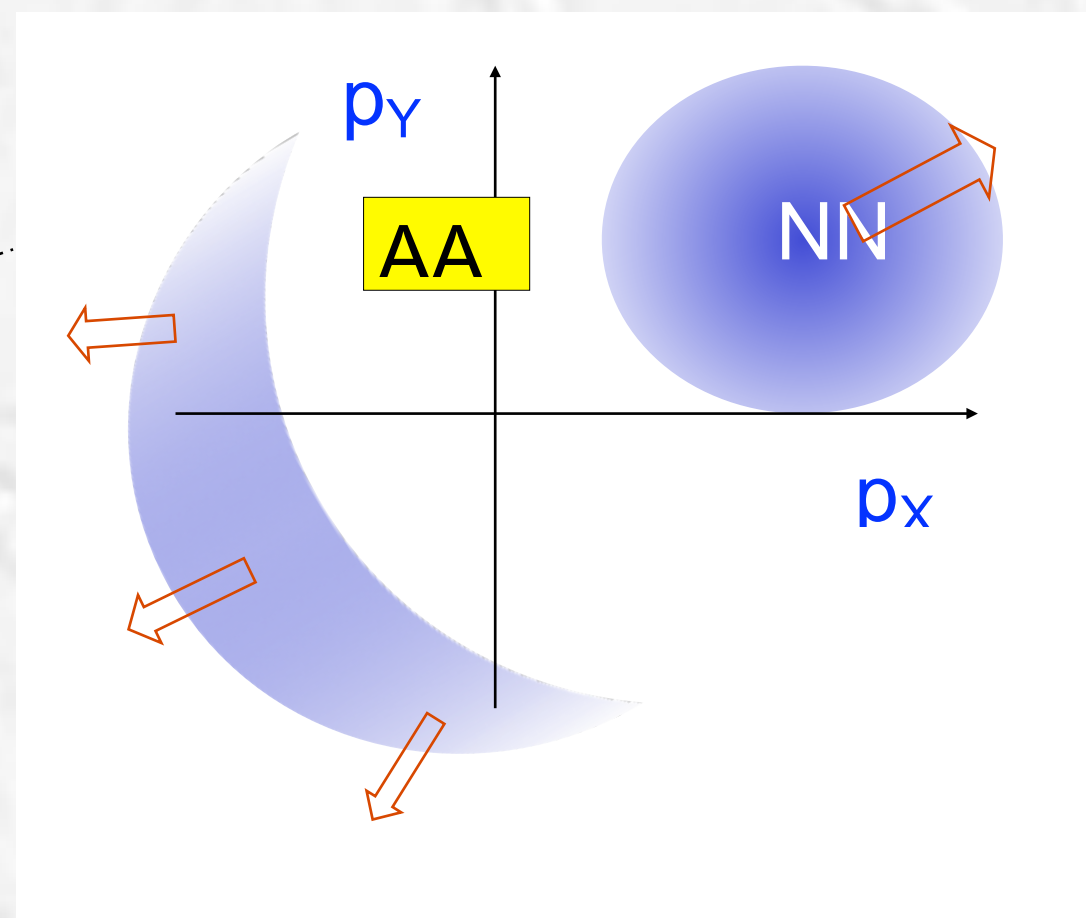
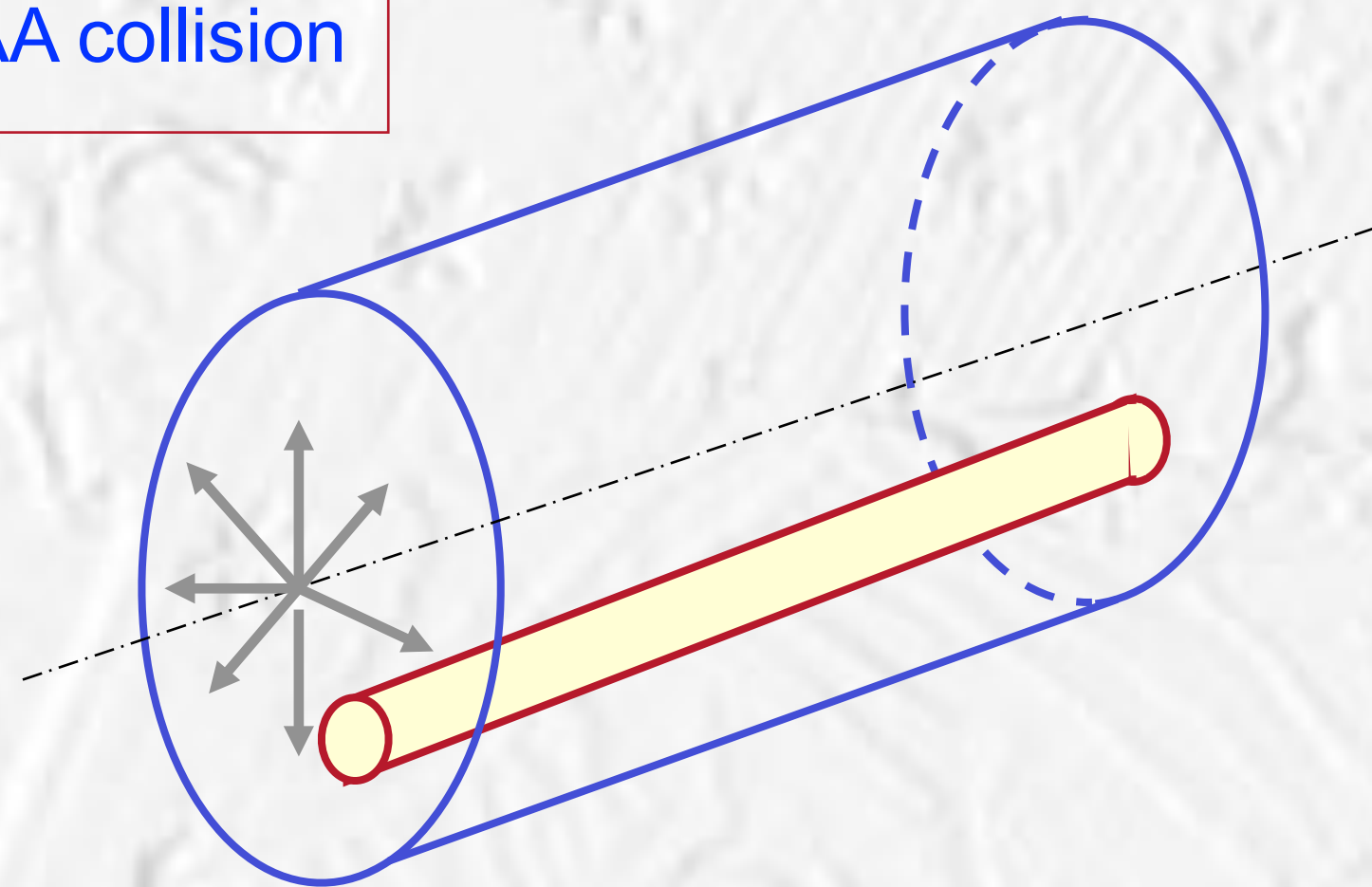


Radial expansion → nonflow

[arXiv:nucl-th/0312065]



AA collision



arXiv:nucl-ex/0301014v1 24 Jan 2003

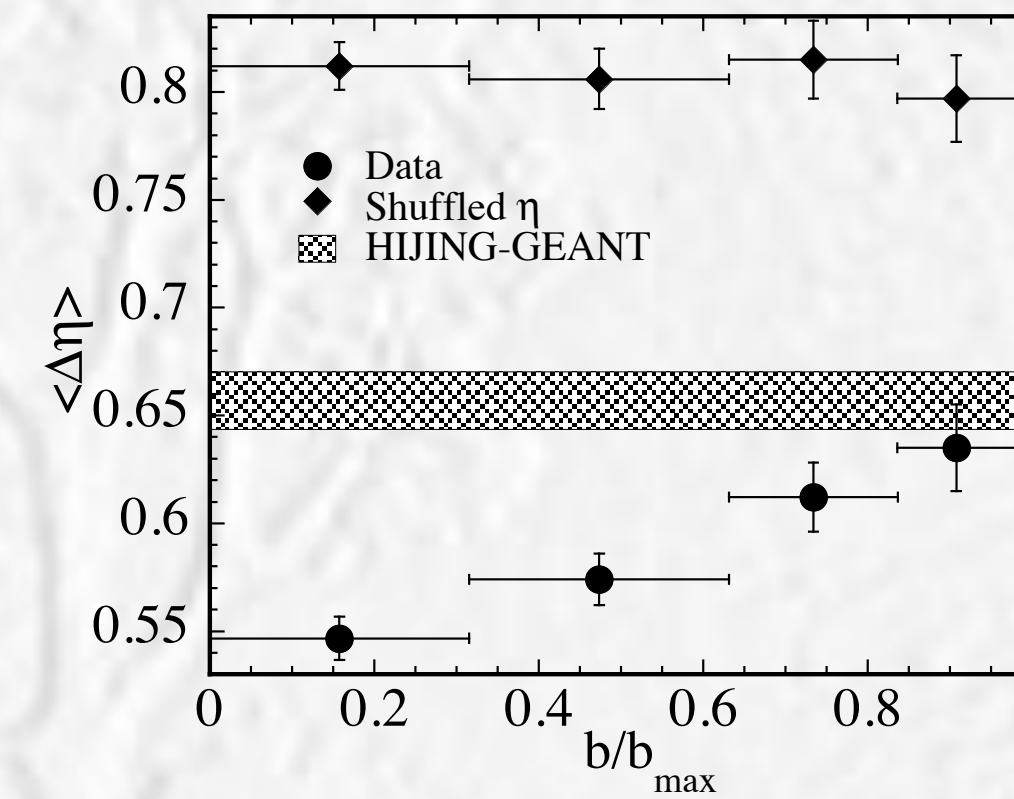
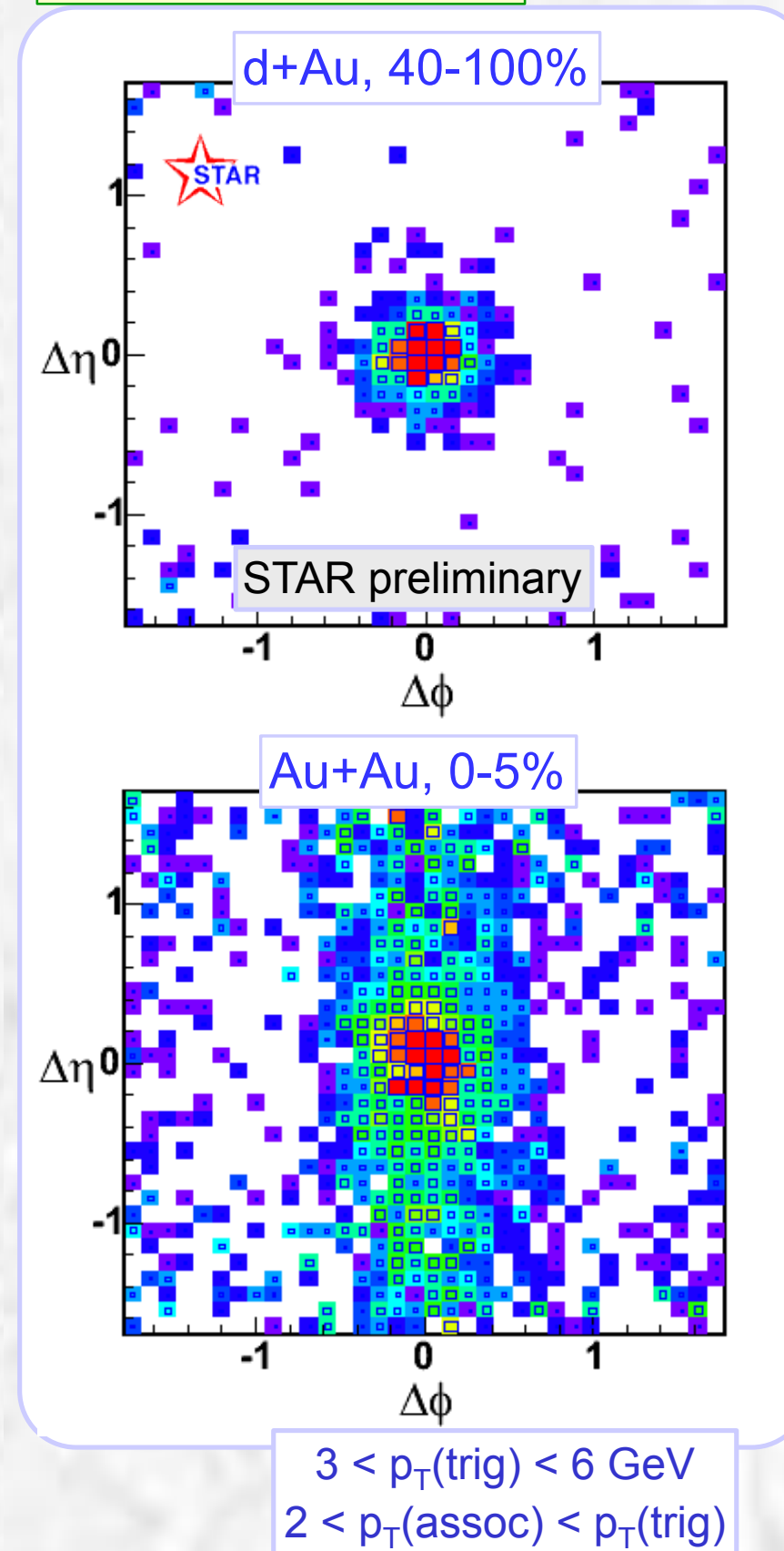
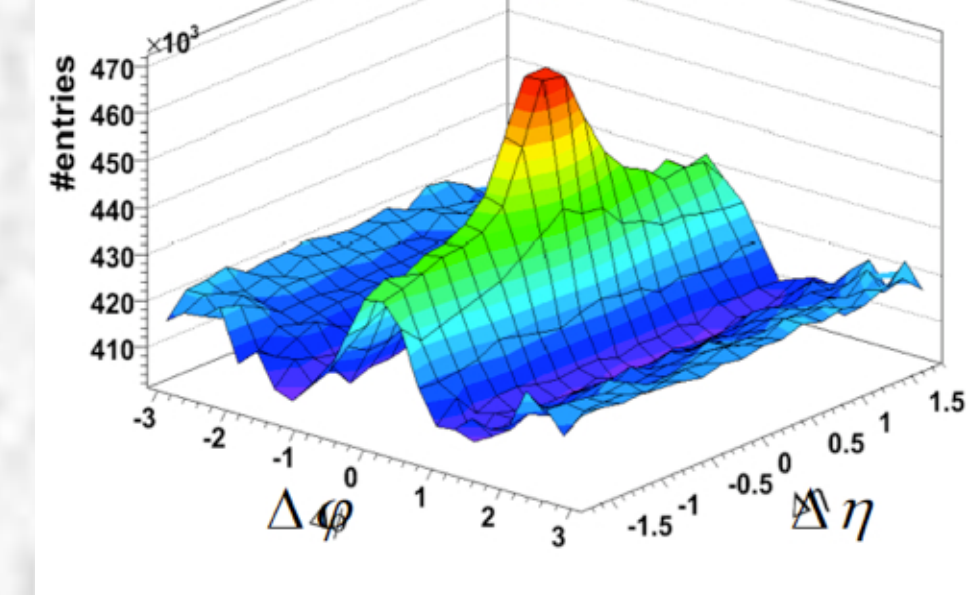


FIG. 2: The width of the balance function for charged particles, $\langle \Delta\eta \rangle$, as a function of normalized impact parameter b/b_{max} . Error bars shown are statistical. The width of the balance function from HIJING events is shown as a band whose height reflects the statistical uncertainty. Also shown are the widths from the shuffled pseudorapidity events.

D. Magestro (STAR) - Hard Probes 2004



B. I. Abelev et al. [STAR Collaboration], Phys. Rev. C 80 (2009) 6491



Radial expansion → nonflow, cont'd

S.A. Voloshin / *Physics Letters B* 632 (2006) 490–494

493

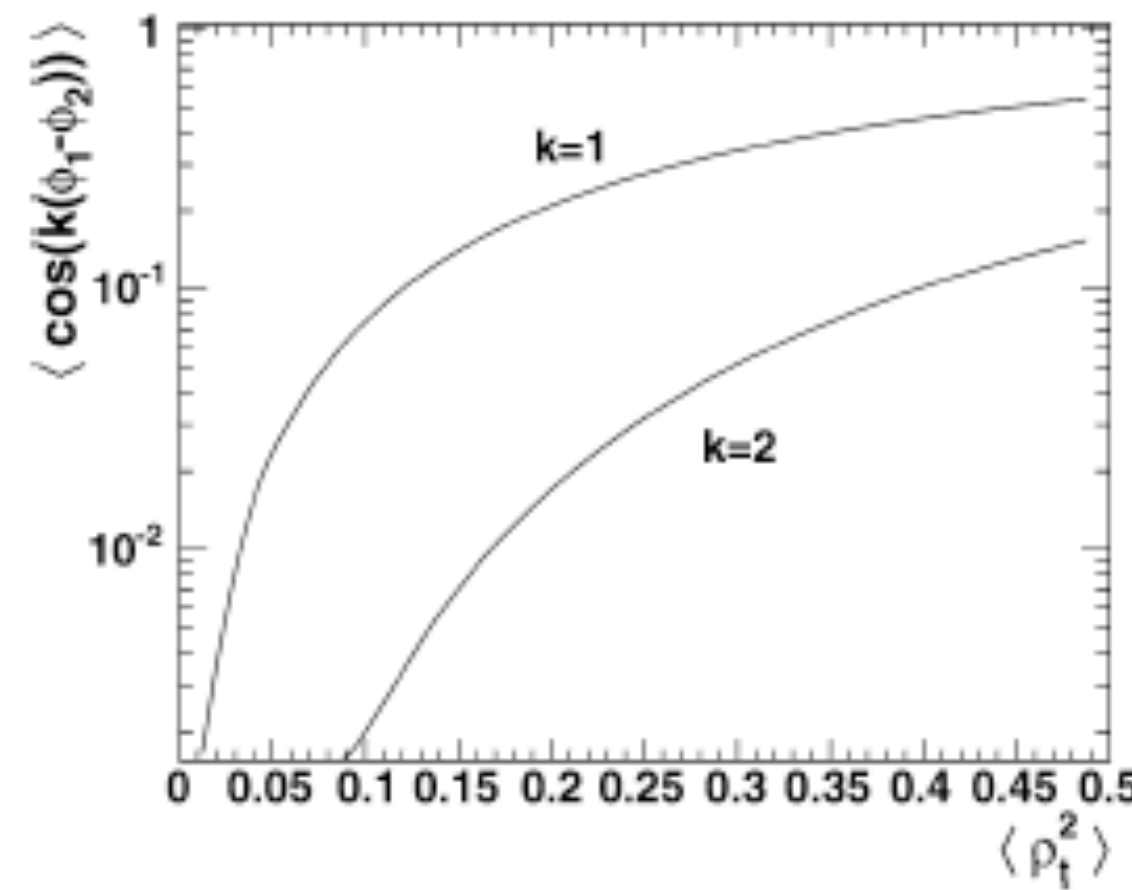
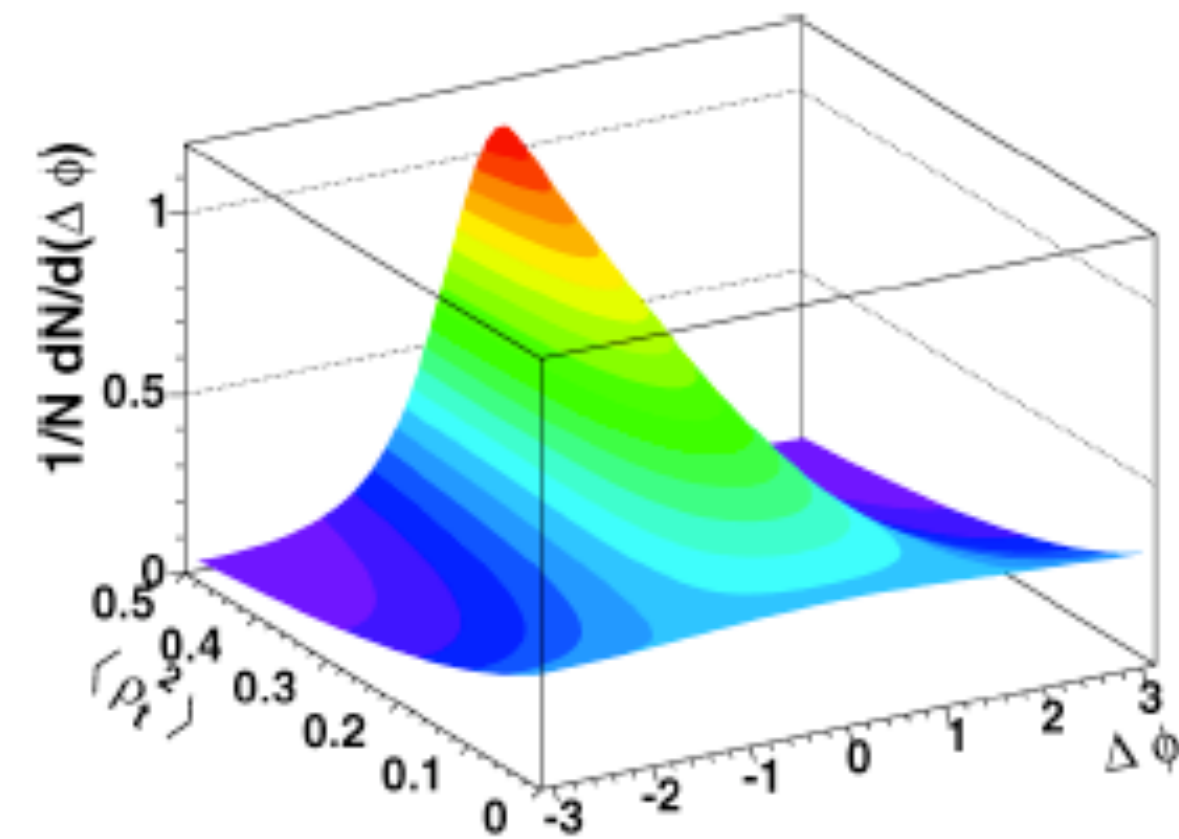


Fig. 3. (Color online.) Two pion $\Delta\phi$ distribution as function of $\langle\rho_t^2\rangle$ in the blast wave model. Linear velocity profile and $T = 110$ MeV have been assumed.

Fig. 4. The average values of $\cos(\Delta\phi)$ and $\cos(2\Delta\phi)$ for the distribution shown in Fig. 3.

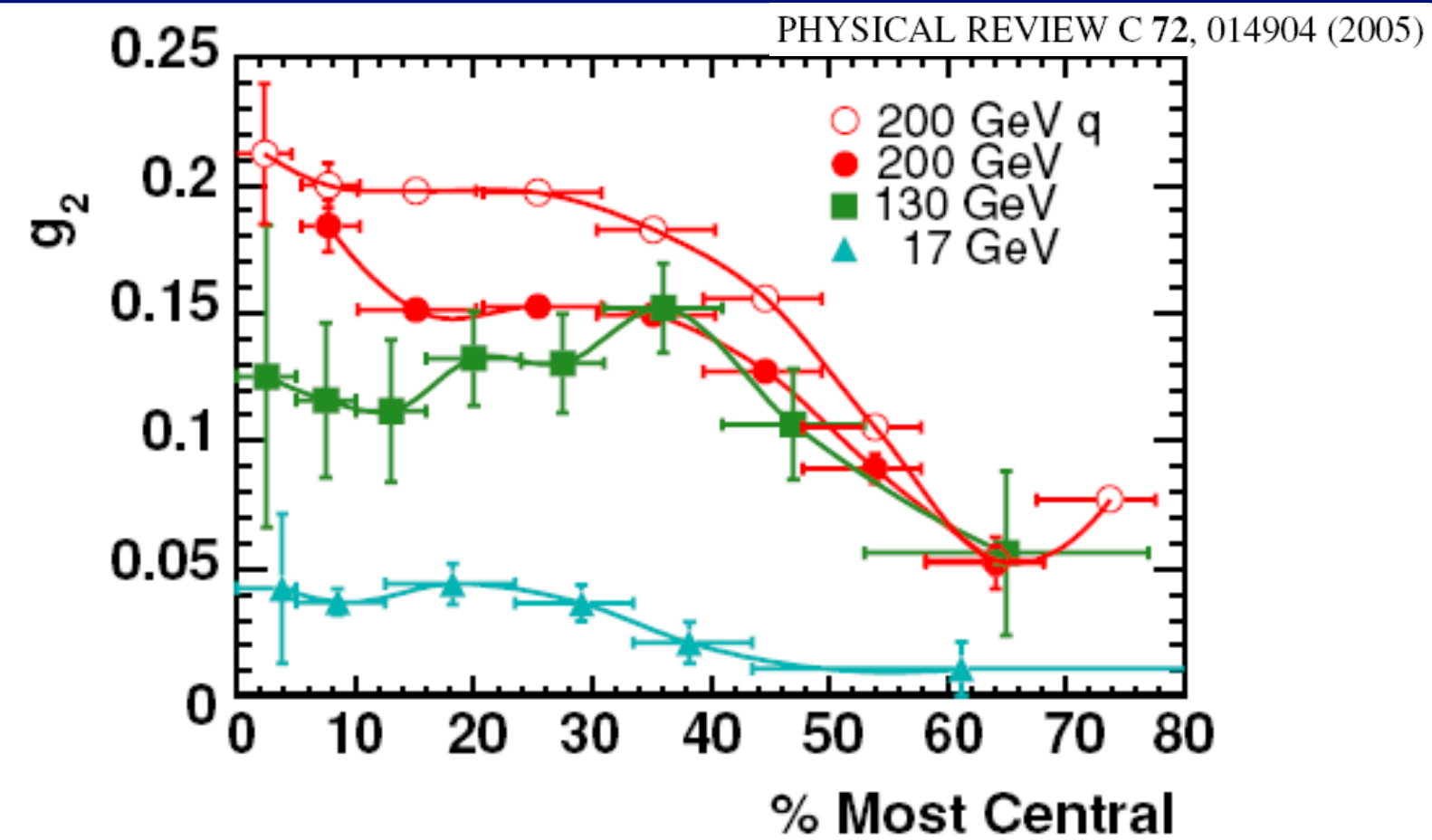


FIG. 31. (Color online) The nonflow parameter, g_2 , as a function of centrality. The solid points are from the cumulant method. The open circles are from the q distribution method.

!!! - the large values of transverse flow, $\rho_t^2 > 0.25$, would contradict “non-flow” estimates in elliptic flow measurements

Flow fluctuations

$$\langle v_2^2 \rangle = \langle v_2 \rangle^2 + \sigma_{v_2}^2 + g_2/N$$

The difference between two-particle and many-particle correlation results are due to **flow fluctuations** and nonflow.

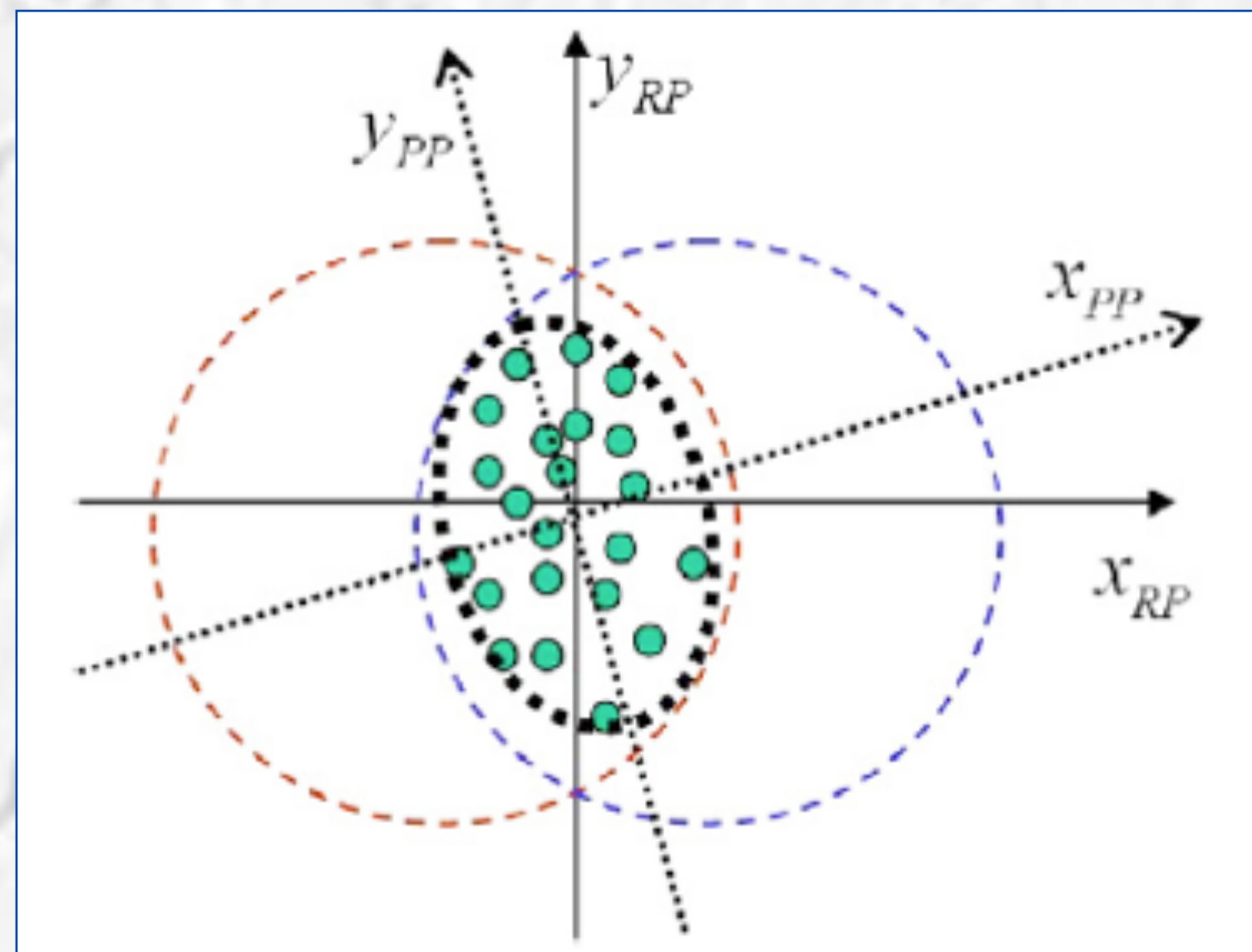
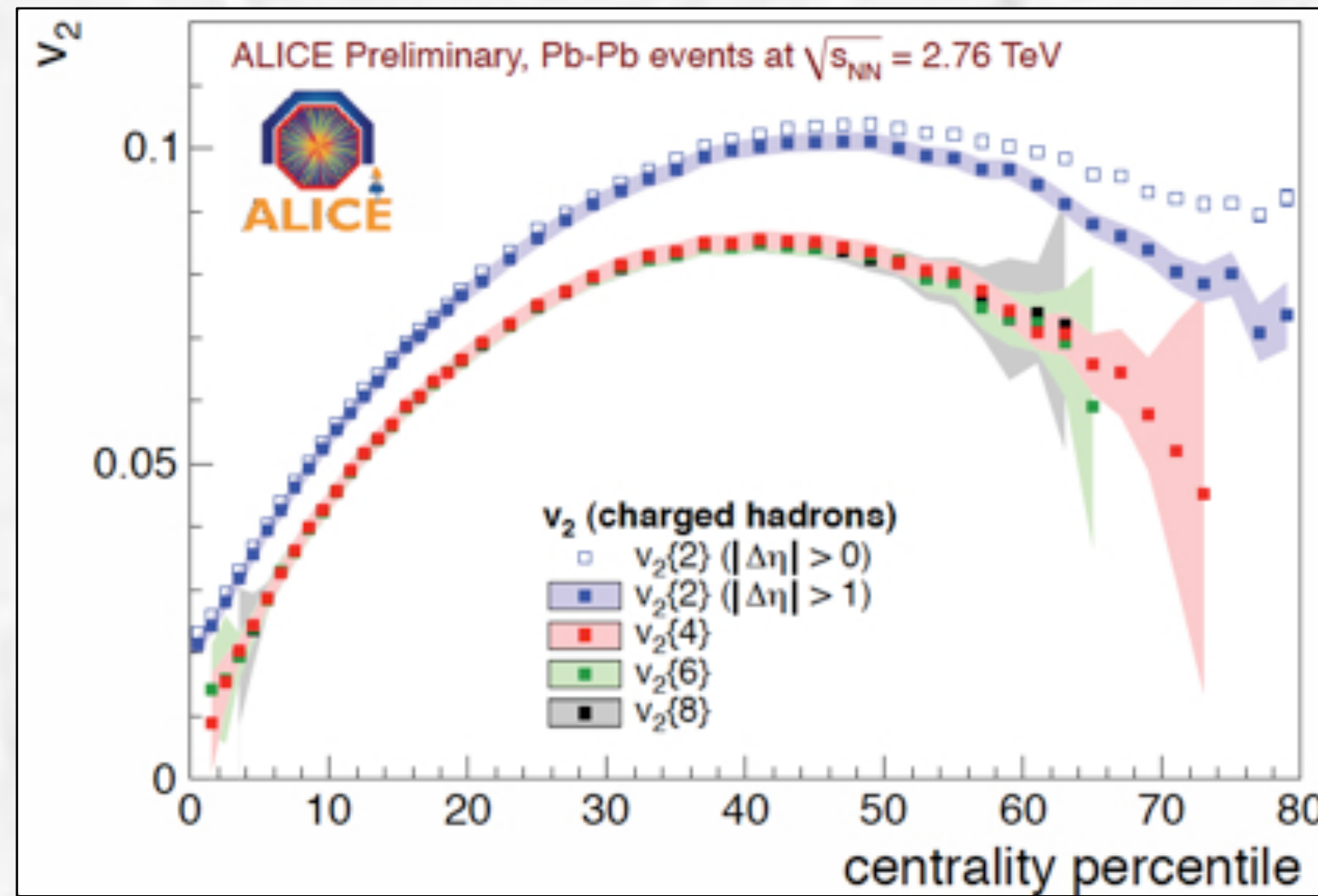
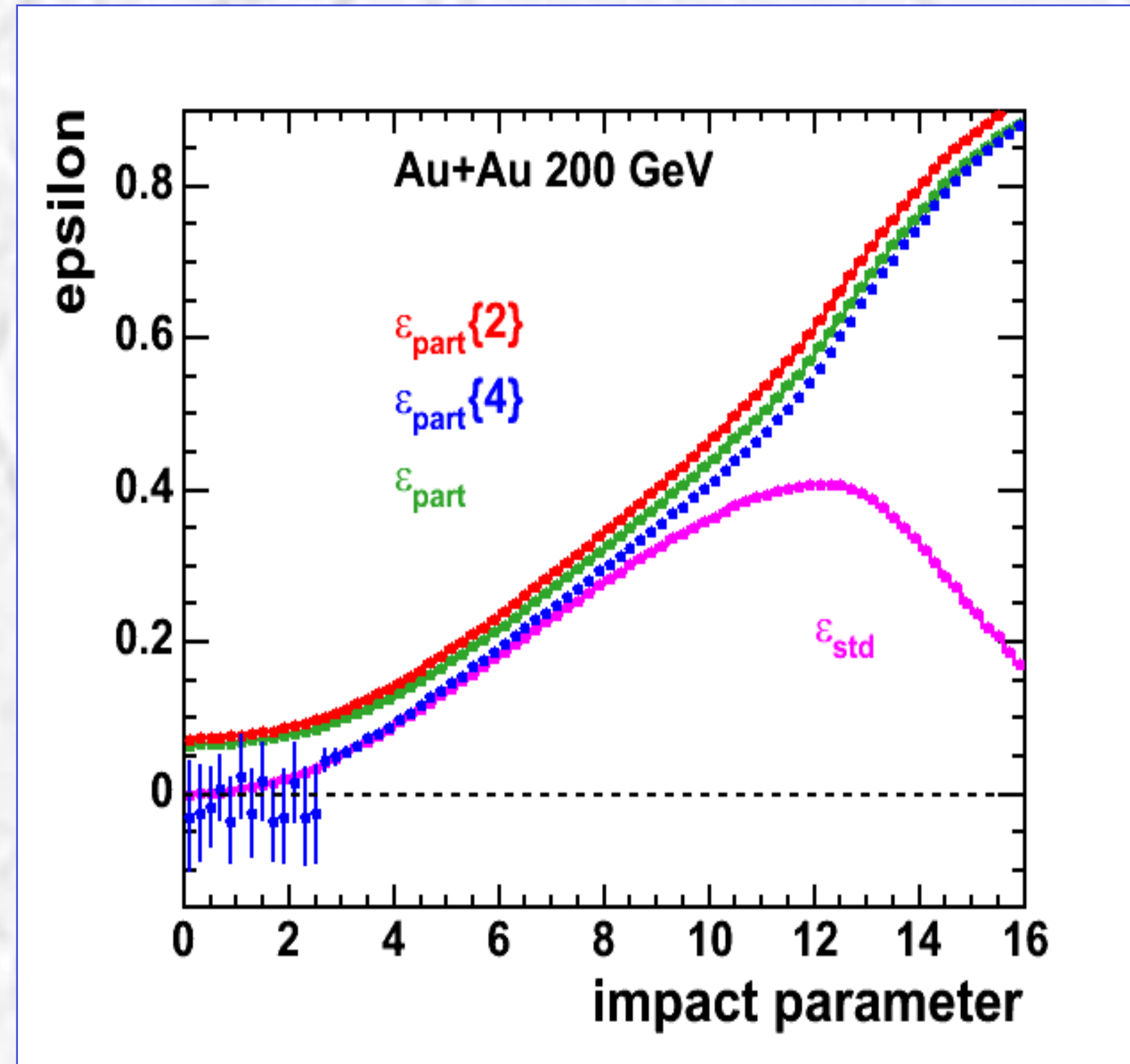


Fig. 1. The definitions of the *RP* and *PP* coordinate systems.

$$\epsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$



Flow fluctuations

$$\langle v_2^2 \rangle = \langle v_2 \rangle^2 + \sigma_{v_2}^2 + g_2/N$$

The difference between two-particle and many-particle correlation results are due to **flow fluctuations** and nonflow.

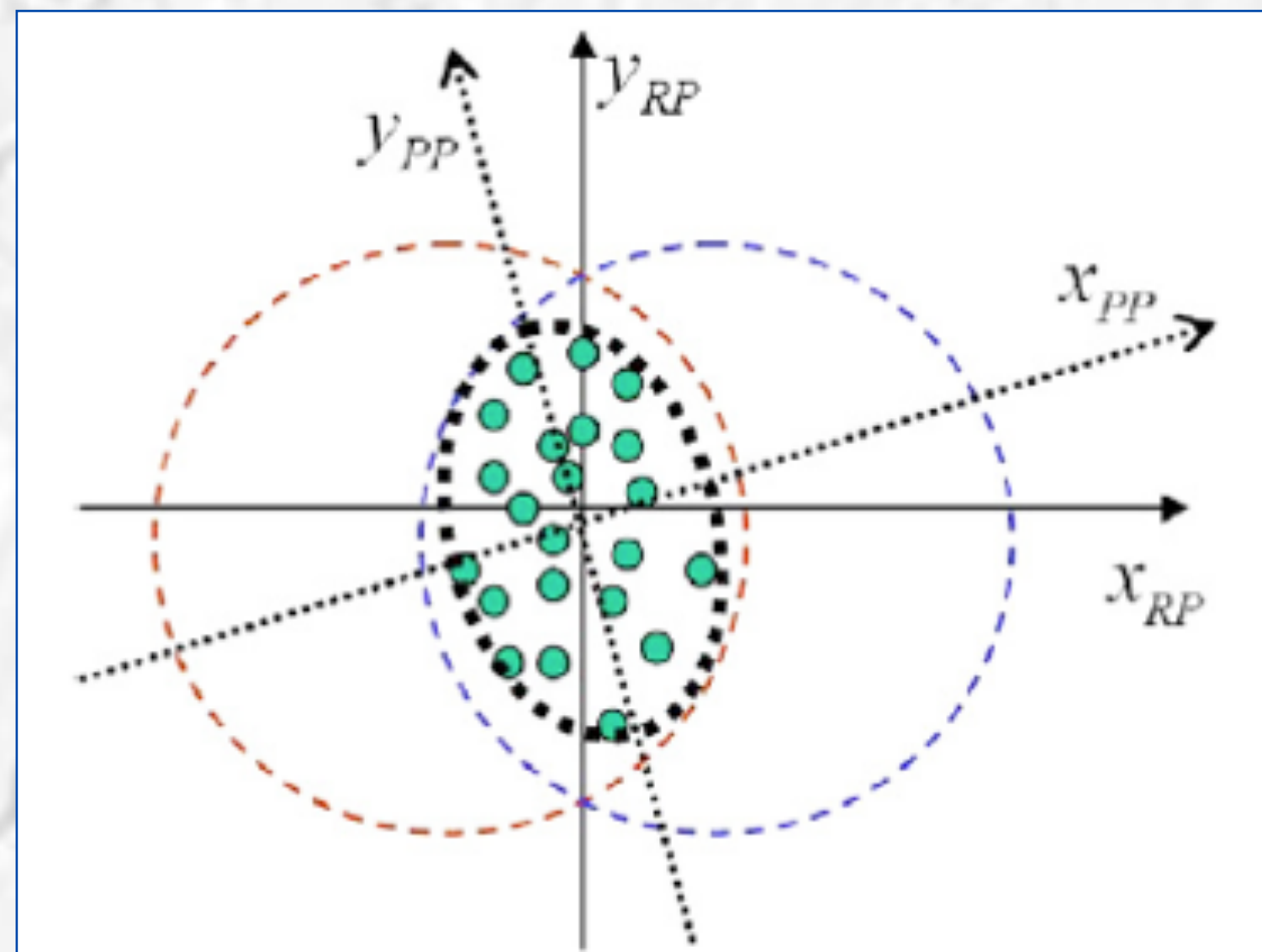
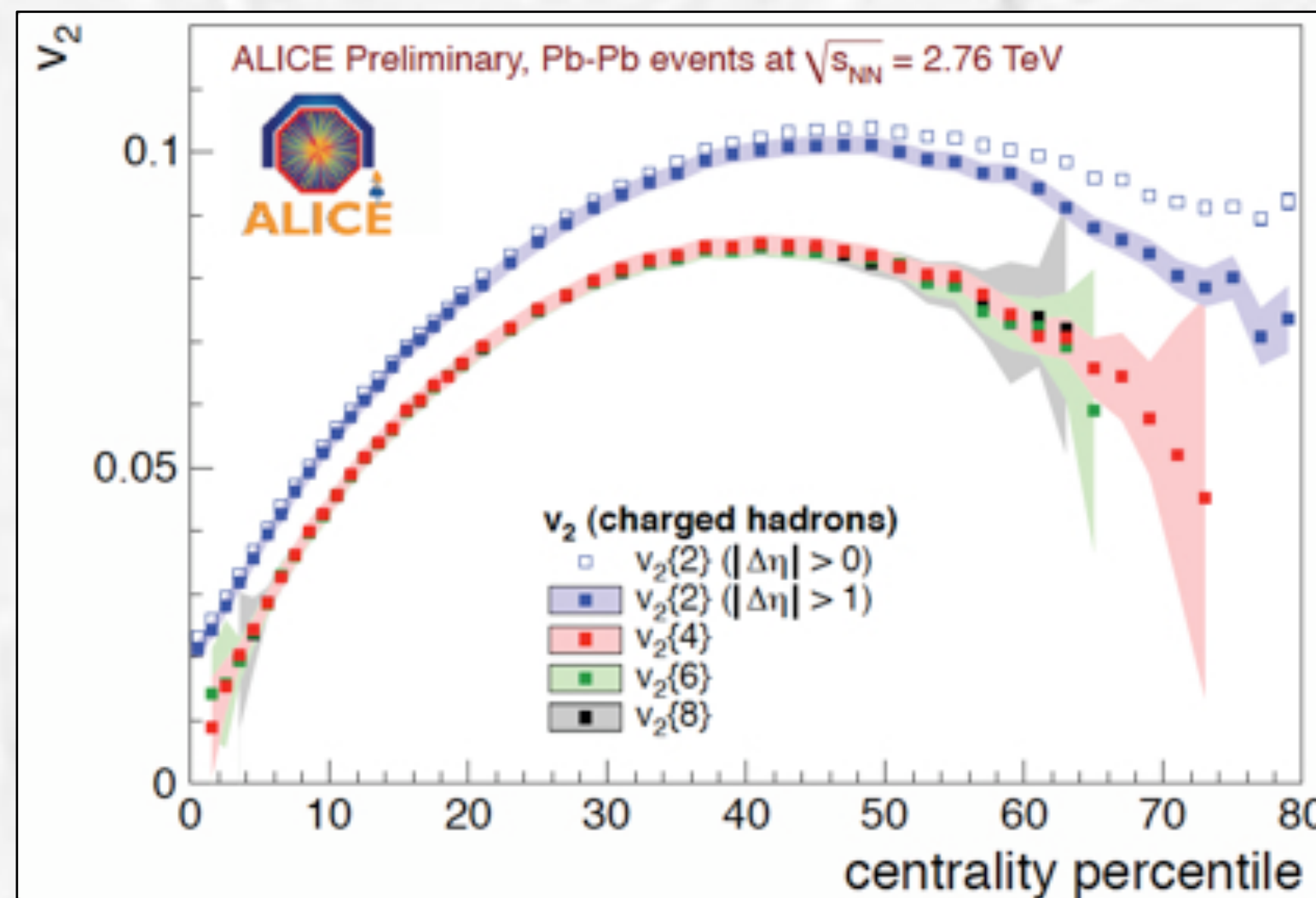
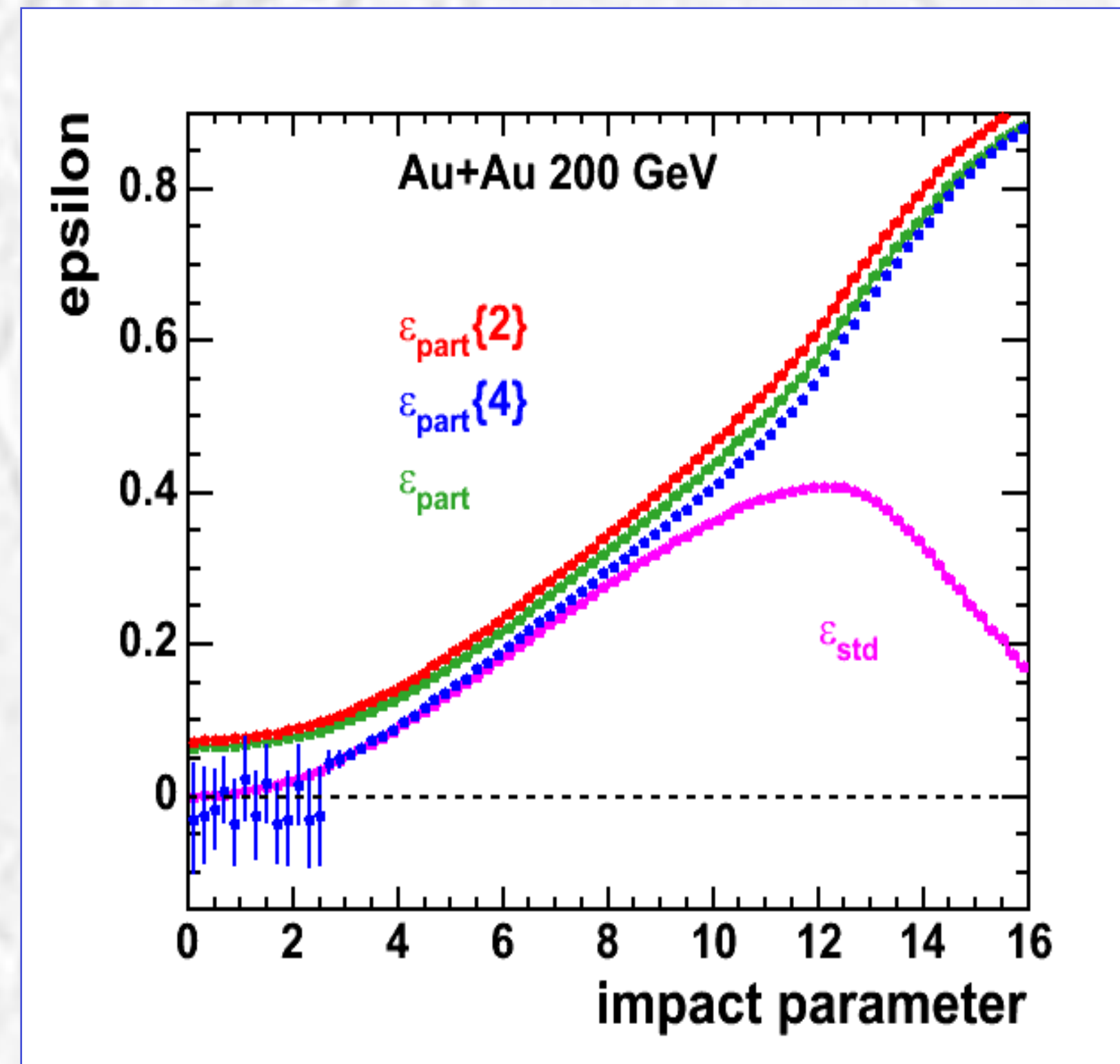


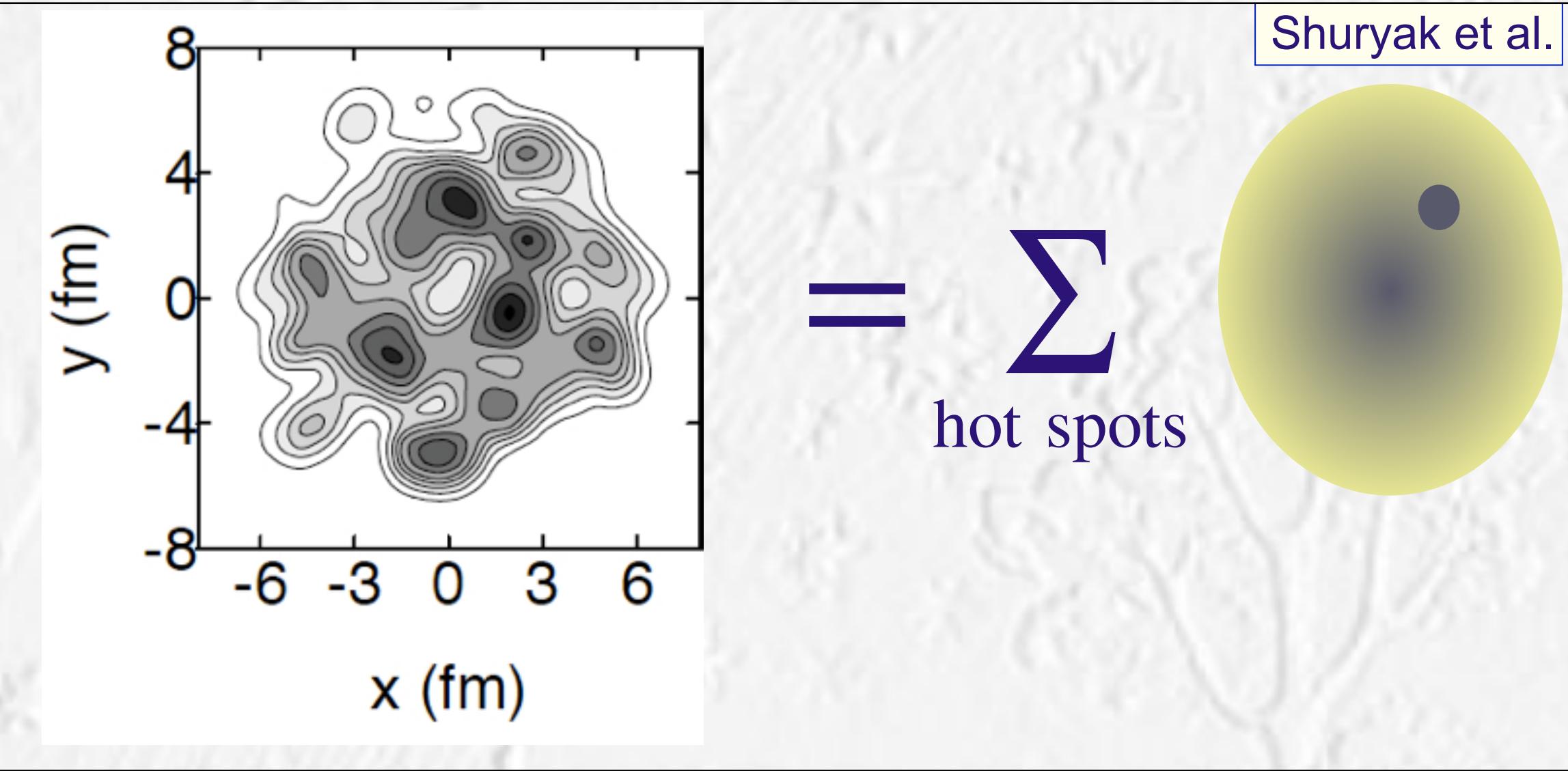
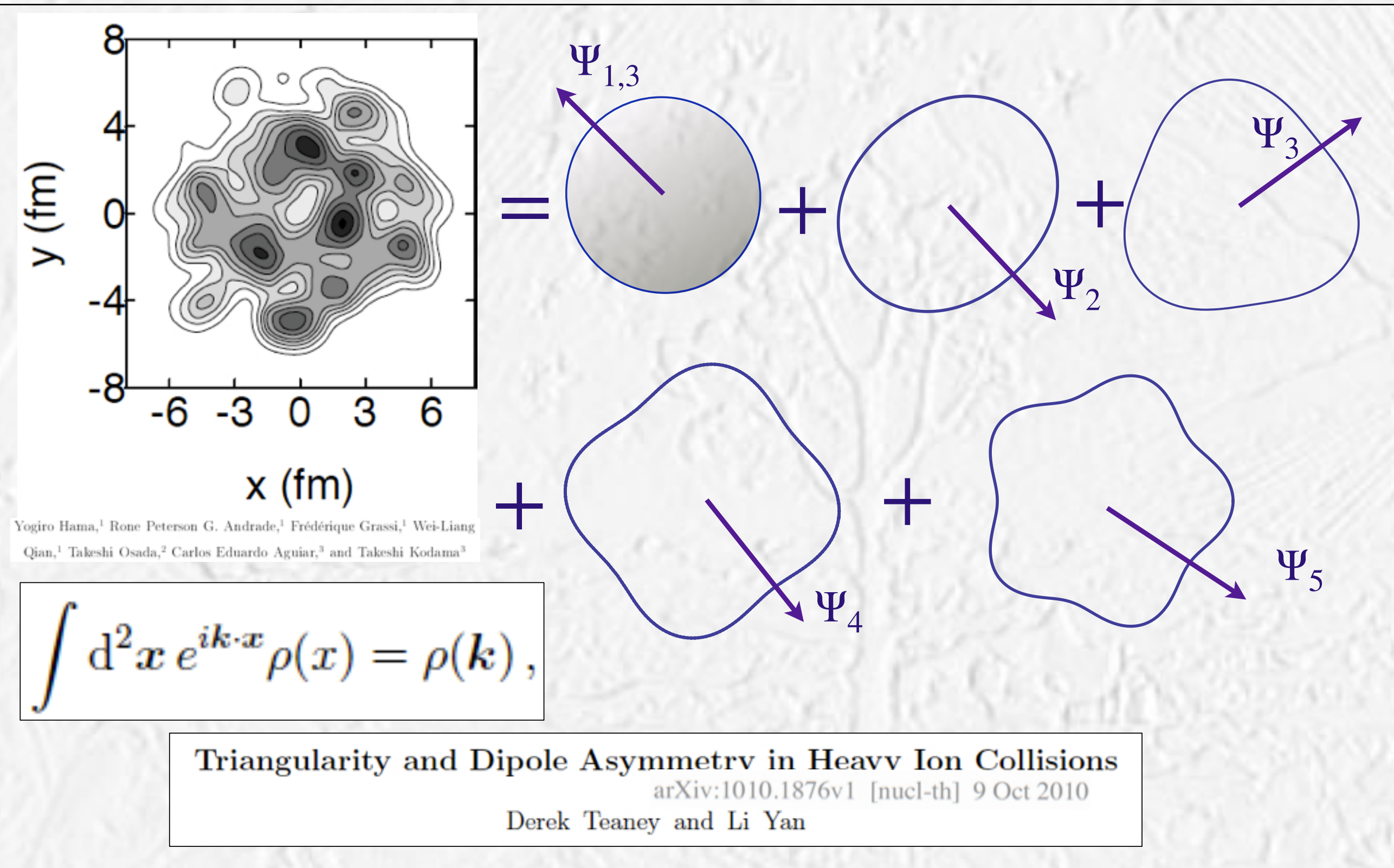
Fig. 1. The definitions of the *RP* and *PP* coordinate systems.

$$\epsilon = \frac{\langle y^2 - x^2 \rangle}{\langle y^2 + x^2 \rangle}$$



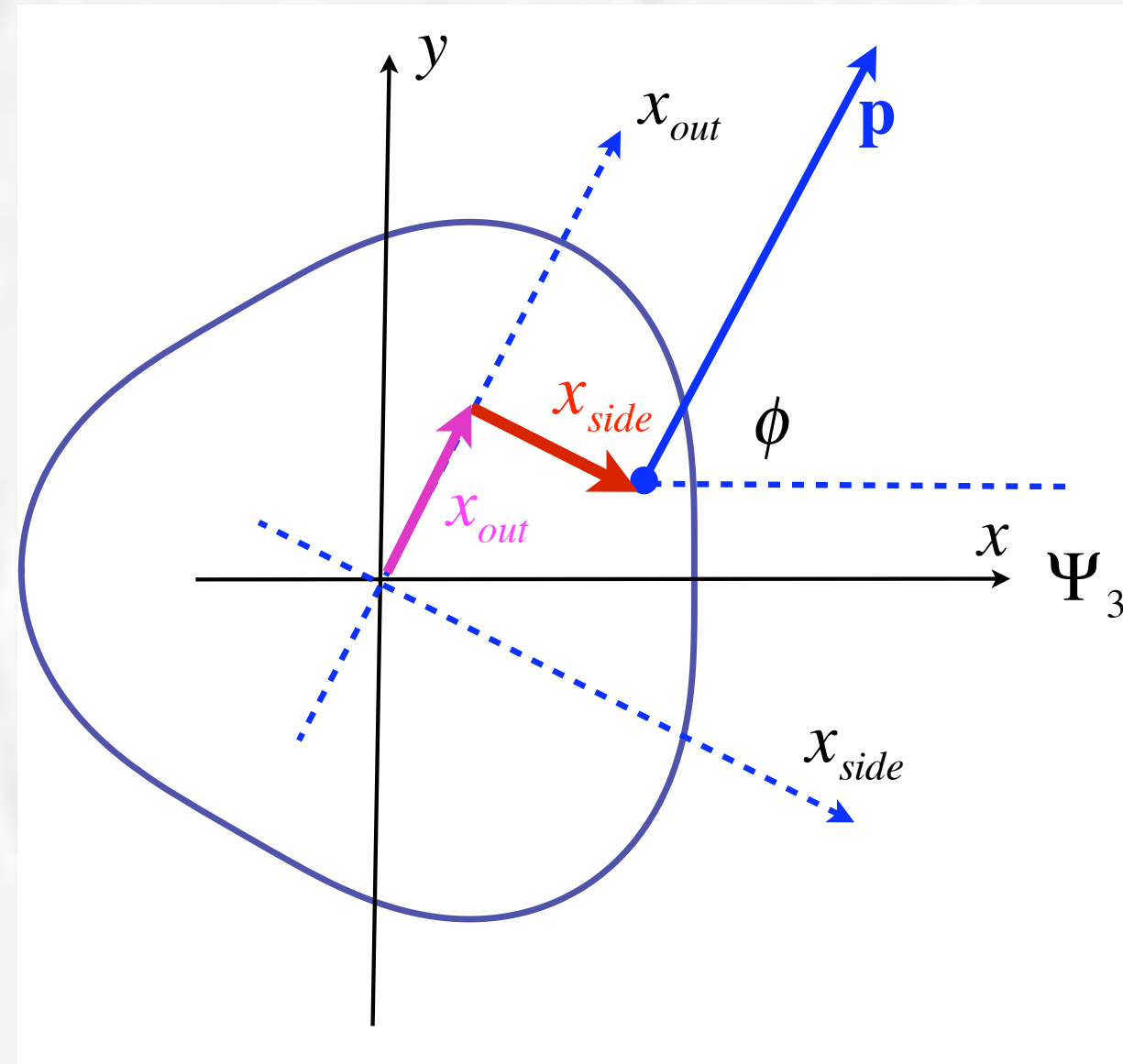
The difference between $v_2\{2\}$ and $v_2\{4\}$ is almost fully saturated by eccentricity fluctuations according to nucleon participant Glauber MC.

Flow fluctuations = nonflow (radial expansion)



$v_n\{\text{RP}\}$ - “hot spots” correlations = nonflow
 $v_n\{\text{PP}\}$ - flow vs “participant planes” - “hot spot” correlations = part of flow fluctuations

Stationary and expanding sources



Rotation of the coordinate system:

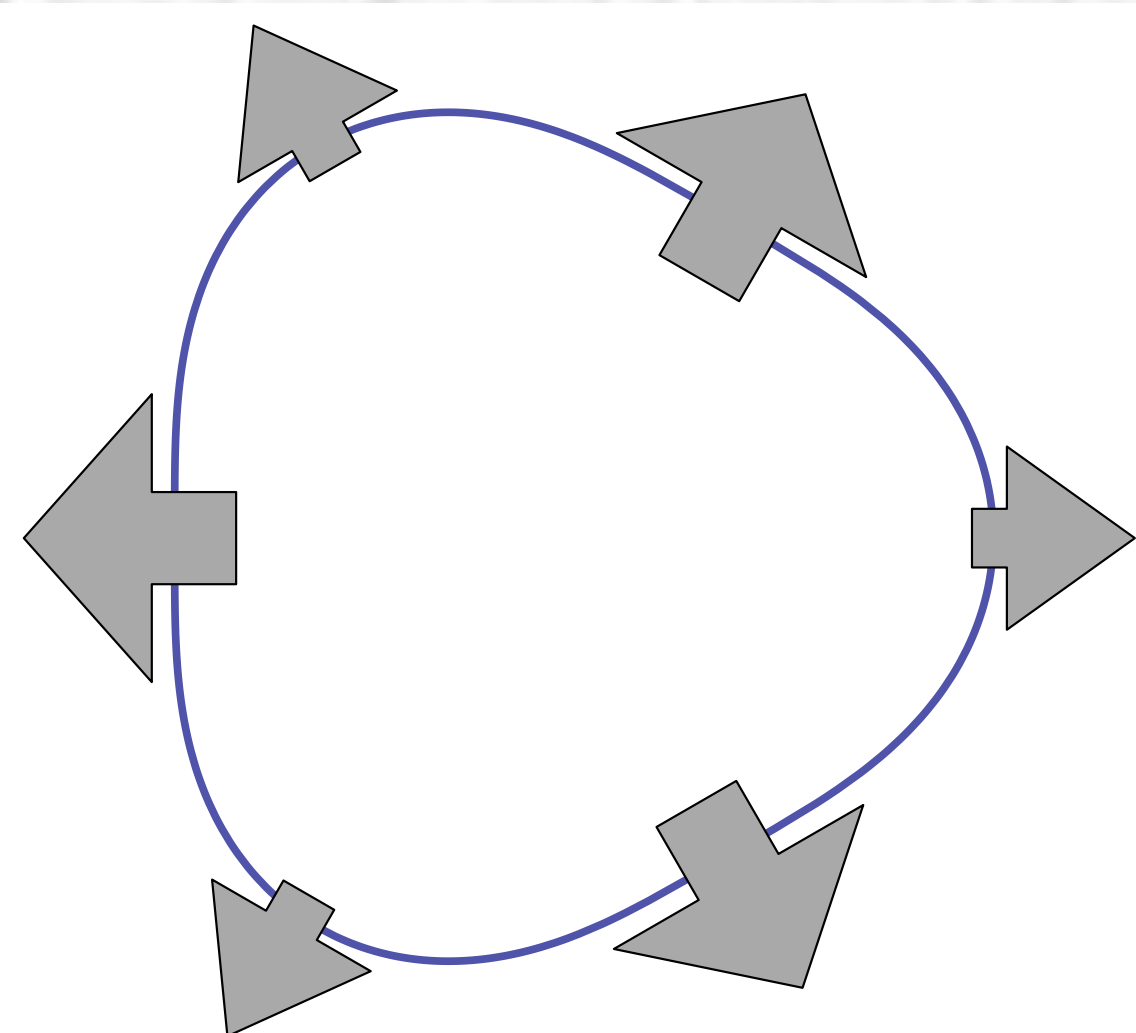
$$\langle x_{side}^2 \rangle = \langle x^2 \rangle \sin^2 \phi + \langle y^2 \rangle \cos^2 \phi - \langle xy \rangle \sin 2\phi$$

Stationary source:

no higher order anisotropy in the Gaussian approximation

4-th harmonic modulations appears only in $\langle x^4 \rangle$

3-rd harmonic modulations appears only in $\langle x^6 \rangle$



$$R_{long} \propto \frac{v_{therm}}{dv_z / dz}$$

Can the collective expansion lead to nontrivial $R(\phi)$ dependence?

Yes, due to several effects:

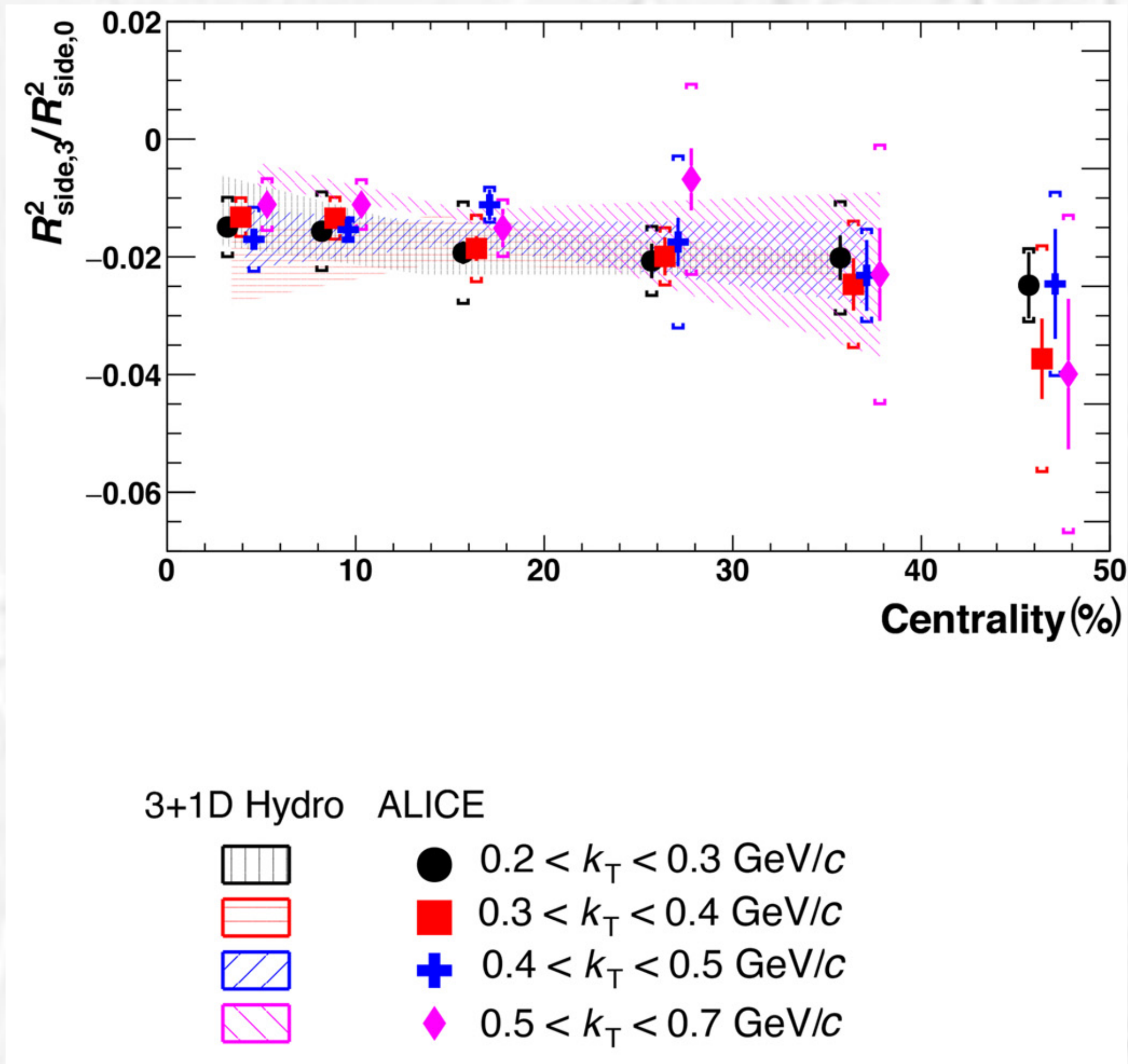
- variation in the “blast wave” velocity

- variation in velocity gradients in “side” direction

Observation of the higher harmonics in azimuthal dependence of femtoscopic radii could originate only in the collective expansion of the source

ALICE, third harmonic HBT

ALICE Collaboration / Physics Letters B 785 (2018) 320–331



to the results from 3+1D hydrodynamical calculations. The observed radii oscillations unambiguously signal a collective expansion and anisotropy in the velocity fields. A comparison of the measured radii oscillations with the Blast-Wave model calculations indicate that the initial state triangularity is washed-out at freeze out.

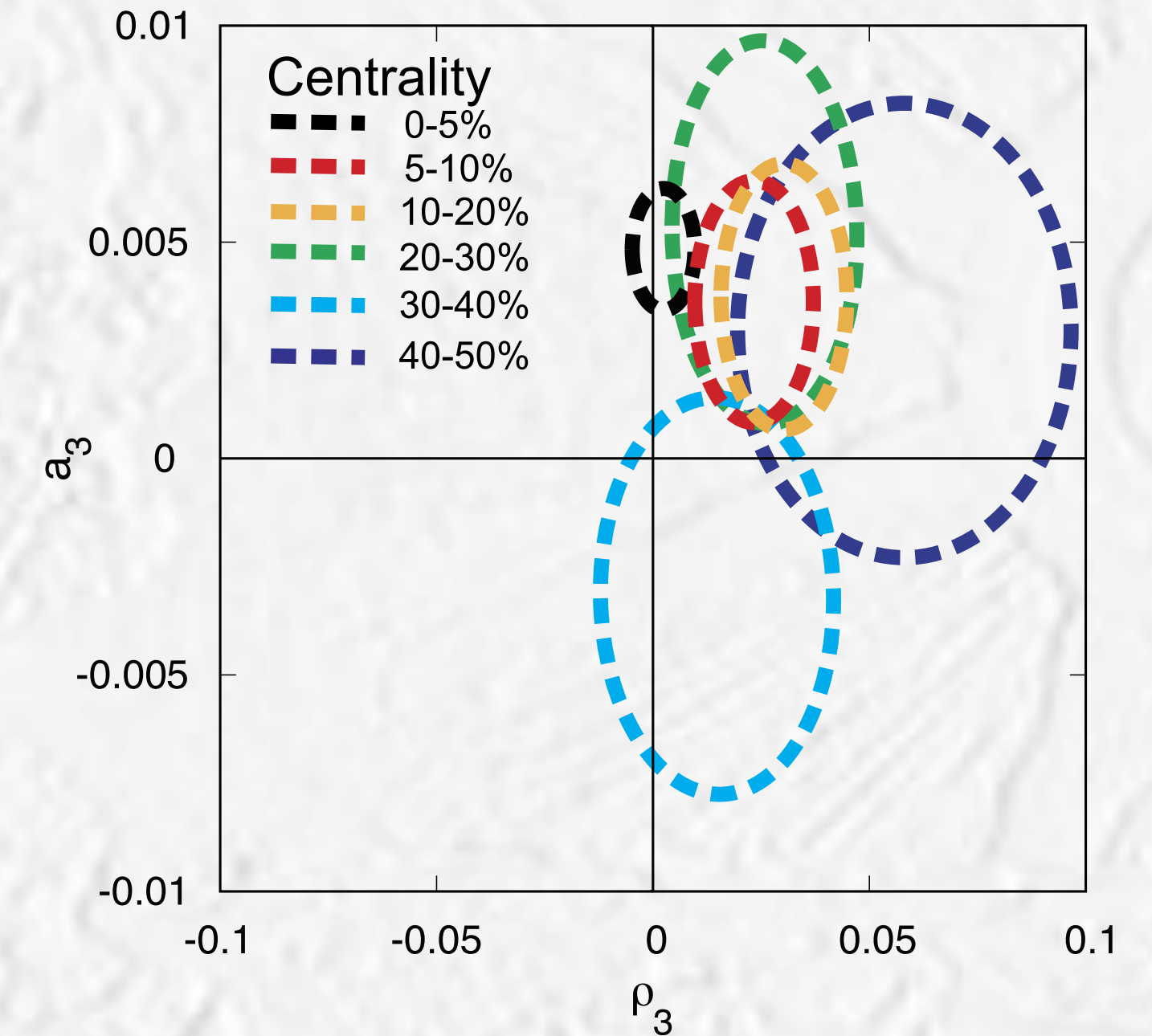
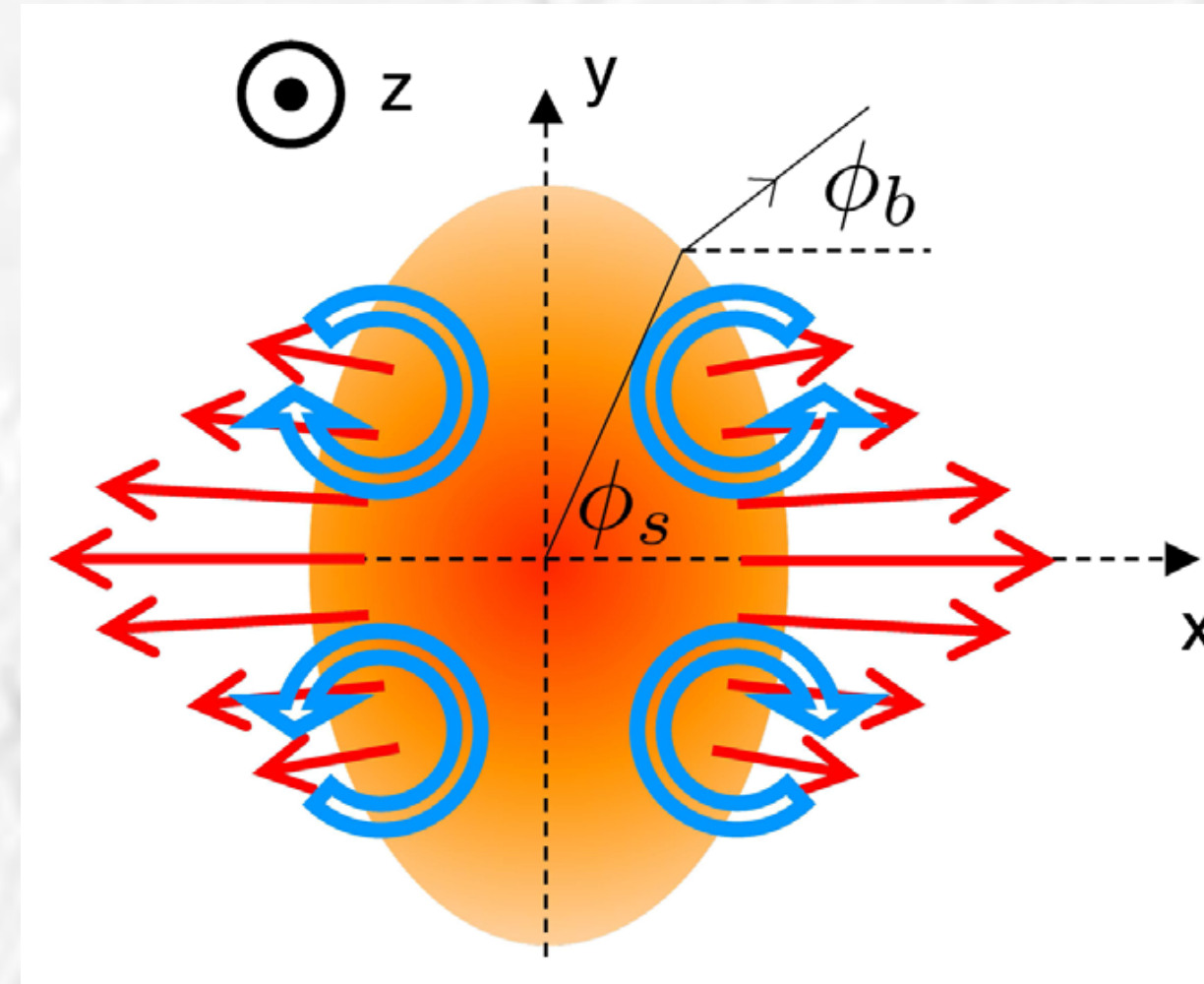
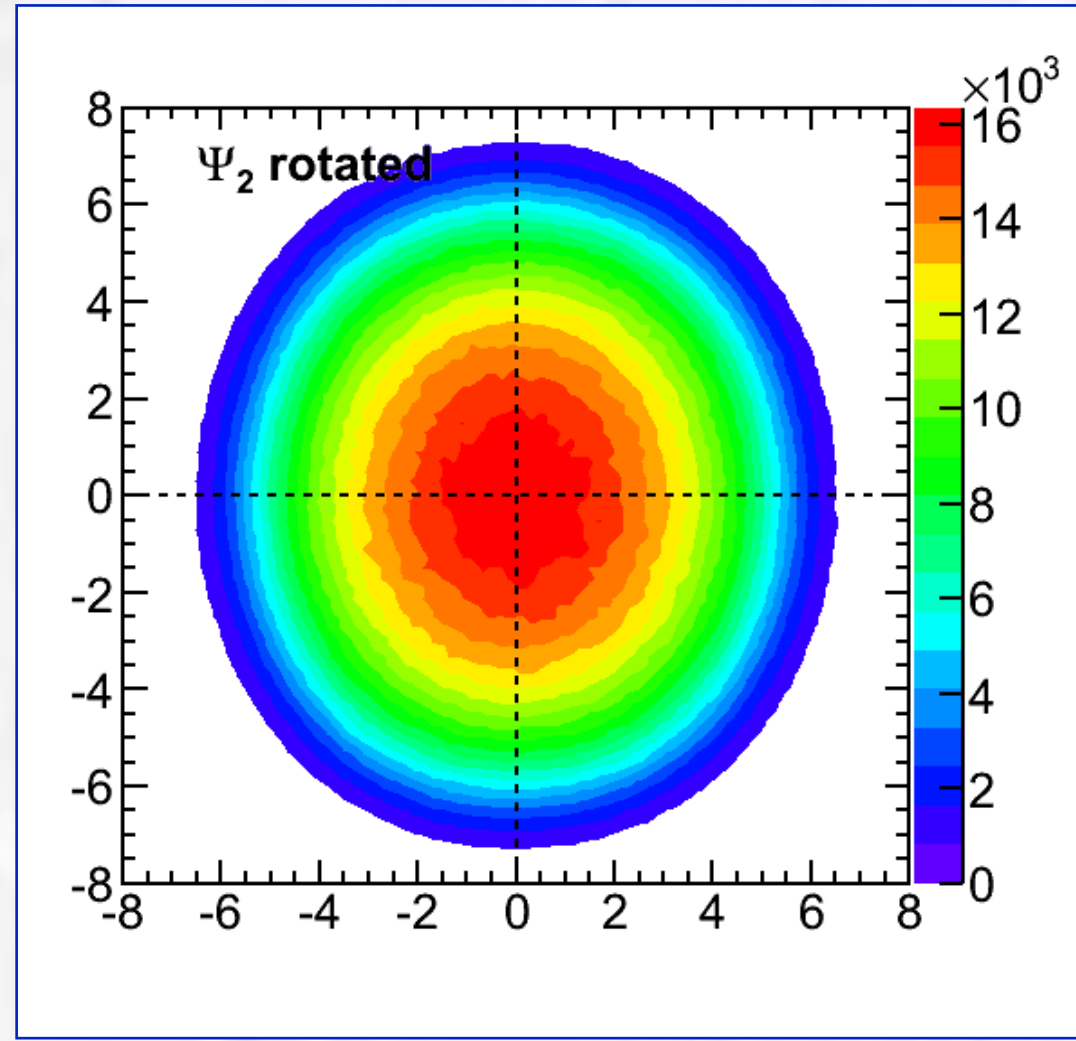


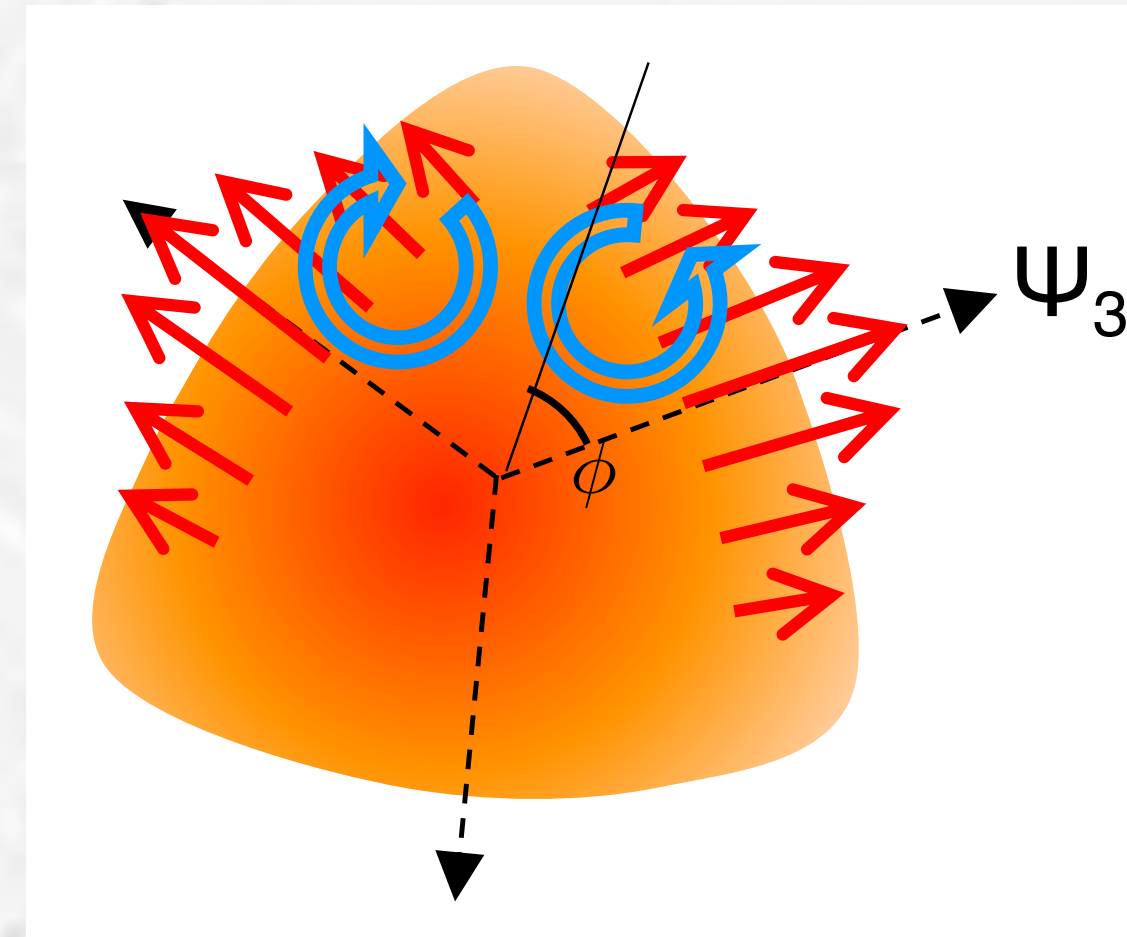
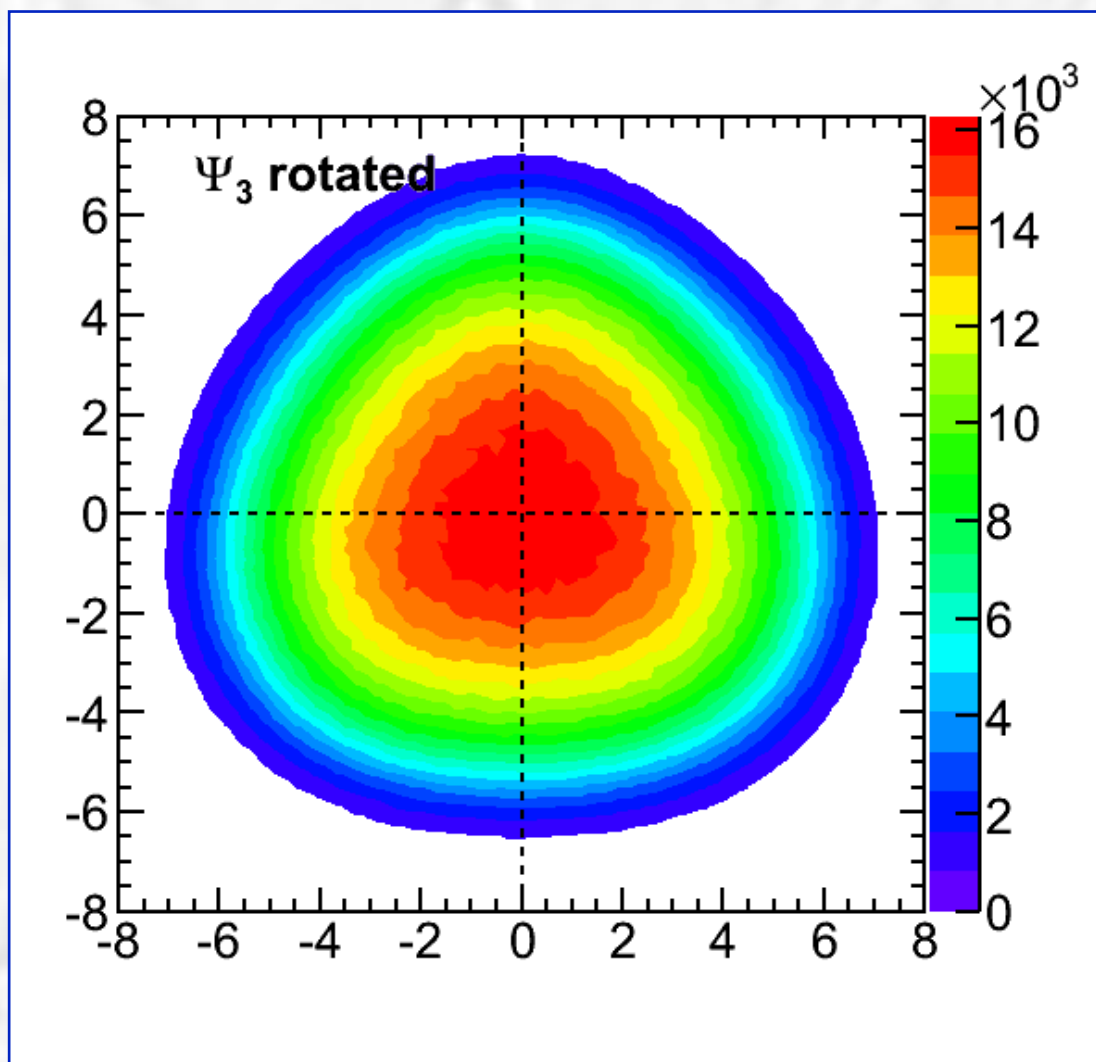
Fig. 5. Blast-Wave model [16] source parameters, final spatial (a_3) and transverse flow (ρ_3) anisotropies, for different centrality ranges, as obtained from the fit to ALICE radii oscillation parameters. The contours represent the one sigma uncertainty.

This results unambiguously indicate collective expansion of the source as no any other “evidence”,

Anisotropic flow and vorticity



$$\omega = \frac{1}{2} \nabla \times \mathbf{v}$$



Anisotropic flow and vorticity

Barnett effect

Second Series.

October, 1915

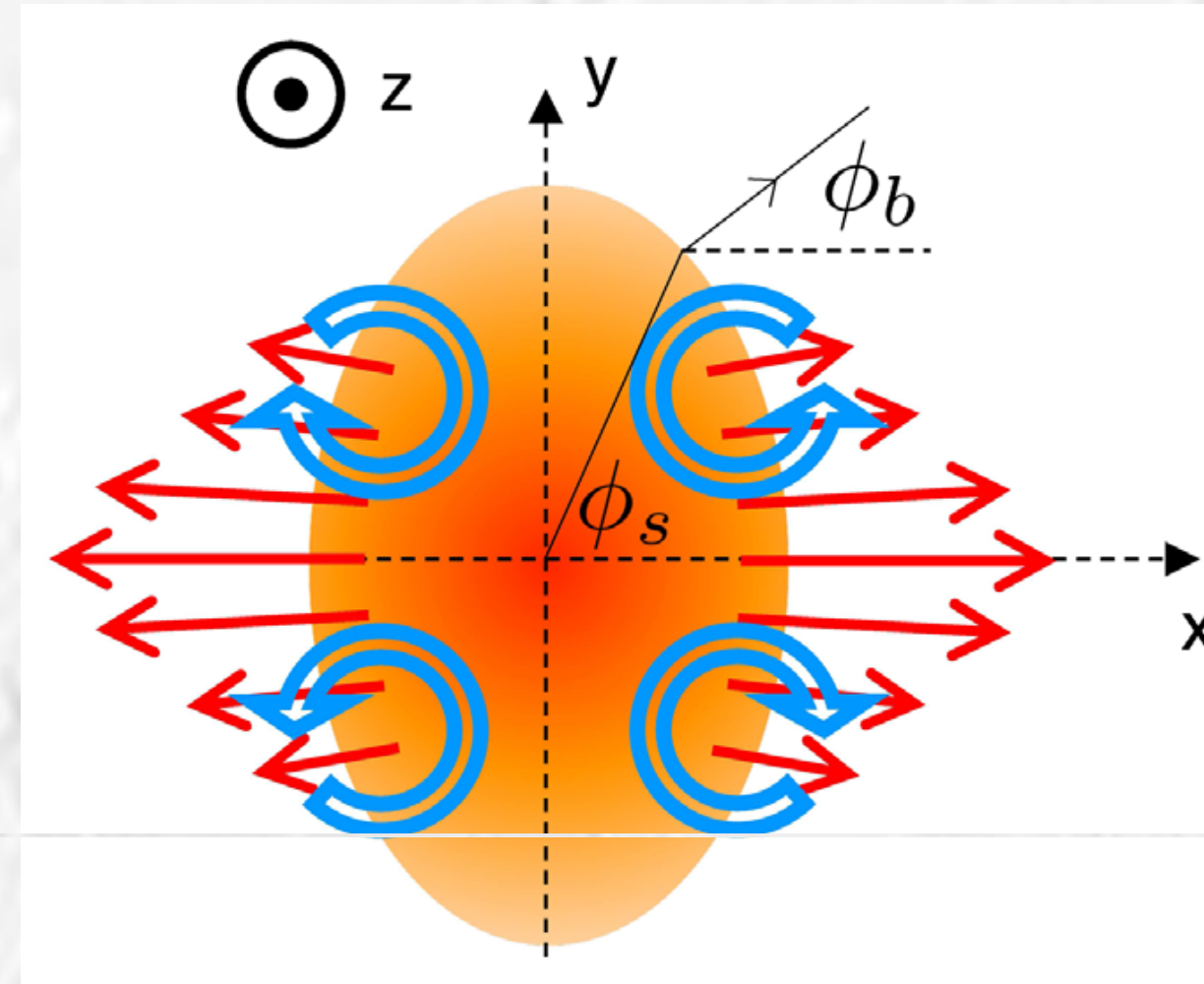
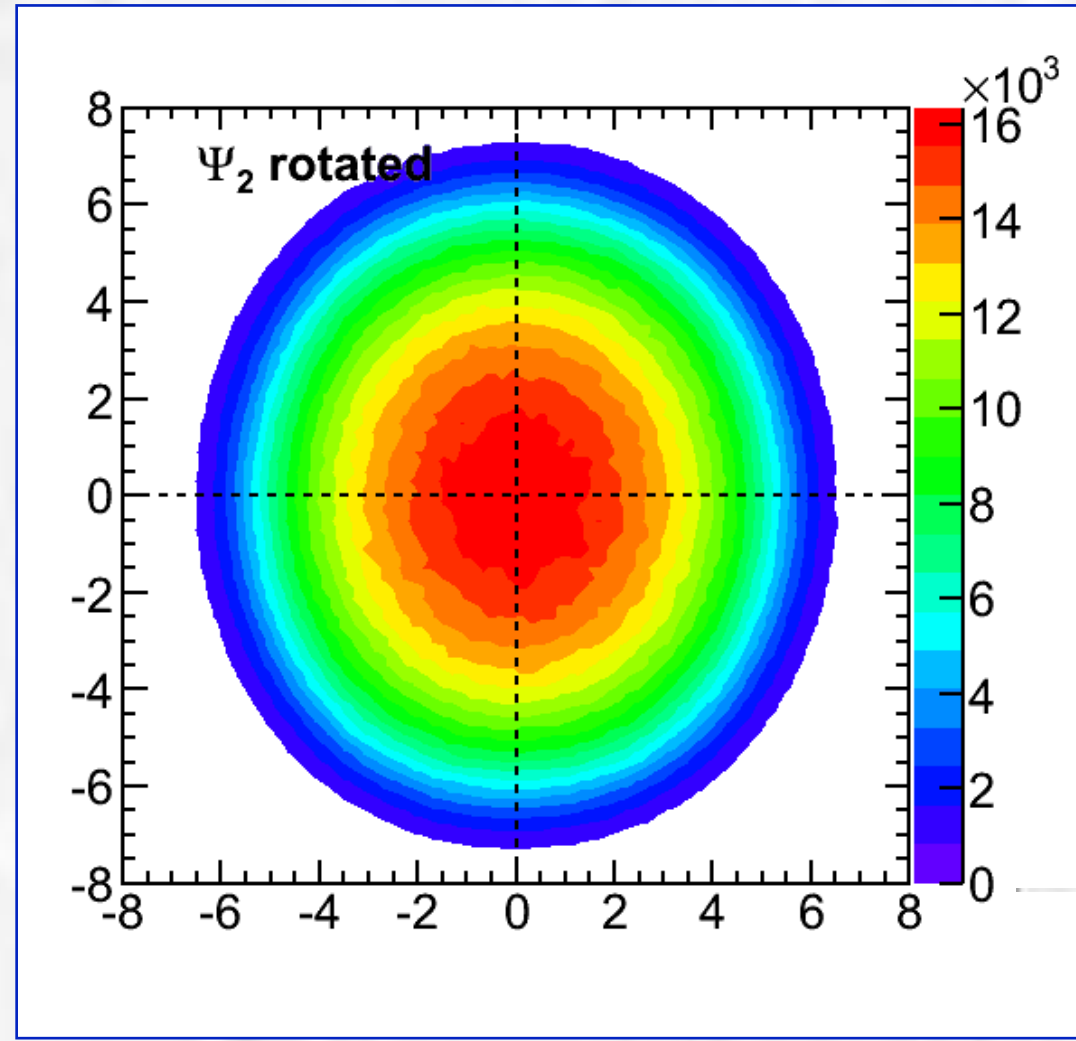
Vol. VI., No. 4

THE PHYSICAL REVIEW.

MAGNETIZATION BY ROTATION.¹

By S. J. BARNETT.

§1. In 1909 it occurred to me, while thinking about the origin of terrestrial magnetism, that a substance which is magnetic (and therefore, according to the ideas of Langevin and others, constituted of atomic or molecular orbital systems with individual magnetic moments fixed in magnitude and differing in this from zero) must become magnetized by a sort of molecular gyroscopic action on receiving an angular velocity.



$$\omega = \frac{1}{2} \nabla \times \mathbf{v}$$

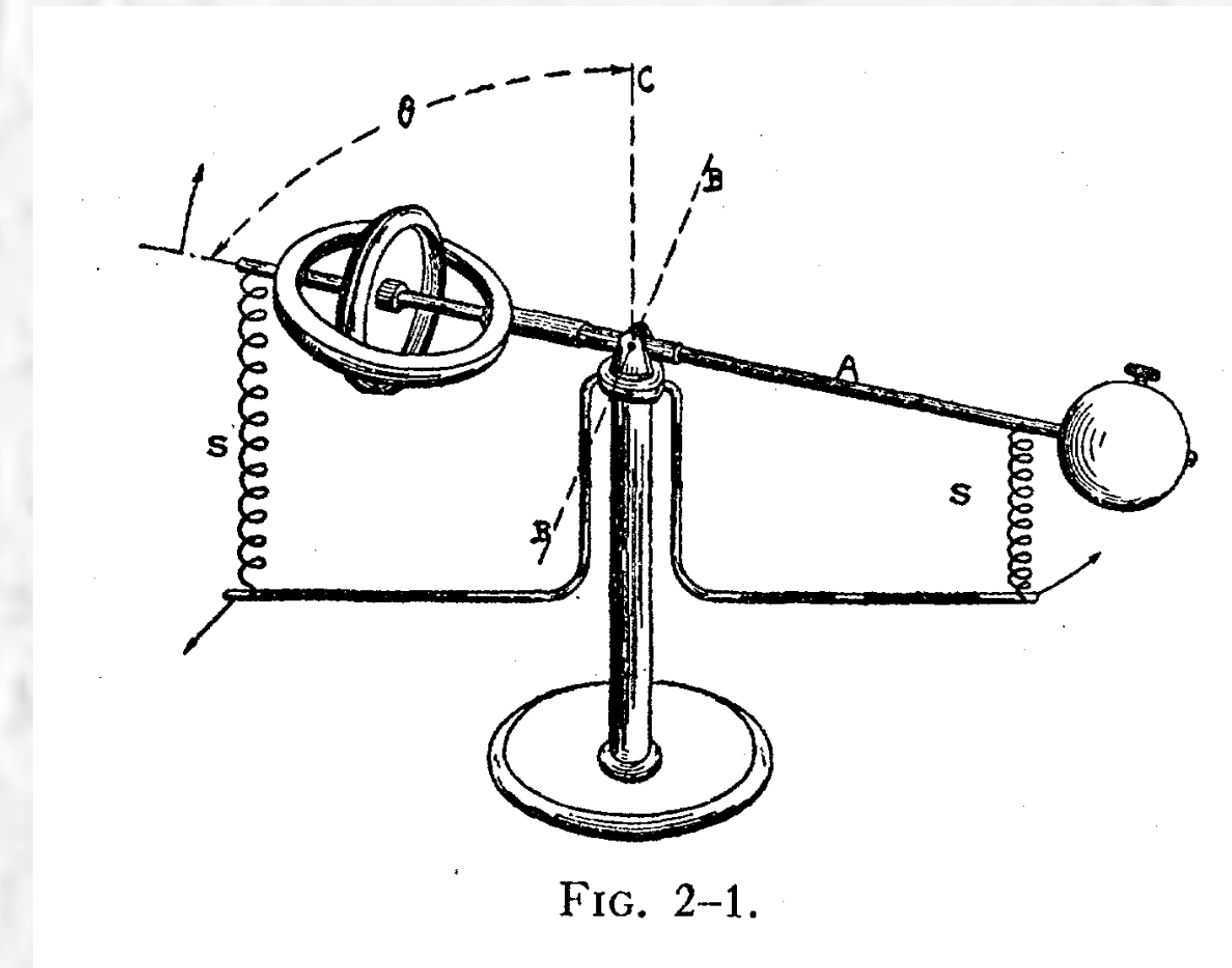
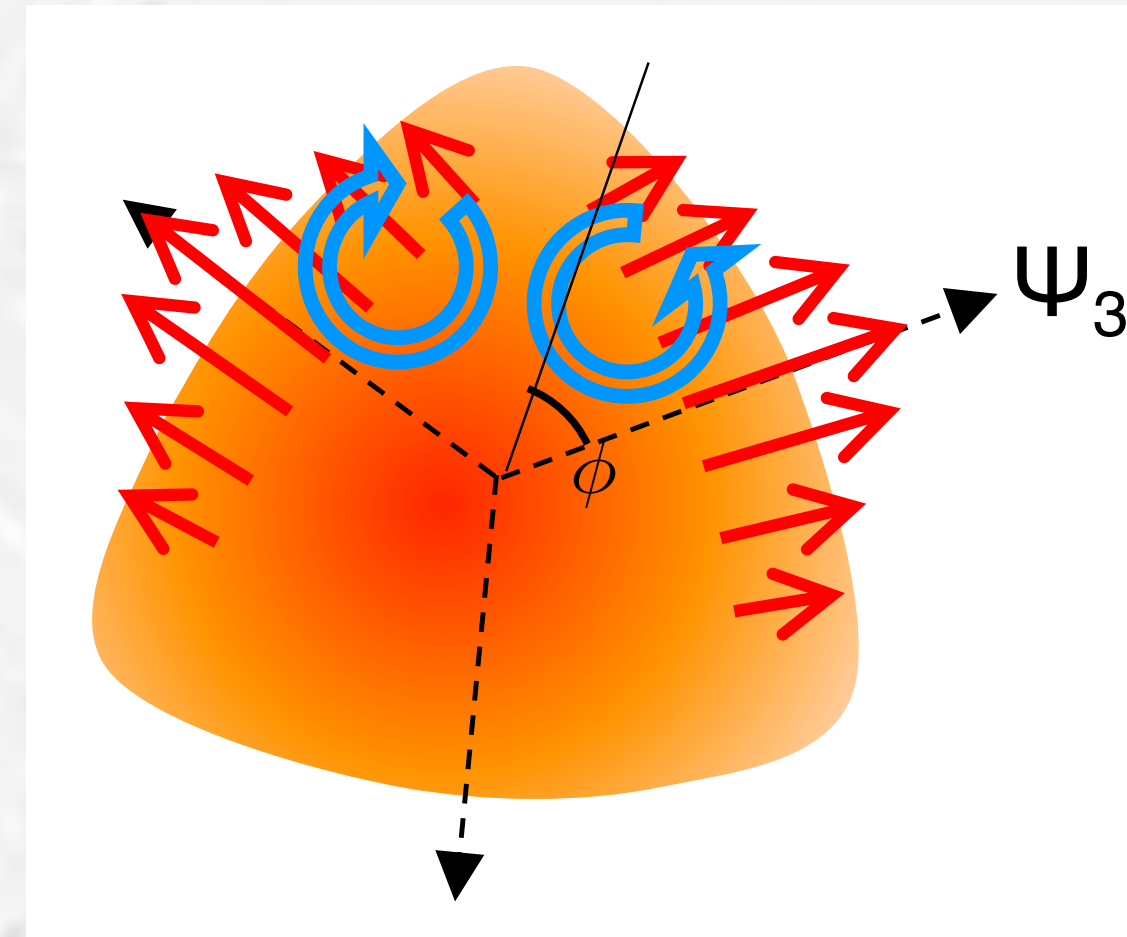
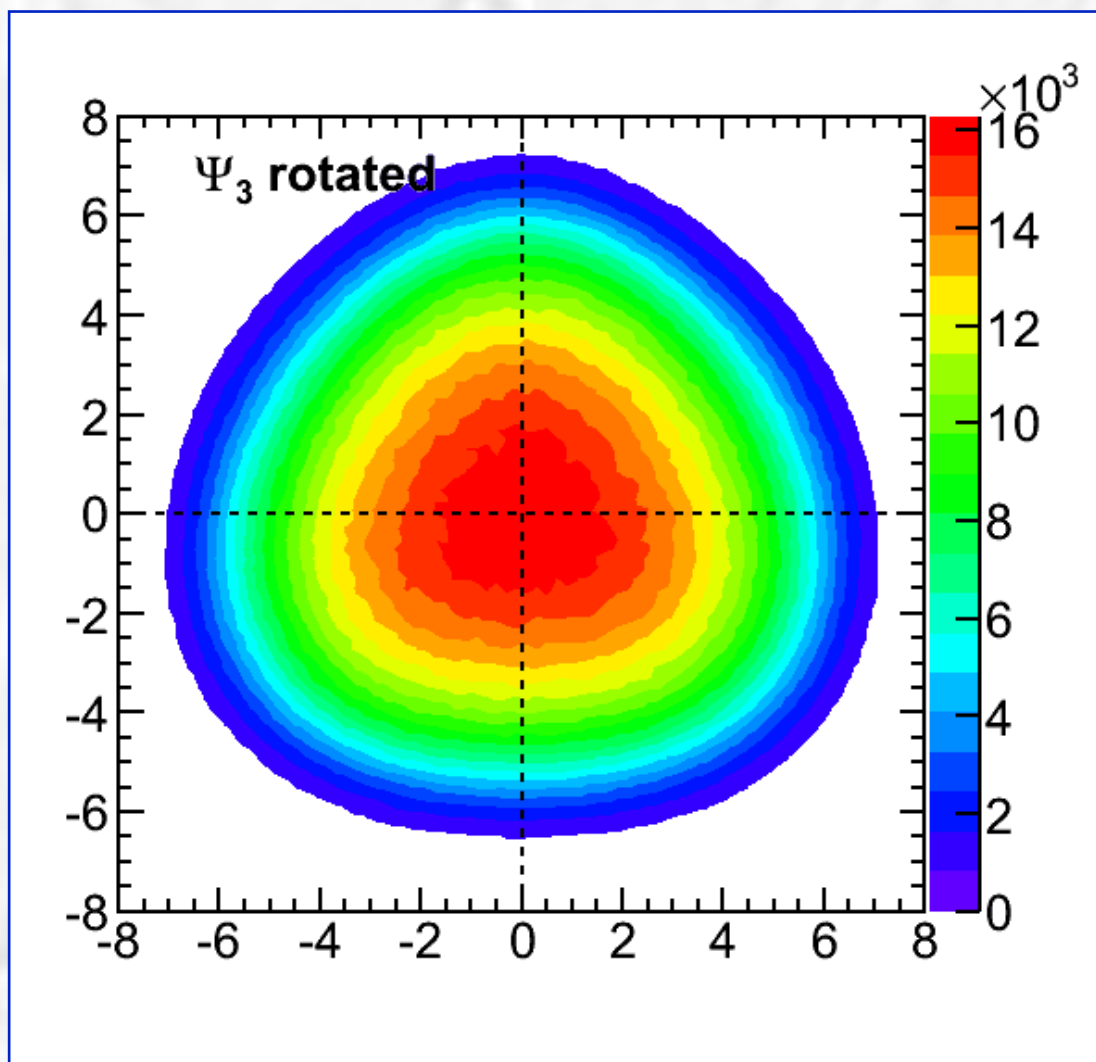
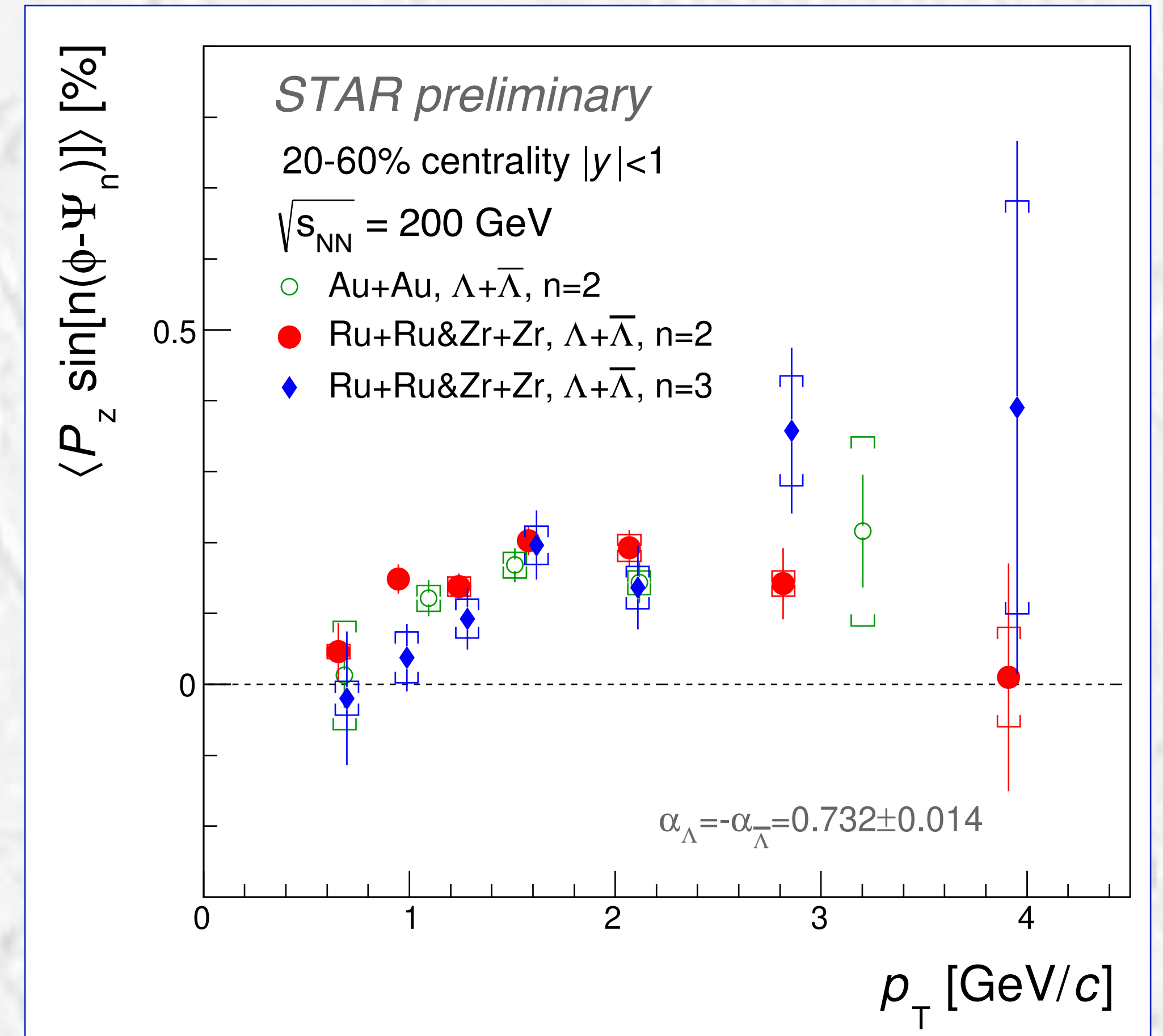
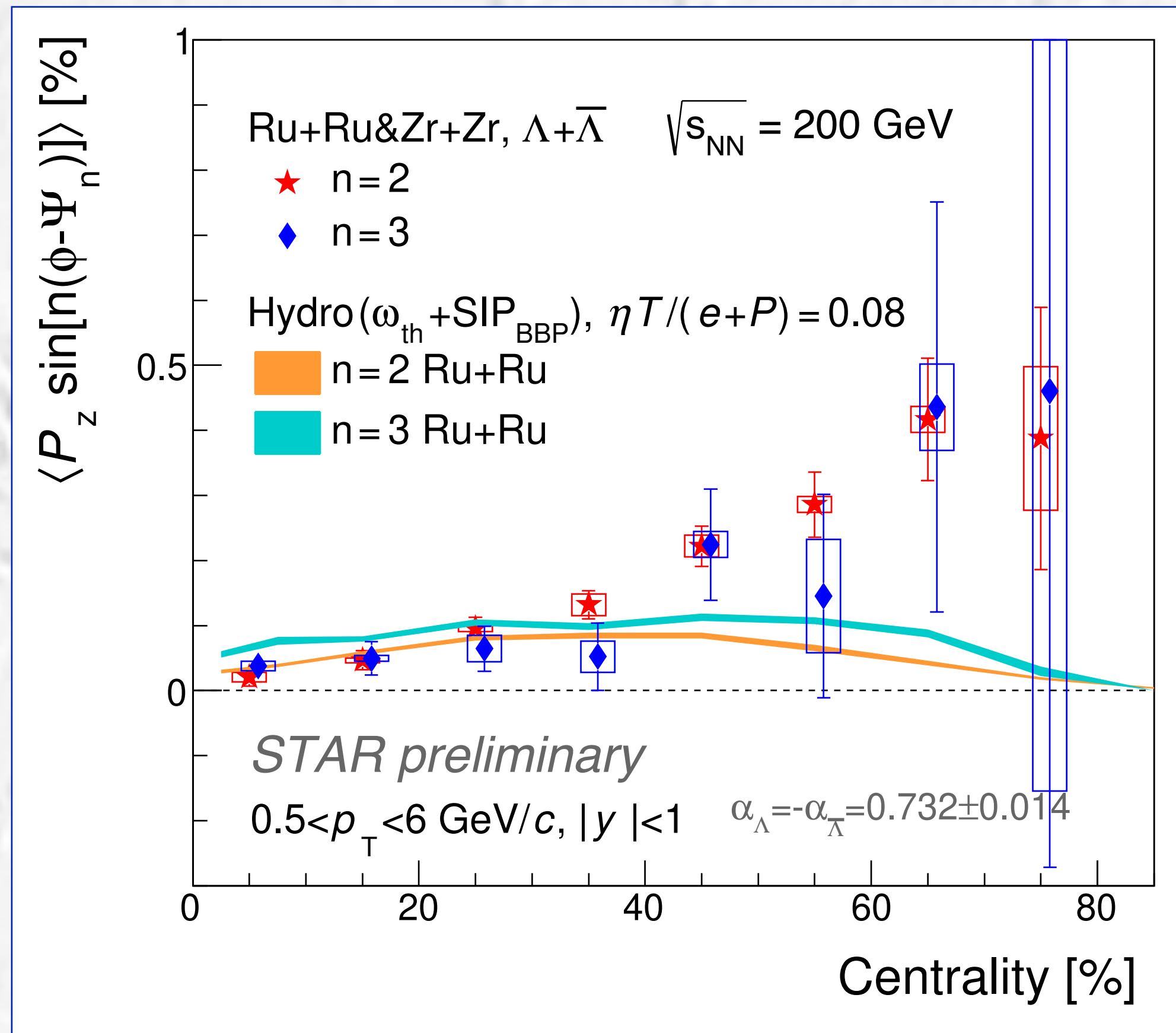
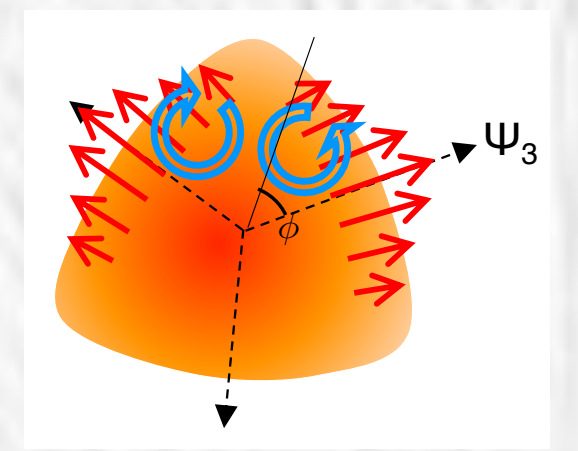
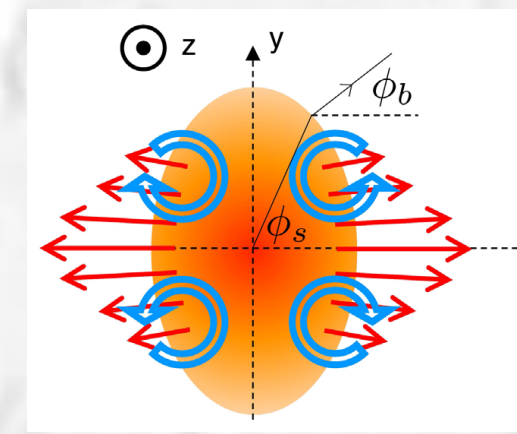


FIG. 2-1.

$$P \approx \omega / (2T)$$

$$\langle P_z \sin[n(\phi_H - \Psi_n)] \rangle$$



Using average over Ru+Ru and Zr+Zr
 Assuming the same polarization for Λ and $\bar{\Lambda}$

Summary

Art: physics, inspiration, and much more



Flow, as a truly ideal fluid, has interpenetrated all parts of heavy ion physics, it brings new discoveries and contributes greatly to our understanding of strongly interacting matter.

We are grateful to Art, who made it works.

EXTRA SLIDES

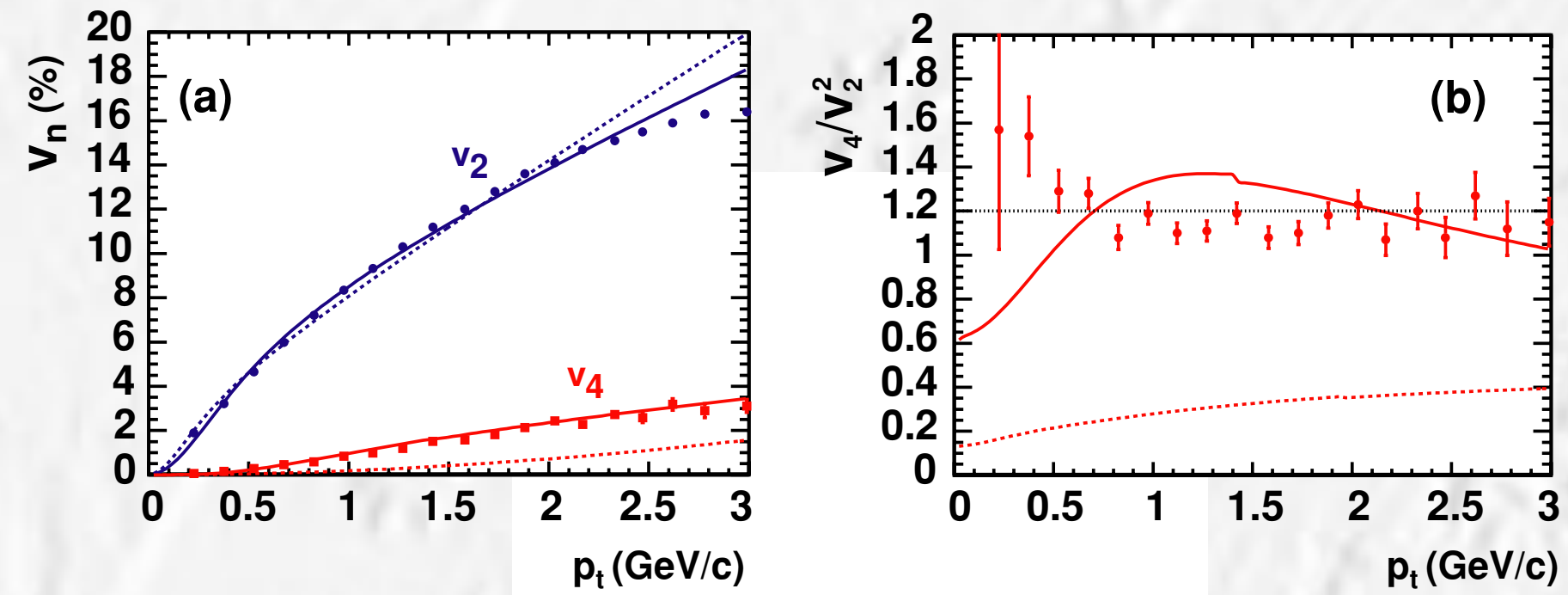


FIG. 22. (Color online) Graphs of v_n and v_4/v_2^2 . The dashed lines are surface shell blast-wave fits with no ρ_4 or s_4 terms (see Sec. VID) to the charged hadron v_2 minimum bias data. The resultant ratio v_4/v_2^2 is shown as the lower dashed line in the ratio graph (b). The solid lines are the fits with the addition of ρ_4 and s_4 . The resultant ratio v_4/v_2^2 is shown as the solid curve in the ratio graph (b). The dotted line in the ratio graph (b) at 1.2 represents the average value of the data.

$$N \cdot (v_n\{2\}^2 - v_n\{k\}^2) = g_n$$

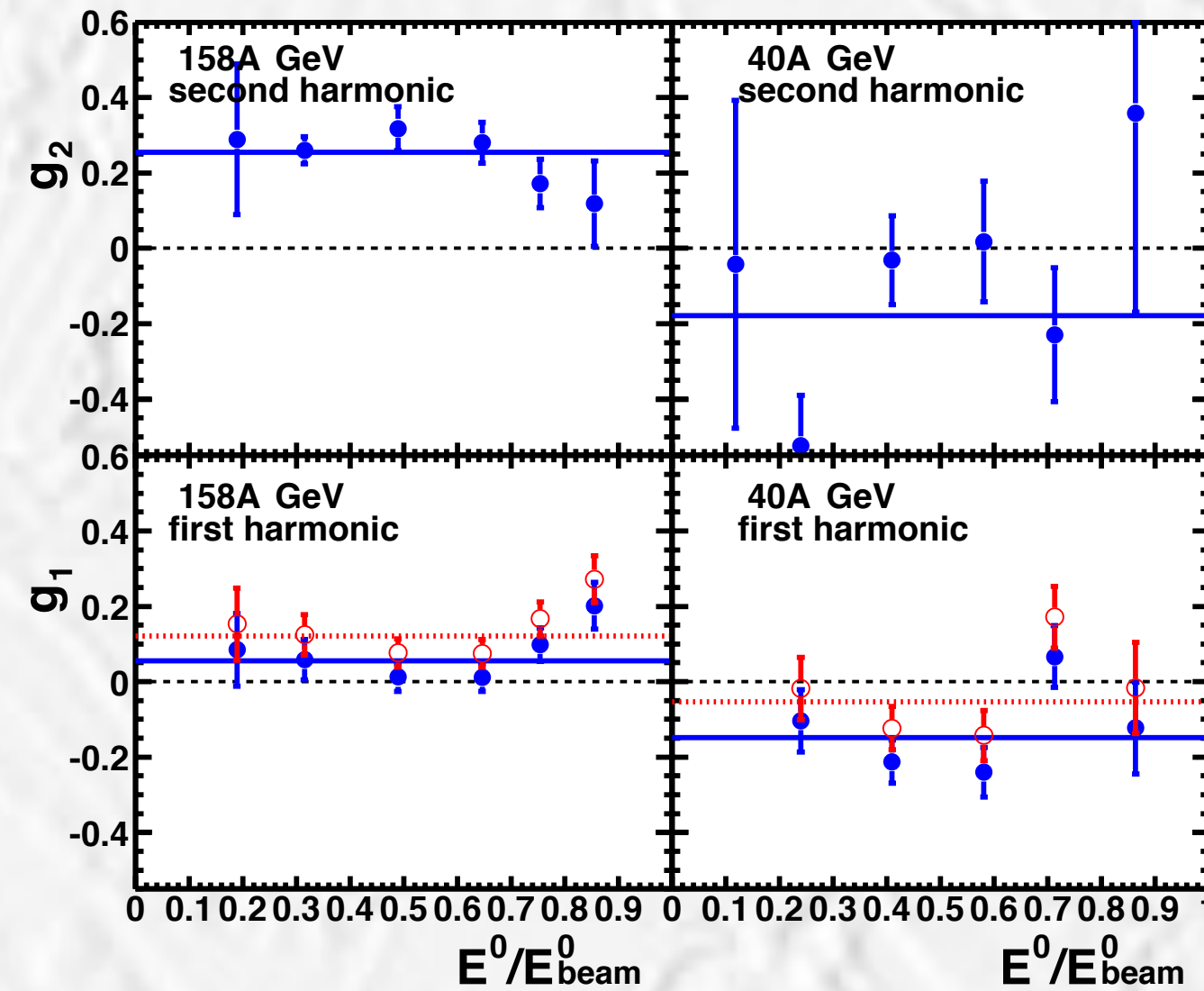


FIG. 22. (Color online) Nonflow azimuthal correlations from Eq. (16), for the first, g_1 , (bottom) and second, g_2 , (top) Fourier harmonics, from 158A GeV (left) and 40A GeV (right) Pb+Pb collisions. For g_1 , the solid points represent all nonflow effects, while the open points are corrected for momentum conservation. The horizontal lines are at the mean values.

Q-vector products and multiparticle correlations

$$u = e^{if}; \quad Q = \sum u; \quad Q_2 = \sum u^2$$

$$\langle u_i u_j^* \rangle = \left\langle \frac{1}{N(N-1)} (QQ^* - N) \right\rangle$$

$$\langle u_i u_j u_k^{*2} \rangle = \left\langle \frac{1}{N(N-1)(N-2)} [(Q^2 Q_2^* - N) - (Q_2 Q_2^* - N) - 2(QQ^* - N)] \right\rangle$$

$$\langle u_i u_j u_k^* u_l^* \rangle = \left\langle \frac{1}{N(N-1)(N-2)(N-3)} [(Q^2 Q^{*2} - N) - 2N(N-1) - 4(N-2)(QQ^* - N) - 2(Q^2 Q_2^* - N) + (Q_2 Q_2^* - N)] \right\rangle$$

the beginning

C. ALT *et al.*

PHYSICAL REVIEW C **68**, 034903 (2003)

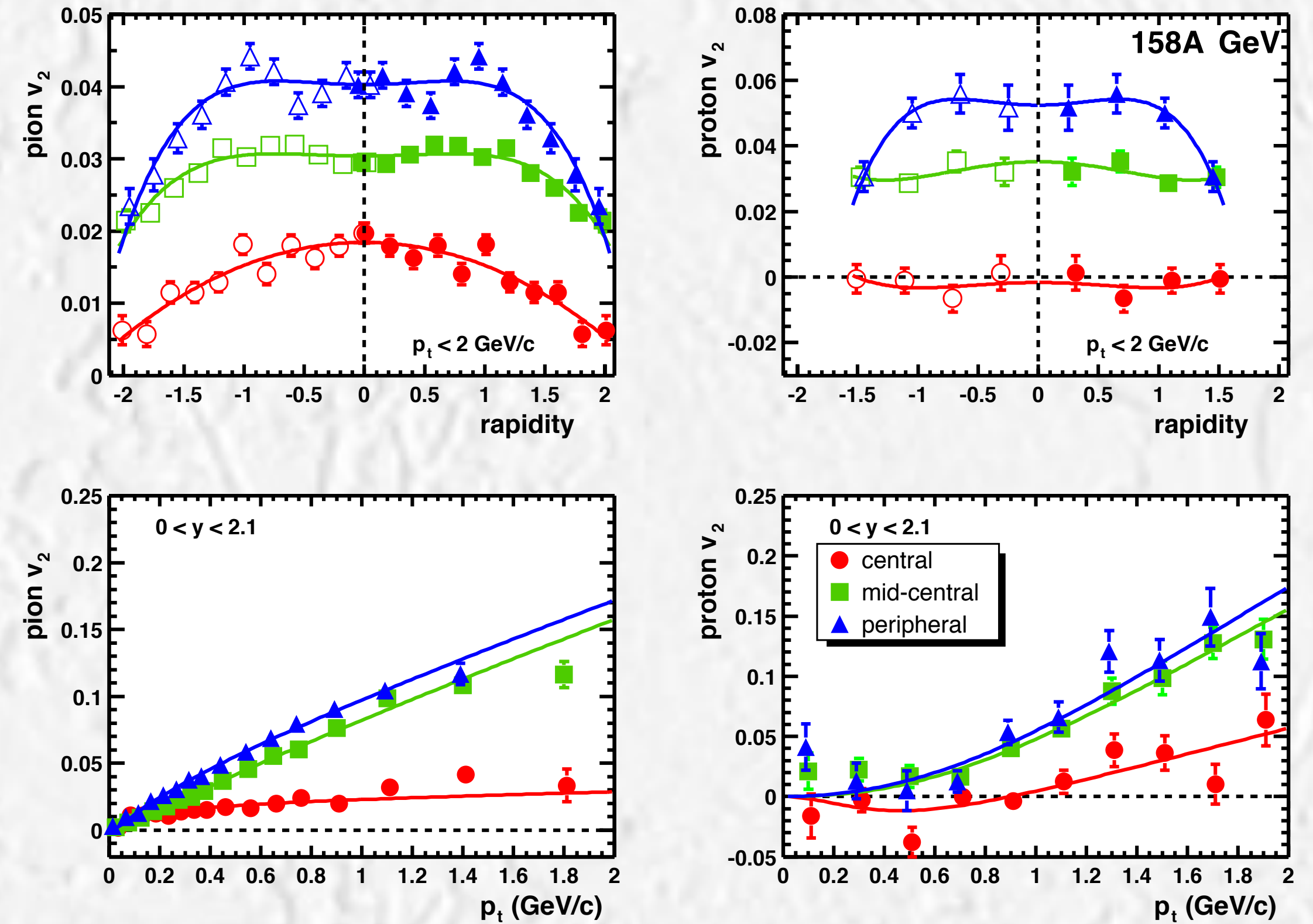


FIG. 6. (Color online) Elliptic flow obtained from the standard method as a function of rapidity (top) and transverse momentum (bottom) for charged pions (left) and protons (right) from 158A GeV Pb+Pb. Three centrality bins are shown. The open points in the top graphs have been reflected about midrapidity. Solid lines are polynomial fits (top) and blast wave model fits (bottom).