

Semileptonic B_s decays

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(RBC-UKQCD collaborations)



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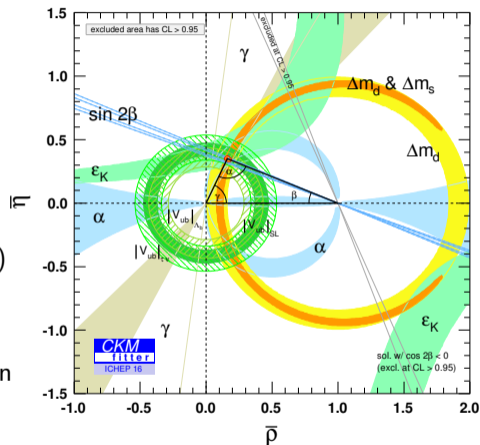
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Nicolas Garron

introduction

Why B_s meson decays?

- ▶ Alternative, tree-level determination of $|V_{cb}|$ and $|V_{ub}|$ from $B_s \rightarrow D_s l \nu$ and $B_s \rightarrow K l \nu$
 - Commonly used $B \rightarrow \pi l \nu$ and $B \rightarrow D^{(*)} l \nu$
 - Long standing $2 - 3\sigma$ discrepancy between exclusive ($B \rightarrow \pi l \nu$) and inclusive ($B \rightarrow X_u l \nu$)
 - $B \rightarrow \tau \nu$ has larger error
 - Alternative, exclusive ($\Lambda_b \rightarrow p l \nu$) determination [Detmold, Lehner, Meinel, PRD92 (2015) 034503]



[<http://ckmfitter.in2p3.fr>]

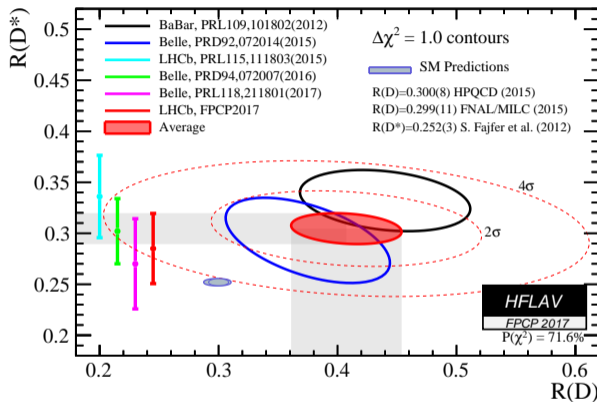
Why B_s meson decays?

- ▶ Alternative tests of lepton flavor violations
 - Determine e.g. $R_{D_s^{(*)}}$ from B_s decays to compare with $R_{D^{(*)}}$ from B decays

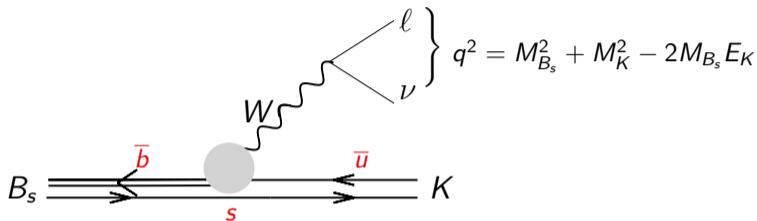
$$\mathcal{R}_{D^{(*)}}^{\tau/\mu} \equiv \frac{d\Gamma(B \rightarrow D^{(*)}\tau\nu_\tau)/d^2q}{d\Gamma(B \rightarrow D^{(*)}\mu\nu_\mu)/d^2q}$$

- ▶ While SM prediction shown has small error, value for $R_{D^{(*)}}$ is a pheno. estimate
- ▶ Nonperturbative lattice calculation favor B_s over B decays (higher precision)
- ▶ Only the spectator quark differs: $R_{D_s^{(*)}}$ may be a good proxy for $R_{D^{(*)}}$

[HFLAV]



$|V_{ub}|$ from exclusive semileptonic $B_s \rightarrow K\ell\nu$ decay



- Conventionally parametrized by (neglecting term $\propto m_\ell^2 f_0^2$)

$$\frac{d\Gamma(B_s \rightarrow K\ell\nu)}{dq^2} = \frac{G_F^2}{192\pi^3 M_{B_s}^3} \left[(M_{B_s}^2 + M_K^2 - q^2)^2 - 4M_{B_s}^2 M_K^2 \right]^{3/2} \times |f_+(q^2)|^2 \times |V_{ub}|^2$$

experiment

known

nonperturbative input

CKM

Nonperturbative input

- ▶ Parametrizes interactions due to the (nonperturbative) strong force
- ▶ Use operator product expansion (OPE) to identify short distance contributions
- ▶ Calculate the flavor changing currents as point-like operators using lattice QCD

\Rightarrow Nonperturbative calculation: lattice QCD

\rightarrow Additional challenge $m_b = 4.18\text{GeV} \sim 1000 \times m_d$

$m_c = 1.28\text{GeV} \sim 270 \times m_d$

Set-up

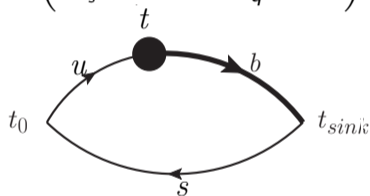
- ▶ RBC-UKQCD's 2+1 flavor domain-wall fermion and Iwasaki gauge action ensembles
 - Three lattice spacings $a \sim 0.11$ fm, 0.08 fm, 0.07 fm; one ensemble with physical pions
[PRD 78 (2008) 114509][PRD 83 (2011) 074508][PRD 93 (2016) 074505][JHEP 1712 (2017) 008]
- ▶ Unitary and partially quenched domain-wall up/down quarks
[Kaplan PLB 288 (1992) 342], [Shamir NPB 406 (1993) 90]
- ▶ Domain-wall strange quarks at/near the physical value
- ▶ Charm: Möbius domain-wall fermions optimized for heavy quarks [Boyle et al. JHEP 1604 (2016) 037]
 - Simulate 3 or 2 charm-like masses then extrapolate/interpolate
- ▶ Effective relativistic heavy quark (RHQ) action for bottom quarks
[Christ et al. PRD 76 (2007) 074505], [Lin and Christ PRD 76 (2007) 074506]
 - Builds upon Fermilab approach [El-Khadra et al. PRD 55 (1997) 3933]
 - Allows to tune the three parameters ($m_0 a$, c_P , ζ) nonperturbatively [PRD 86 (2012) 116003]
 - Smooth continuum limit; heavy quark treated to all orders in $(m_b a)^n$

$$B_s \rightarrow K l \nu$$

$B_s \rightarrow K\ell\nu$ form factors

- ▶ Parametrize the hadronic matrix element for the flavor changing vector current V^μ in terms of the form factors $f_+(q^2)$ and $f_0(q^2)$

$$\langle K | V^\mu | B_s \rangle = f_+(q^2) \left(p_{B_s}^\mu + p_K^\mu - \frac{M_{B_s}^2 - M_K^2}{q^2} q^\mu \right) + f_0(q^2) \frac{M_{B_s}^2 - M_K^2}{q^2} q^\mu$$



- ▶ Calculate 3-point function by
 - Inserting a quark source for a “light” propagator at t_0
 - Allow it to propagate to t_{sink} , turn it into a sequential source for a b quark
 - Use another “light” quark propagating from t_0 and contract both at t

Determining $B_s \rightarrow K\ell\nu$ form factors f_+ and f_0 on the lattice

- ▶ Updating calculation [PRD 91 (2015) 074510] with new values for a^{-1} and RHQ parameters
- ▶ New analysis directly fitting form factors and accounting for excited state contributions
- ▶ On the lattice we prefer using the B_s -meson rest frame and compute

$$f_{\parallel}(E_K) = \langle K | V^0 | B_s \rangle / \sqrt{2M_{B_s}} \quad \text{and} \quad f_{\perp}(E_K) p_K^i = \langle K | V^i | B_s \rangle / \sqrt{2M_{B_s}}$$

- ▶ Both are related by

$$f_0(q^2) = \frac{\sqrt{2M_{B_s}}}{M_{B_s}^2 - M_K^2} [(M_{B_s} - E_K) f_{\parallel}(E_K) + (E_K^2 - M_K^2) f_{\perp}(E_K)]$$

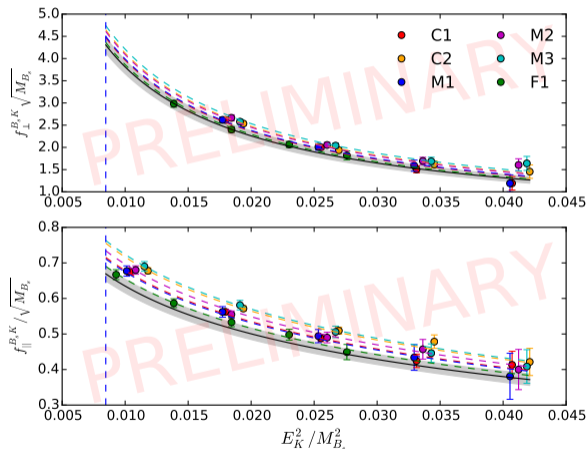
$$f_+(q^2) = \frac{1}{\sqrt{2M_{B_s}}} [f_{\parallel}(E_K) + (M_{B_s} - E_K) f_{\perp}(E_K)]$$

Chiral-continuum extrapolation using SU(2) hard-kaon χ PT

$$f_{\perp}(M_K, E_K, a^2) = \frac{1}{E_K + \Delta} c_{\perp}^{(1)} \times \left[1 + \frac{\delta f_{\perp}}{(4\pi f)^2} + c_{\perp}^{(2)} \frac{M_K^2}{\Lambda^2} + c_{\perp}^{(3)} \frac{E_K}{\Lambda} + c_{\perp}^{(4)} \frac{E_K^2}{\Lambda^2} + c_{\perp}^{(5)} \frac{a^2}{\Lambda^2 a_{32}^4} \right]$$

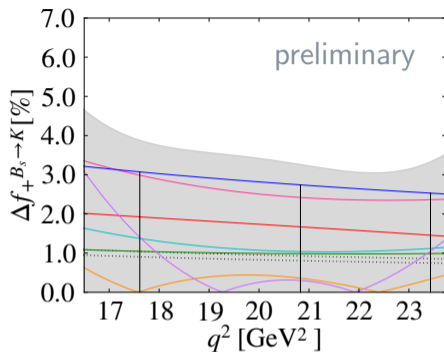
$$f_{\parallel}(M_K, E_K, a^2) = \frac{1}{E_K + \Delta} c_{\parallel}^{(1)} \times \left[1 + \frac{\delta f_{\parallel}}{(4\pi f)^2} + c_{\parallel}^{(2)} \frac{M_K^2}{\Lambda^2} + c_{\parallel}^{(3)} \frac{E_K}{\Lambda} + c_{\parallel}^{(4)} \frac{E_K^2}{\Lambda^2} + c_{\parallel}^{(5)} \frac{a^2}{\Lambda^2 a_{32}^4} \right]$$

with δf non-analytic logs of the kaon mass
and hard-kaon limit is taken by $M_K/E_K \rightarrow 0$



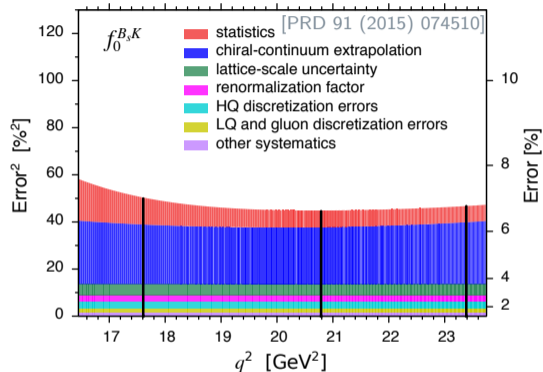
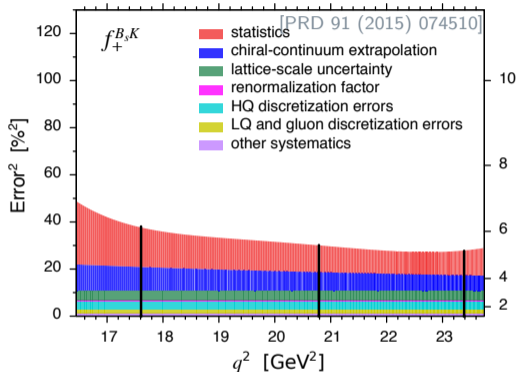
Estimate systematic errors due to

- ▶ Chiral-continuum extrapolation
 - Use alternative fit functions
 - Impose different cuts on the data
- ▶ Uncertainties of the lattice spacing (a^{-1})
 - Repeat the fit varying a^{-1} by its uncertainty
- ▶ Uncertainty of the renormalization factors
 - Estimate effect of higher loop corrections
- ▶ Discretization errors and uncertainties of light and heavy quarks
 - Vary by uncertainty
 - Carry out additional simulations to test effects on form factors
- ▶ Finite volume, iso-spin breaking, ...



⇒ full error budget

Graphical error budget (plots from previous analysis!)



► Read off values for “synthetic” data points

- Use values in the chiral-continuum limit with uncertainties representing the full error budget
- Chiral-continuum extrapolation performed over range of our data
- Avoids parametrizing lattice artifacts in kinematic expansion

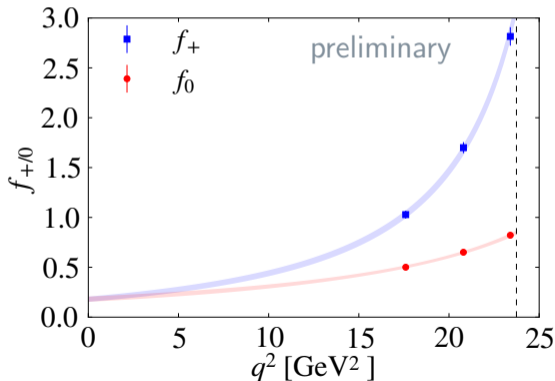
Kinematical extrapolation (z-expansion)

- Map q^2 to z with minimized magnitude in the semileptonic region: $|z| \leq 0.146$

$$z(q^2, t_0) = \frac{\sqrt{1-q^2/t_+} - \sqrt{1-t_0/t_+}}{\sqrt{1-q^2/t_+} + \sqrt{1-t_0/t_+}} \quad \text{with} \quad \begin{aligned} t_{\pm} &= (M_B \pm M_{\pi})^2 \\ t_0 &\equiv t_{\text{opt}} = (M_B + M_{\pi})(\sqrt{M_B} - \sqrt{M_{\pi}})^2 \end{aligned}$$

[Boyd, Grinstein, Lebed, PRL 74 (1995) 4603]

[Bourrely, Caprini, Lellouch, PRD 79 (2009) 013008]



- Express f_+ as convergent power series
- f_0 is analytic, except for B^* pole
- Exploit kinematic constraint $f_+ = f_0$ at $q^2 = 0$
- Use HQ power counting to constrain size of f_+ coefficients

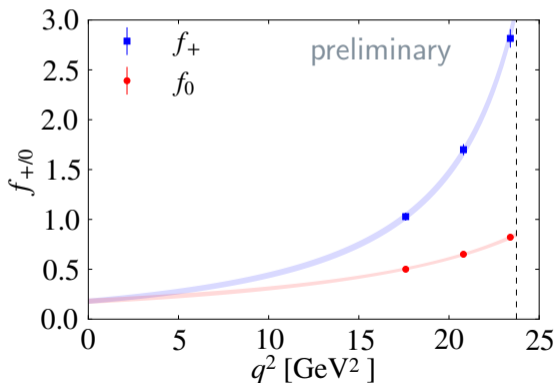
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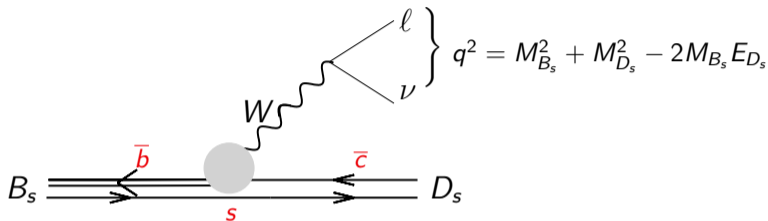
[Bourrely, Caprini, Lellouch, PRD 79 (2009) 013008]



- ▶ Allows to compare shape of form factors
 - Obtained by other lattice calculations [HPQCD PRD90 (2014) 054506]
 - Predicted by QCD sum rules and alike
- ▶ Combination with experiment leads to the overall normalization: $|V_{ub}|$

$$B_s \rightarrow D_s l \nu$$

$|V_{cb}|$ from exclusive semileptonic $B_s \rightarrow D_s\ell\nu$ decay



- Conventionally parametrized by (neglecting term $\propto m_\ell^2 f_0^2$)

$$\frac{d\Gamma(B_s \rightarrow D_s\ell\nu)}{dq^2} = \frac{G_F^2}{192\pi^3 M_{B_s}^3} \left[(M_{B_s}^2 + M_{D_s}^2 - q^2)^2 - 4M_{B_s}^2 M_{D_s}^2 \right]^{3/2} \times |f_+(q^2)|^2 \times |V_{cb}|^2$$

experiment

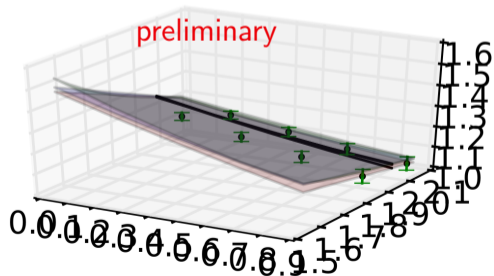
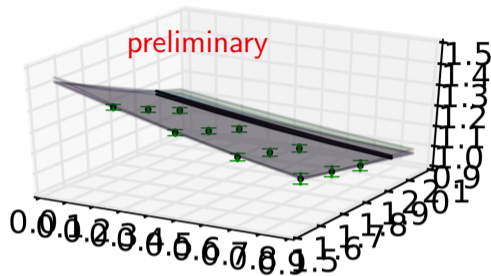
known

nonperturbative input

CKM

Charm extra-/interpolation for $B_s \rightarrow D_s\ell\nu$

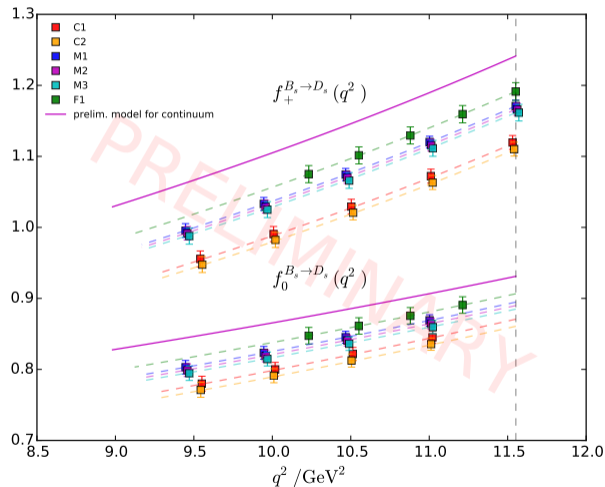
- ▶ Simulate charm quarks using DWF
 - Similar action as for u , d , s quarks
 - “Fully” relativistic setup simplifies renormalization
 - Established by calculating $f_{D_{(s)}}$
[Boyle et al. JHEP 1712 (2017) 008]
- ▶ Coarse ensembles
 - Linearly extrapolate three charm-like masses
- ▶ Medium and fine ensembles
 - Interpolate between two charm-like masses
- ▶ Analysis of data at third, finer lattice spacing will help to better estimate uncertainty



Chiral-continuum extrapolation

- ▶ No light valence quarks, no need for χ PT
- ▶ Account for dependence on
 - charm quark mass
 - lattice spacing
 - light sea-quark mass

$$f(q, a) = \frac{\alpha_0 + \alpha_1 M_{D_s} + \alpha_2 a^2 + \alpha_3 M_\pi^2}{1 + \alpha_4 q^2 / M_{B_s}^2}$$



(Only stat. errors for data points and central value of extrapolation)

conclusion

Conclusion

- ▶ In the final stages to complete $B_s \rightarrow K\ell\nu$ and $B_s \rightarrow D_s\ell\nu$ form factor calculation
 - As usual, carefully estimating all systematic uncertainties is tedious
 - Can even require additional simulations

- ▶ Our lattice calculation also includes
 - $B \rightarrow \pi\ell\nu$, $B \rightarrow \pi\ell^+\ell^-$
 - $B \rightarrow K^*\ell^+\ell^-$
 - $B \rightarrow D^{(*)}\ell\nu$
 - $B_s \rightarrow K^*\ell^+\ell^-$
 - $B_s \rightarrow D_s^*\ell\nu$
 - $B_s \rightarrow \phi\ell^+\ell^-$
 - ...

Resources and Acknowledgments

USQCD: Ds, Bc, and pi0 cluster (Fermilab), qcd12s cluster (Jlab)

RBC qcdcl (RIKEN) and cuth (Columbia U)

UK: ARCHER, Cirrus (EPCC) and DiRAC (UKQCD)

appendix

2+1 Flavor Domain-Wall Iwasaki ensembles

L	$a^{-1}(\text{GeV})$	am_l	am_s	$M_\pi(\text{MeV})$	# configs.	#sources	
24	1.784	0.005	0.040	338	1636	1	[PRD 78 (2008) 114509]
24	1.784	0.010	0.040	434	1419	1	[PRD 78 (2008) 114509]
32	2.383	0.004	0.030	301	628	2	[PRD 83 (2011) 074508]
32	2.383	0.006	0.030	362	889	2	[PRD 83 (2011) 074508]
32	2.383	0.008	0.030	411	544	2	[PRD 83 (2011) 074508]
48	1.730	0.00078	0.0362	139	40	81/1*	[PRD 93 (2016) 074505]
64	2.359	0.000678	0.02661	139	—	—	[PRD 93 (2016) 074505]
48	2.774	0.002144	0.02144	234	70	24	[arXiv:1701.02644]

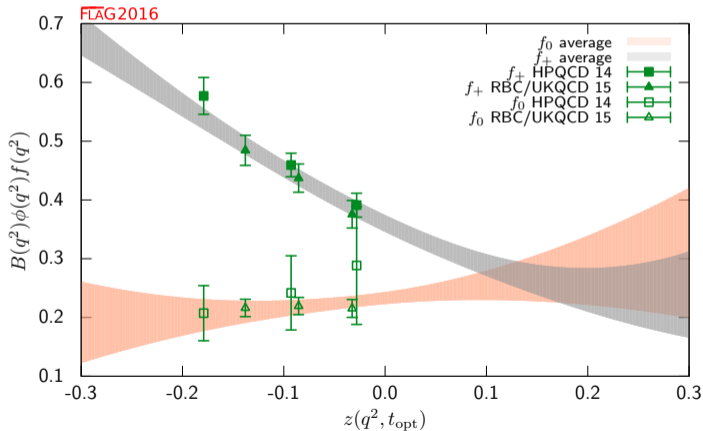
* All mode averaging: 81 “sloppy” and 1 “exact” solve [Blum et al. PRD 88 (2012) 094503]

► Lattice spacing determined from combined analysis [Blum et al. PRD 93 (2016) 074505]

► a : ~ 0.11 fm, ~ 0.08 fm, ~ 0.07 fm

Flavor Lattice Averaging Group

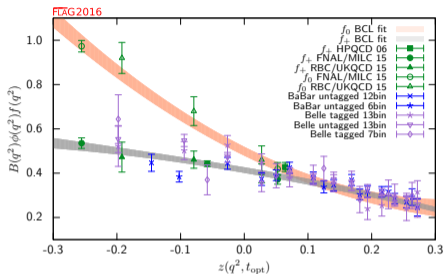
Lattice determinations of $B_s \rightarrow K\ell\nu$ form factors



- ▶ Two independent calculations
 - Different actions
 - Different gauge field ensembles
 - ⇒ Entirely uncorrelated
- ▶ Combined analysis by FLAG

Lattice determinations of $|V_{ub}|$ and $|V_{cb}|$

$B \rightarrow \pi \ell \nu$



$B \rightarrow D \ell \nu$

