

# Nucleon spin structure measurements at JLab

**A. Deur**

Thomas Jefferson National Accelerator Facility

# Why do we study the nucleon spin structure?

\* Spin degrees of freedom: additional handles to test theories.

\* Interesting:  $S_N = \frac{1}{2} = \frac{1}{2}\Delta\Sigma + \Delta G + L_G + L_q$ .

\* Spin permits more complete study of QCD;

\* mechanism of confinement;

\* how effective degrees of freedom (hadrons) emerge from fundamental ones (quark and gluons);

\* Test nucleon/nuclear structure effective theories or models ( $\chi$ PT, AdS/QCD, Dyson-Schwinger Equations...)

\* Precise PDFs needed for high energy or atomic physics.

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1970s-1980s: success of constituent quark model. Suggests  $S_N = \frac{1}{2}\Delta\Sigma$

EMC (1987):  $\Delta\Sigma \sim 0$

⇒ Nucleon spin composition is not trivial. Thus it reveals interesting information on the nucleon structure and the mechanisms of the strong force

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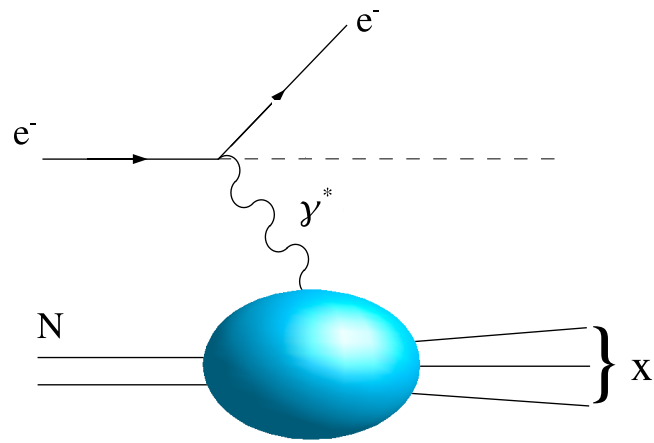
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**JLab is contributing to all these aspects**

# Lepton scattering spin structure experiments (mostly inclusive):



Experiment	Target	Analysis	$W$ (GeV)	$x_{Bj}$	$Q^2$ (GeV <sup>2</sup> )
E80 (SLAC)	p	$A_1$	2.1 to 2.6	0.2 to 0.33	1.4 to 2.7
E130 (SLAC)	p	$A_1$	2.1 to 4.0	0.1 to 0.5	1.0 to 4.1
EMC (CERN)	p	$A_1$	5.9 to 15.2	$1.5 \times 10^{-2}$ to 0.47	3.5 to 29.5
SMC (CERN)	p, d	$A_1$	7.7 to 16.1	$10^{-4}$ to 0.482	0.02 to 57
E142 (SLAC)	<sup>3</sup> He	$A_1, A_2$	2.7 to 5.5	$3.6 \times 10^{-2}$ to 0.47	1.1 to 5.5
E143 (SLAC)	p, d	$A_1, A_2$	1.1 to 6.4	$3.1 \times 10^{-2}$ to 0.75	0.45 to 9.5
E154 (SLAC)	<sup>3</sup> He	$A_1, A_2$	3.5 to 8.4	$1.7 \times 10^{-2}$ to 0.57	1.2 to 15.0
E155/x (SLAC)	p, d	$A_1, A_2$	3.5 to 9.0	$1.5 \times 10^{-2}$ to 0.75	1.2 to 34.7
HERMES (DESY)	p, <sup>3</sup> He	$A_1$	2.1 to 6.2	$2.1 \times 10^{-2}$ to 0.85	0.8 to 20
E94010 (JLab)	<sup>3</sup> He	$g_1, g_2$	1.0 to 2.4	$1.9 \times 10^{-2}$ to 1.0	0.019 to 1.2
EG1a (JLab)	p, d	$A_1$	1.0 to 2.1	$5.9 \times 10^{-2}$ to 1.0	0.15 to 1.8
RSS (JLab)	p, d	$A_1, A_2$	1.0 to 1.9	0.3 to 1.0	0.8 to 1.4
COMPASS (CERN) DIS	p, d	$A_1$	7.0 to 15.5	$4.6 \times 10^{-3}$ to 0.6	1.1 to 62.1
COMPASS (CERN) low- $Q^2$	p, d	$A_1$	5.2 to 19.1	$4 \times 10^{-5}$ to $4 \times 10^{-2}$	0.001 to 1.
EG1b (JLab)	p, d	$A_1$	1.0 to 3.1	$2.5 \times 10^{-2}$ to 1.0	0.05 to 4.2
E99-117 (JLab)	<sup>3</sup> He	$A_1, A_2$	2.0 to 2.5	0.33 to 0.60	2.7 to 4.8
E99-107 (JLab)	<sup>3</sup> He	$g_1, g_2$	2.0 to 2.5	0.16 to 0.20	0.57 to 1.34
E01-012 (JLab)	<sup>3</sup> He	$g_1, g_2$	1.0 to 1.8	0.33 to 1.0	1.2 to 3.3
E97-110 (JLab)	<sup>3</sup> He	$g_1, g_2$	1.0 to 2.6	$2.8 \times 10^{-3}$ to 1.0	0.006 to 0.3
EG4 (JLab)	p, n	$g_1$	1.0 to 2.4	$7.0 \times 10^{-3}$ to 1.0	0.003 to 0.84
SANE (JLab)	p	$A_1, A_2$	1.4 to 2.8	0.3 to 0.85	2.5 to 6.5
EG1dvcs (JLab)	p	$A_1$	1.0 to 3.1	$6.9 \times 10^{-2}$ to 0.63	0.61 to 5.8
E06-014 (JLab)	<sup>3</sup> He	$g_1, g_2$	1.0 to 2.9	0.25 to 1.0	1.9 to 6.9
E06-010/011 (JLab)	<sup>3</sup> He	single spin asy.	2.4 to 2.9	0.16 to 0.35	1.4 to 2.7
E07-013 (JLab)	<sup>3</sup> He	single spin asy.	1.7 to 2.9	0.16 to 0.65	1.1 to 4.0
E08-027 (JLab)	p	$g_1, g_2$	1. to 2.1	$3.0 \times 10^{-3}$ to 1.0	0.02 to 0.4

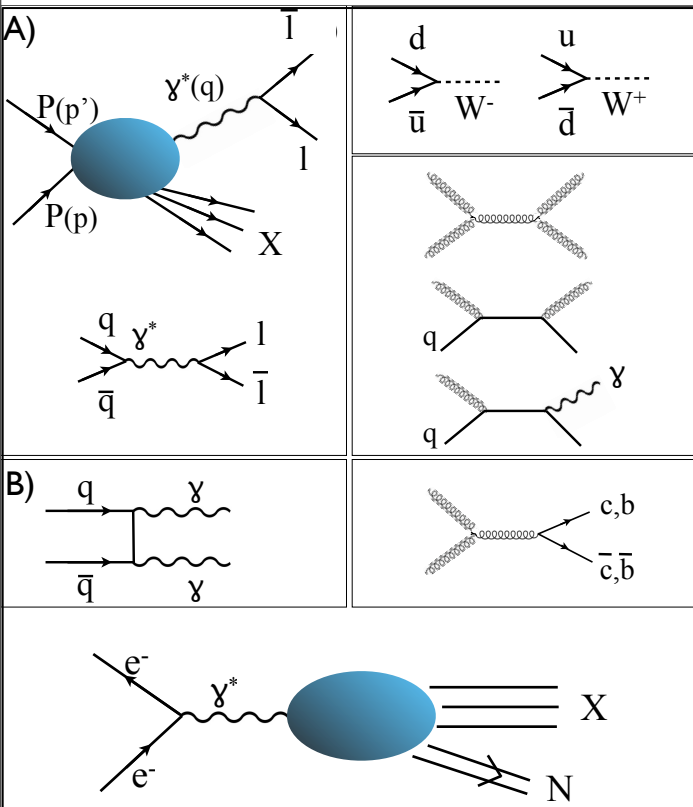


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Pol. SIDIS experiments.  
Colliders experiments:



# Car traffic photos

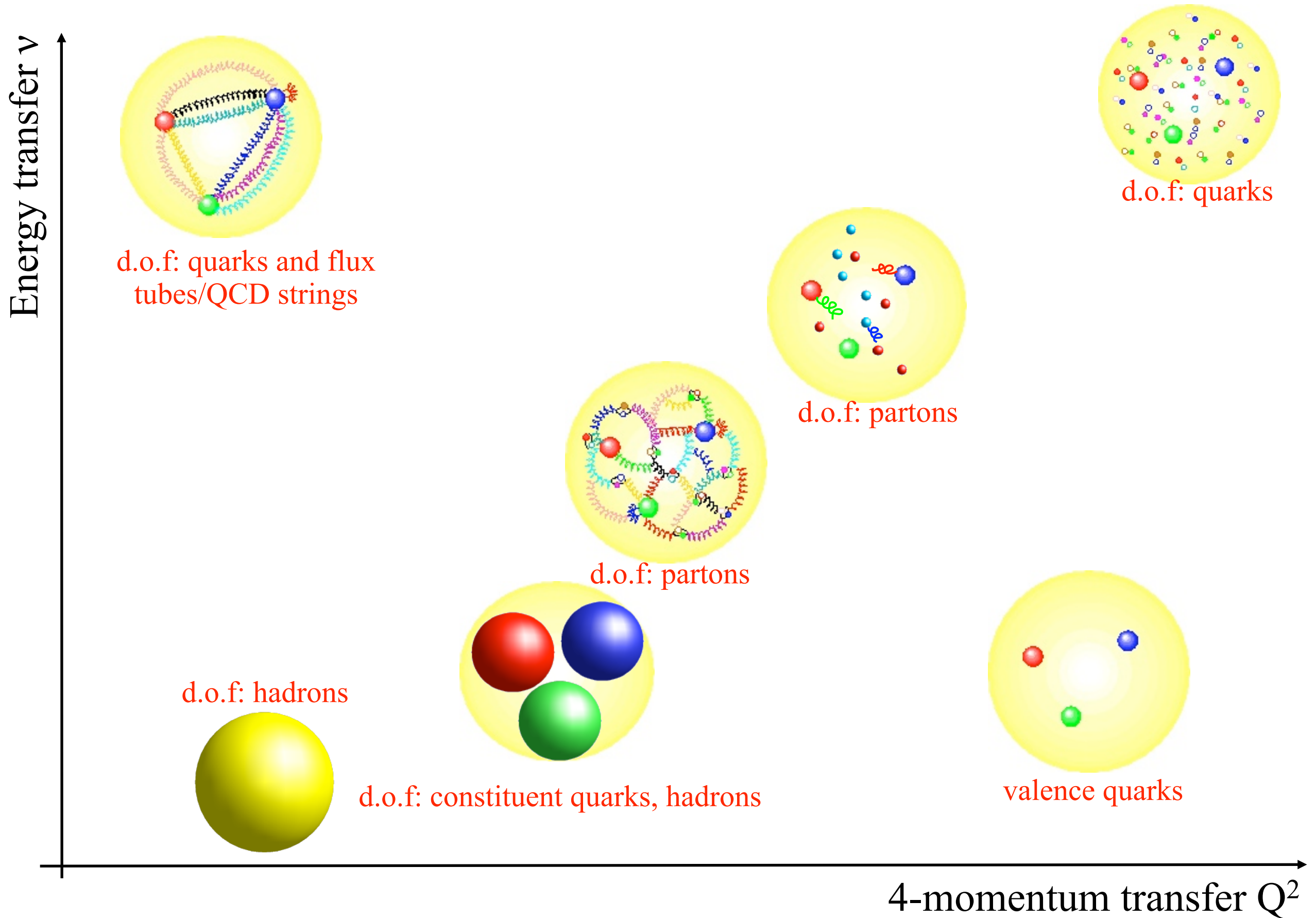
(Exposure time)<sup>-1</sup>



Resolution

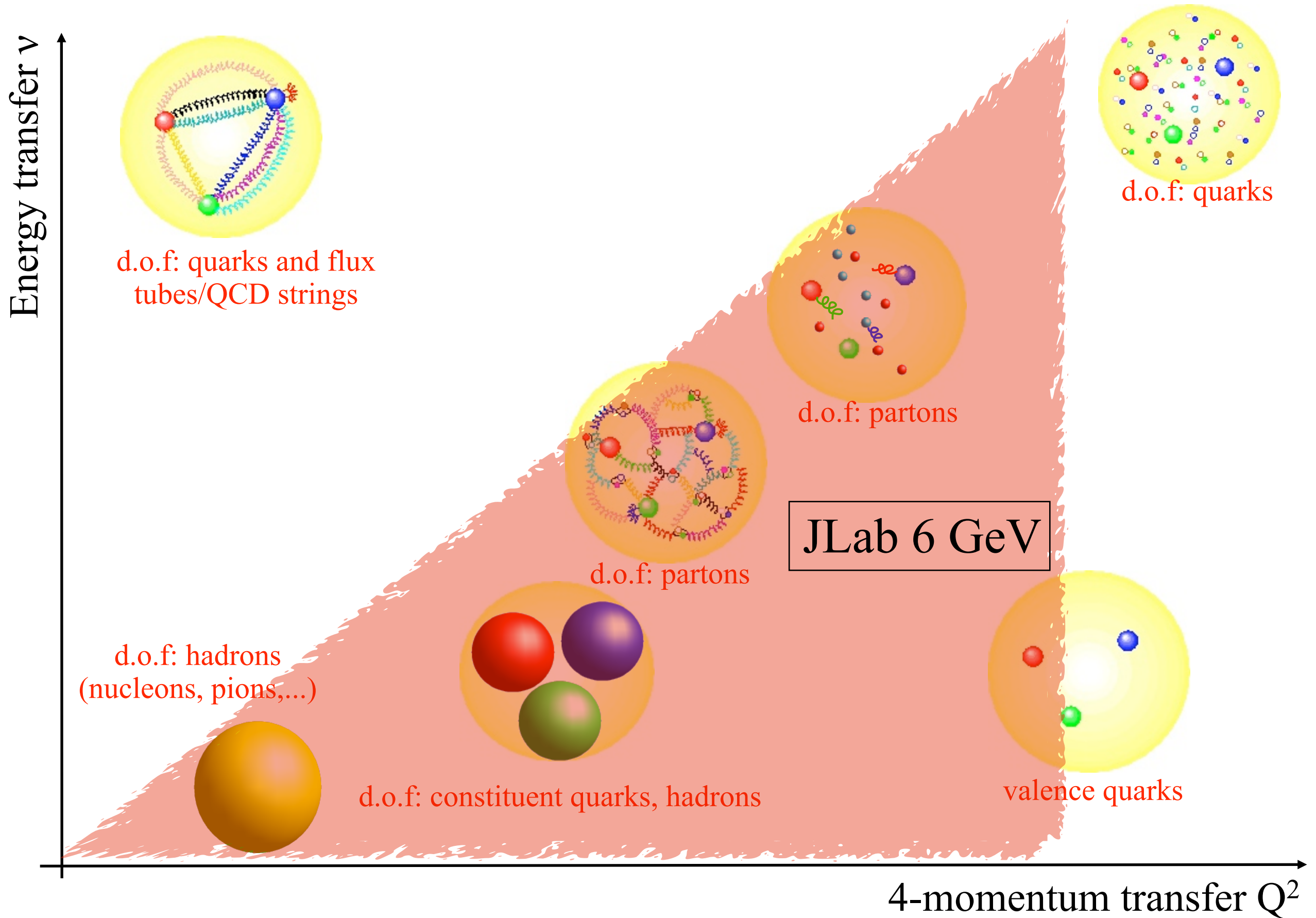


# JLab's spin program and the multiple aspects the nucleon

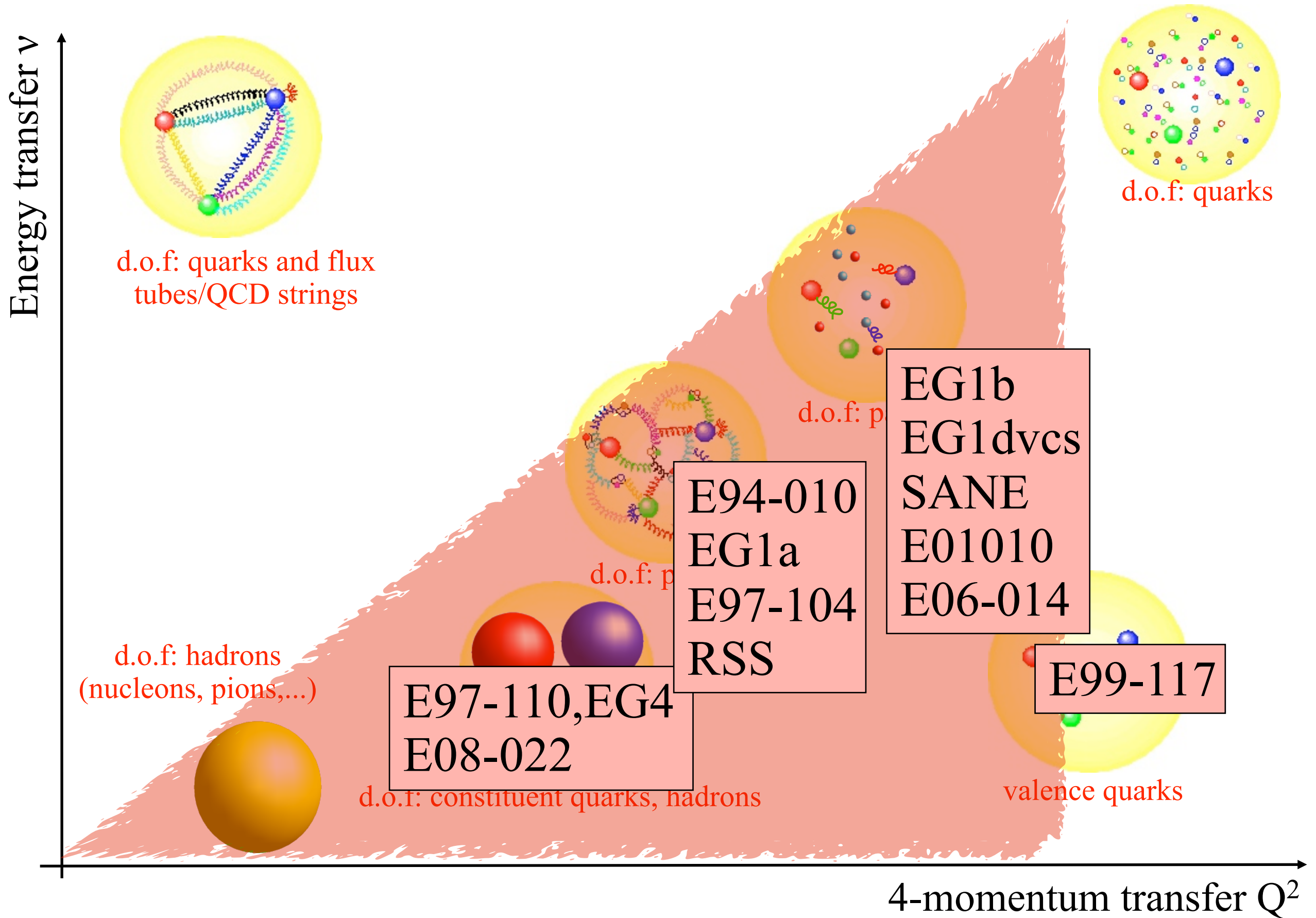




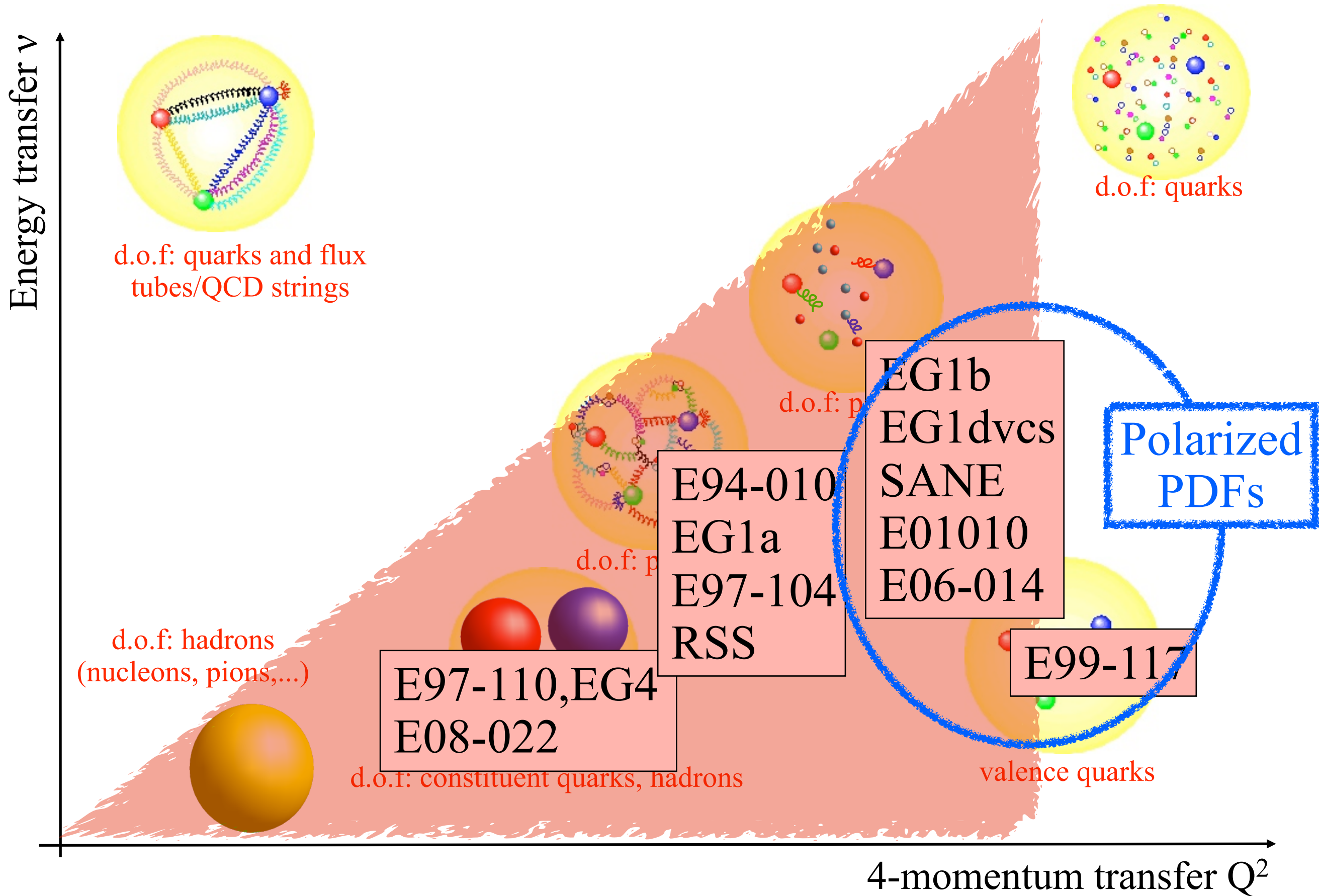
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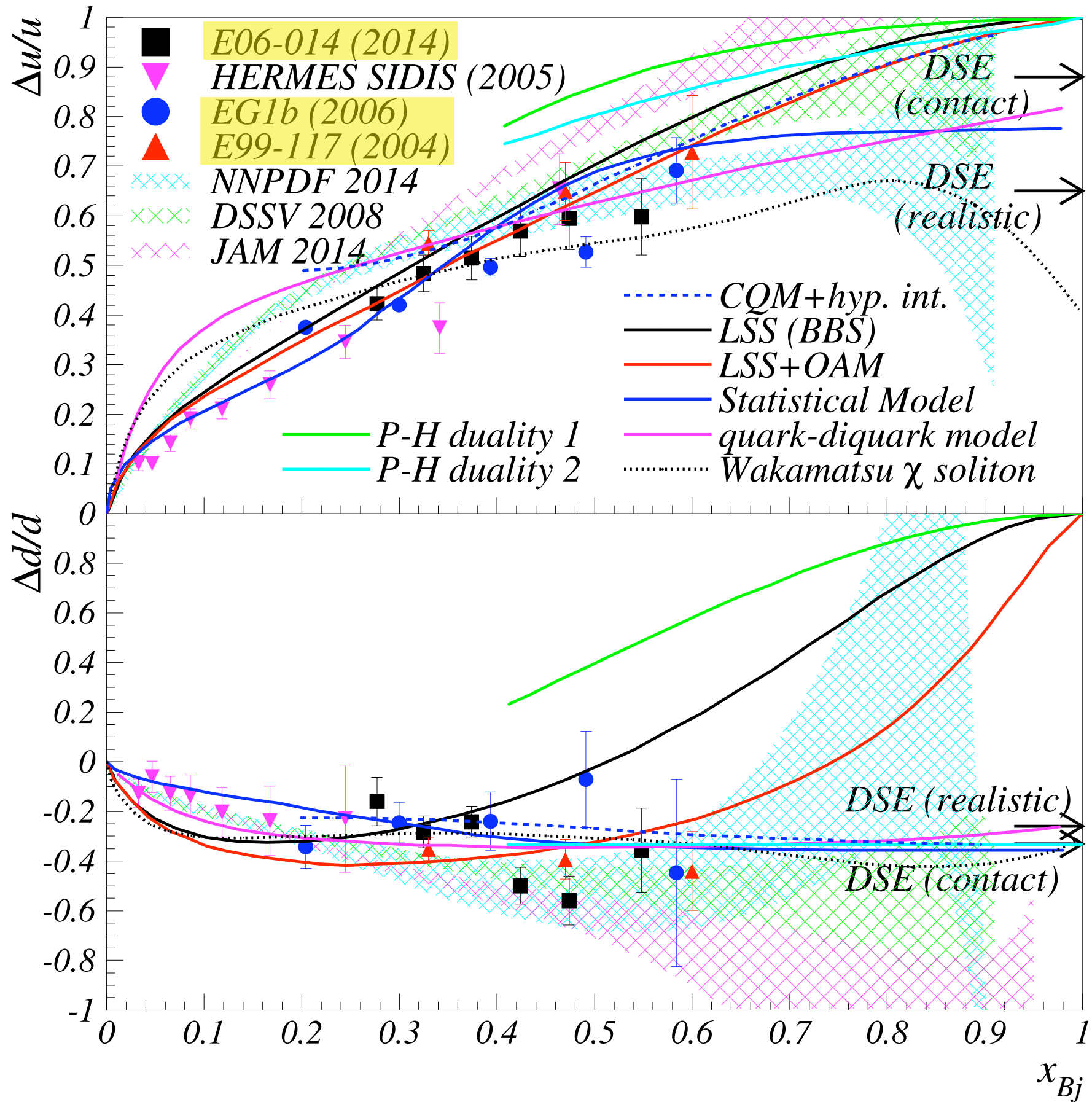
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# PDFs measurements at JLab



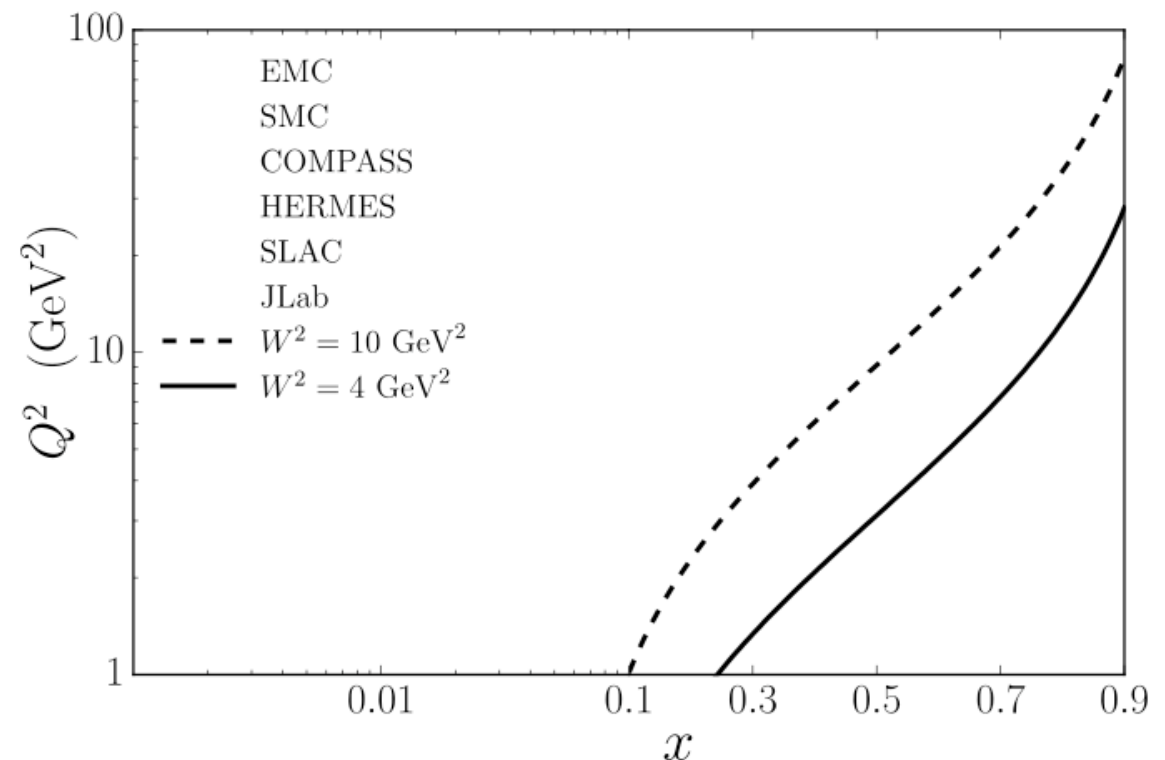
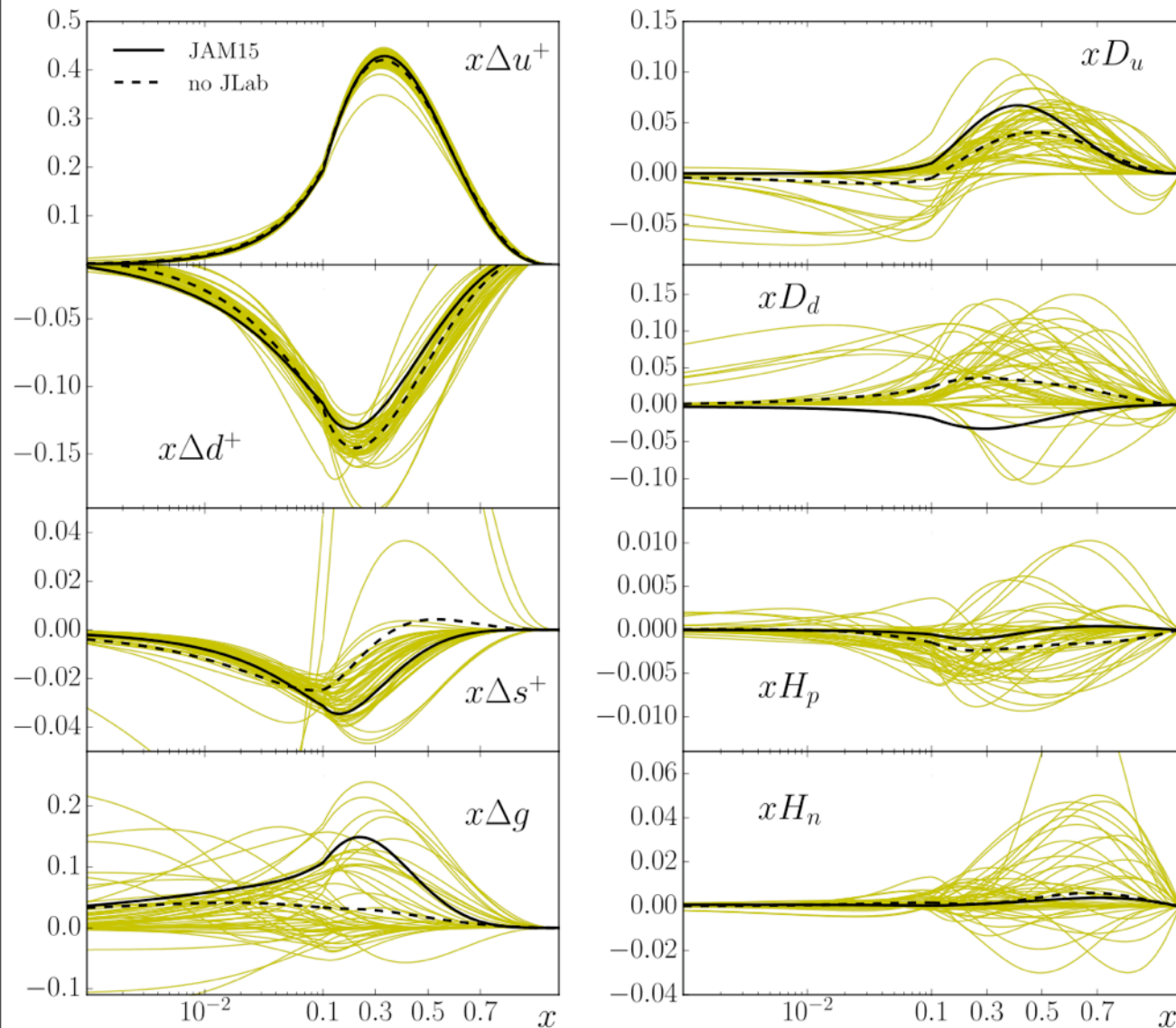


## JAM15 Analysis – Impact of JLab Data

$$g_1(x, Q^2) = g_1^{\text{LT+TMC}}(\Delta u^+, \Delta d^+, \Delta g, \dots) + g_1^{\text{T3+TMC}}(D_u, D_d) + g_1^{\text{T4}}(H_{p,n})$$

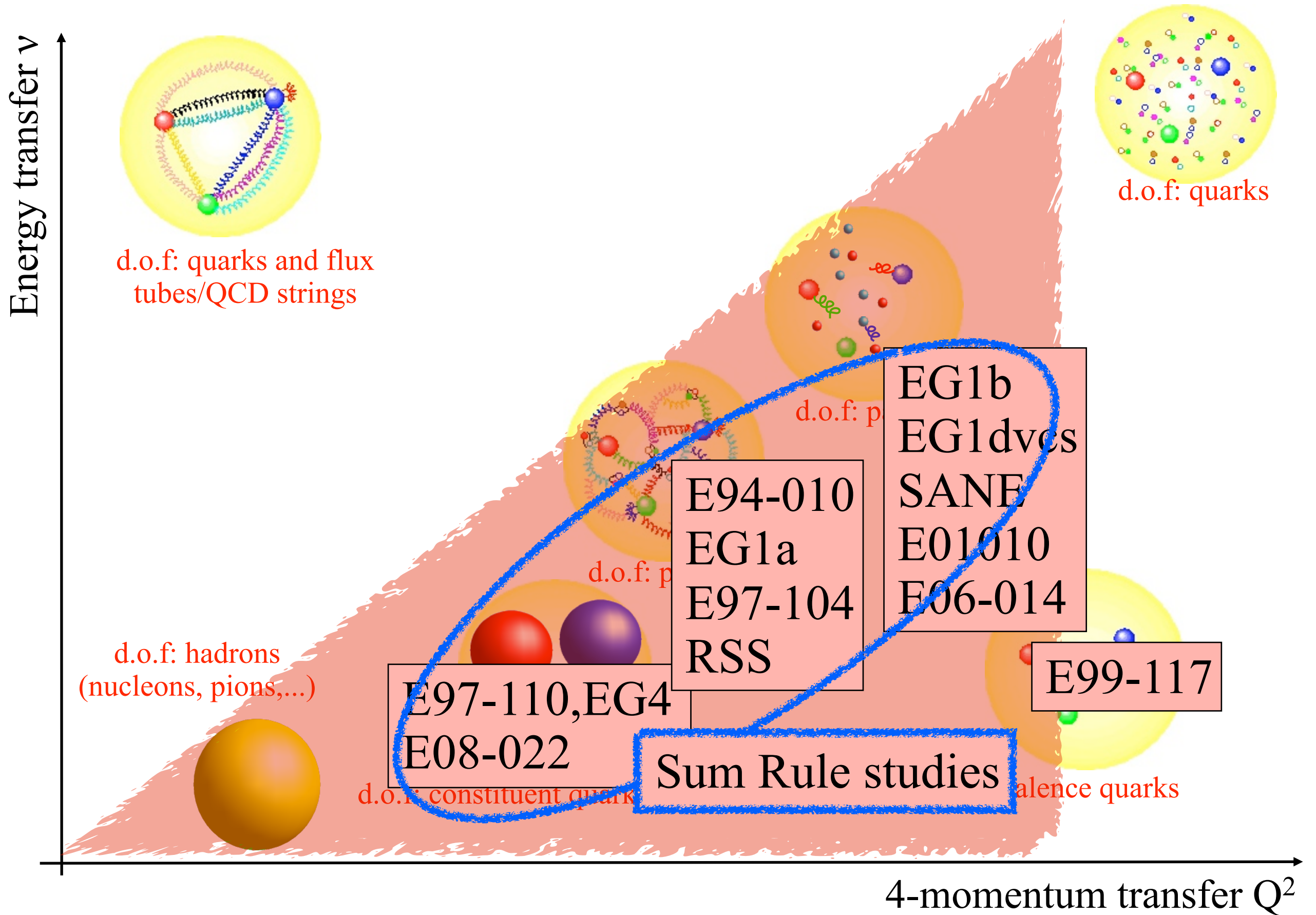
$$g_2(x, Q^2) = g_2^{\text{LT+TMC}}(\Delta u^+, \Delta d^+, \Delta g, \dots) + g_2^{\text{T3+TMC}}(D_u, D_d)$$

N. Sato et. al. Phys. Rev. D93 074005 (2016)



- Reduction of uncertainties in region  $0.1 < x < 0.7$
- Impact on low- $x$  uncertainties from imposing  $SU(3)_f$  constraints
- JLab data prefers positive glue for  $x > 0.1$   
 → constrained via evolution
- Non-zero twist-3 quark distributions ; twist-4 consistent with zero

# JLab's spin program and the multiple aspects the nucleon



# Sum Rules

**Bjorken sum rule** (most famous sum rule of polarized lepton scattering):

$$\int g_1^p - g_1^n dx = \frac{1}{6} g_a \left( 1 + \frac{\alpha_s(Q^2)}{\pi} + \dots \right) + \text{non-pert. cor.}$$

↑  
Axial charge

# The Gerasimov-Drell-Hearn Sum Rule

GDH sum rule:

$$\int_{v_{\text{thr}}}^{\infty} (\sigma^{1/2} - \sigma^{3/2}) \frac{dv}{v} = \frac{-2\alpha\pi^2\kappa^2}{M^2}$$

Photo-absorption cross sections

Photon energy

anomalous magnetic moment  $\alpha$ : fine structure constant



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Originally derived for photo-absorption ( $Q^2=0$ )

Later generalized to  $Q^2>0$

$$\frac{16\alpha\pi^2}{Q^2} \int_0^1 g_1 dx = 2\alpha\pi^2 S_1$$

spin-dep.  
DDVCS



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**Bjorken sum rule:**

$$\int g_1^p - g_1^n dx = \frac{1}{6} g_a \left( 1 + \frac{\alpha_s(Q^2)}{\pi} + \dots \right) + \text{non-pert. cor.}$$

$$\text{GDH}(\text{proton}) - \text{GDH}(\text{neutron}) \propto Q^2 \times \text{Bjorken sum}$$

# Spin polarizabilities sum rules

Sum rules with higher moments exist, e.g. spin polarizabilities sum rules:

Generalized forward spin polarizability:

$$\gamma_0 = \frac{4e^2 M^2}{\pi Q^6} \int x^2 (g_1 - \frac{4M^2}{Q^2} x^2 g_2) dx$$

Longitudinal-Transverse polarizability:

$$\delta_{LT} = \frac{4e^2 M^2}{\pi Q^6} \int x^2 (g_1 + g_2) dx$$

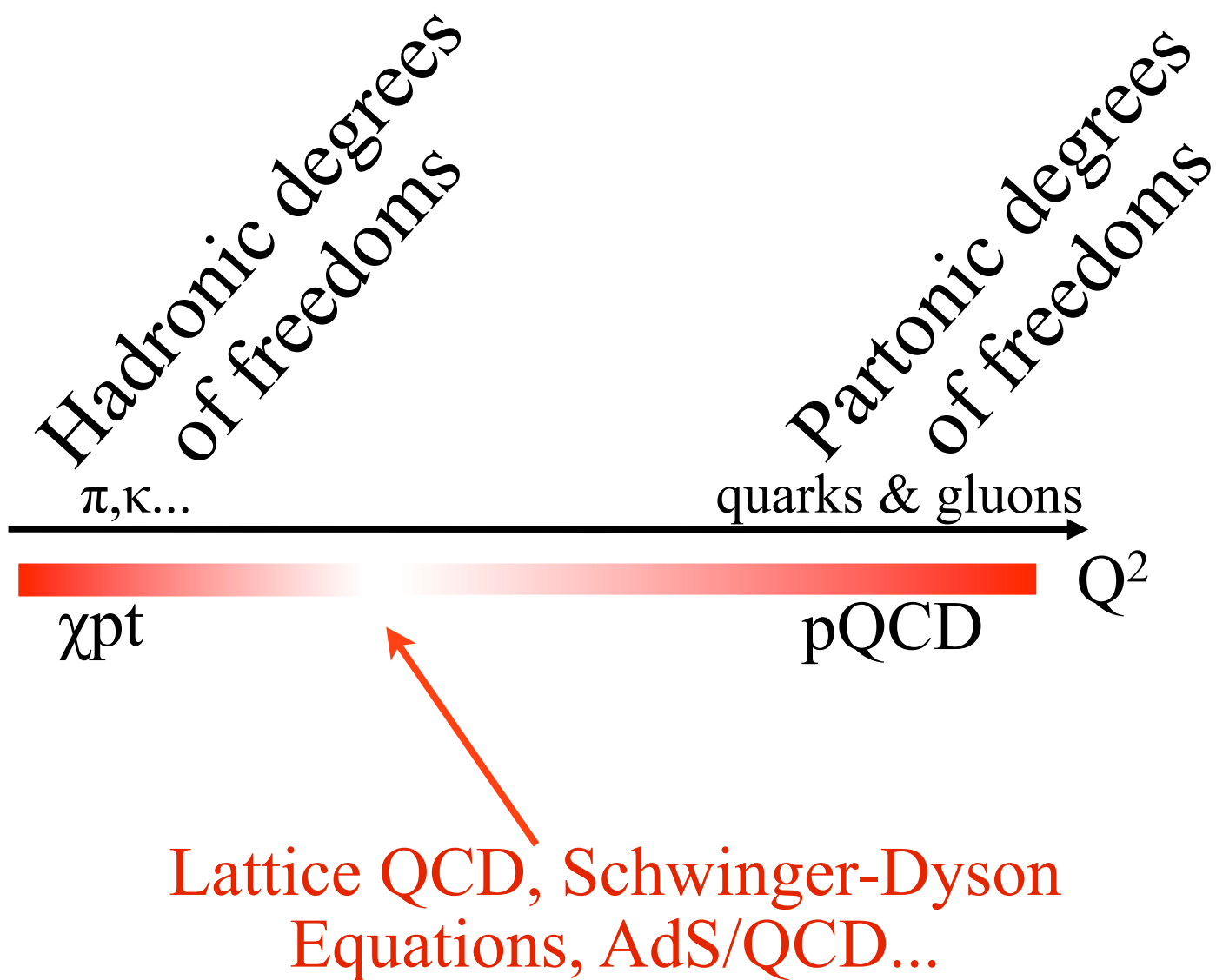
Or twist-3 term  $d_2$ :

$$d_2(Q^2) = \int_0^1 x^2 2g_1(x, Q^2) + 3g_2(x, Q^2) dx$$

# Interest of the generalized GDH sum rule

Sum rule valid at all  $Q^2$ :

We can measure  $\int g_1 dx$  at different  $Q^2$  and compute the other side of the sum rule using different techniques:



⇒ Study transition from hadronic to partonic description of strong force.  
Test Lattice QCD, effective approaches to QCD, and models.

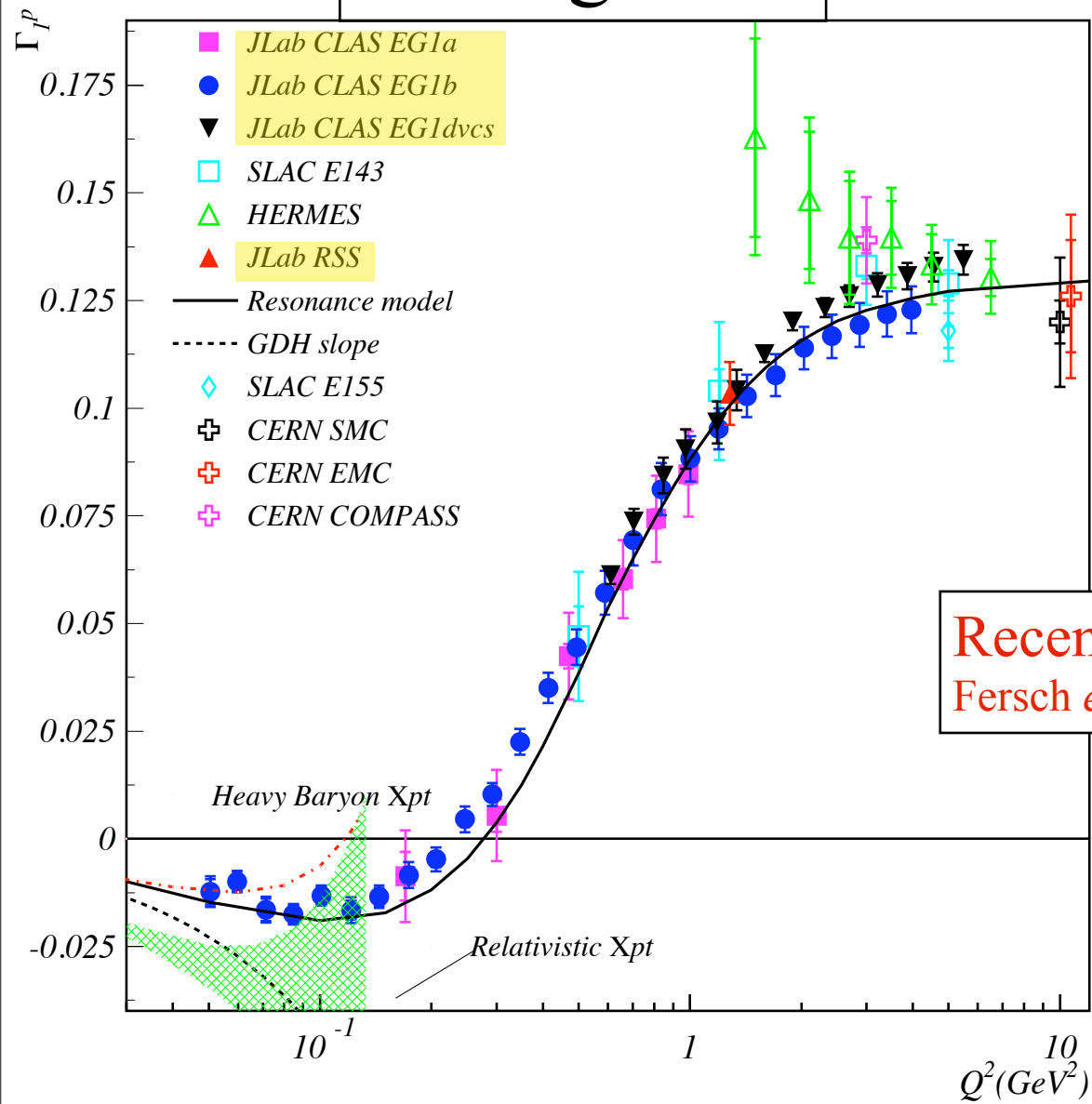
# Existing data on GDH sum



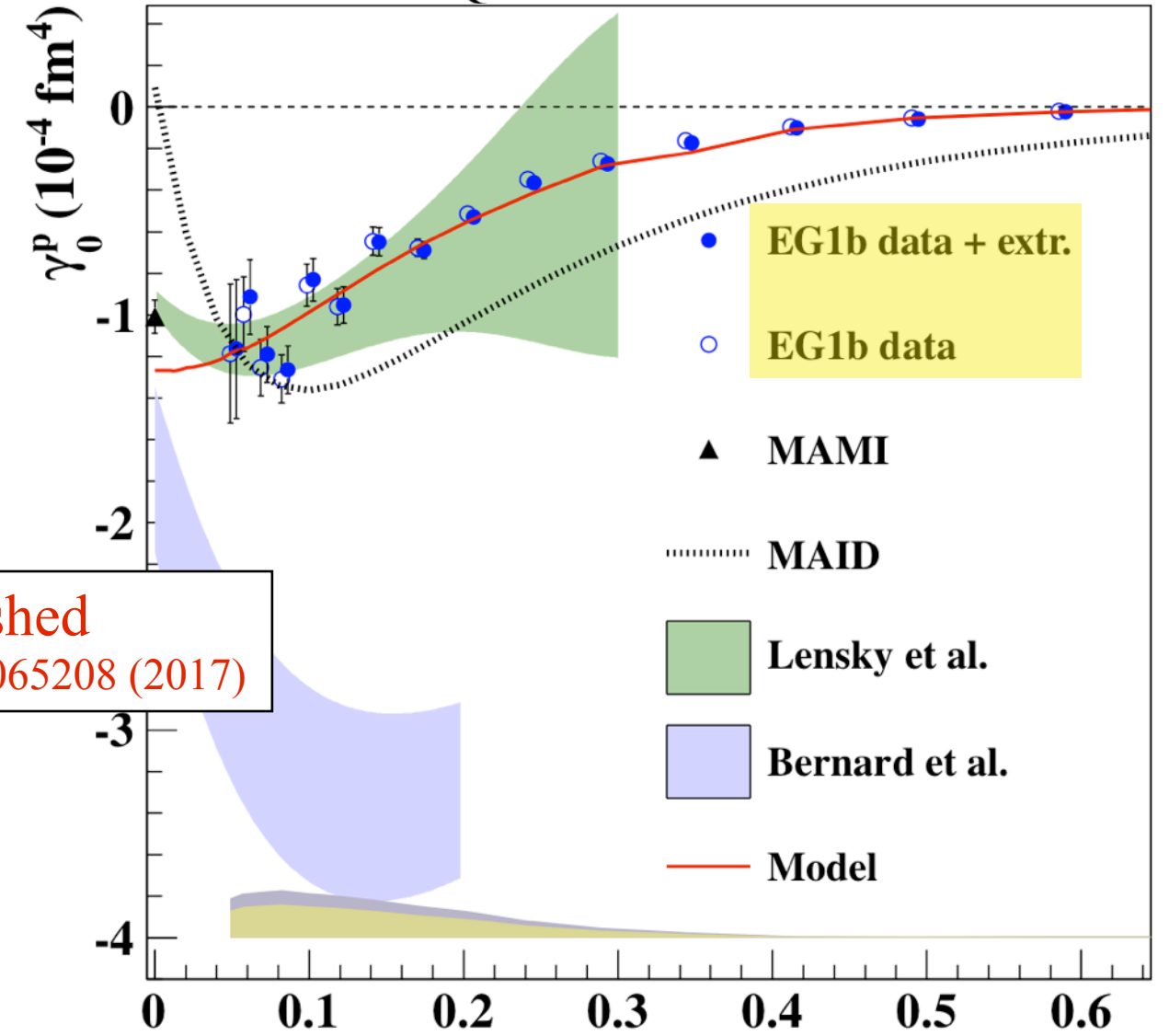
# Existing data (proton)

$$\Gamma_1 = \int g_1 dx$$

$$\gamma_0 = \frac{4e^2 M^2}{\pi Q^6} \int x^2 (g_1 - \frac{4M^2}{Q^2} x^2 g_2) dx$$



Recently published  
Fersch *et al.* PC 96 065208 (2017)



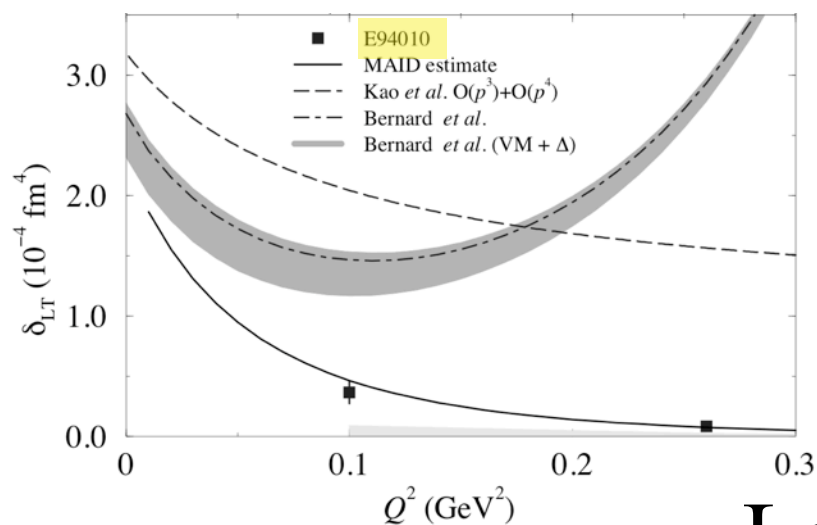
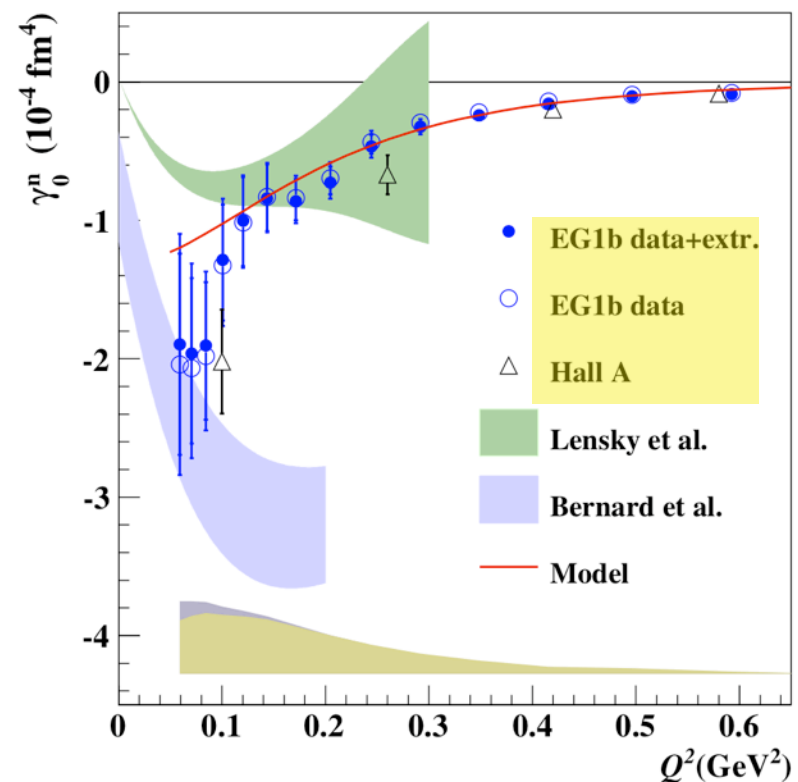
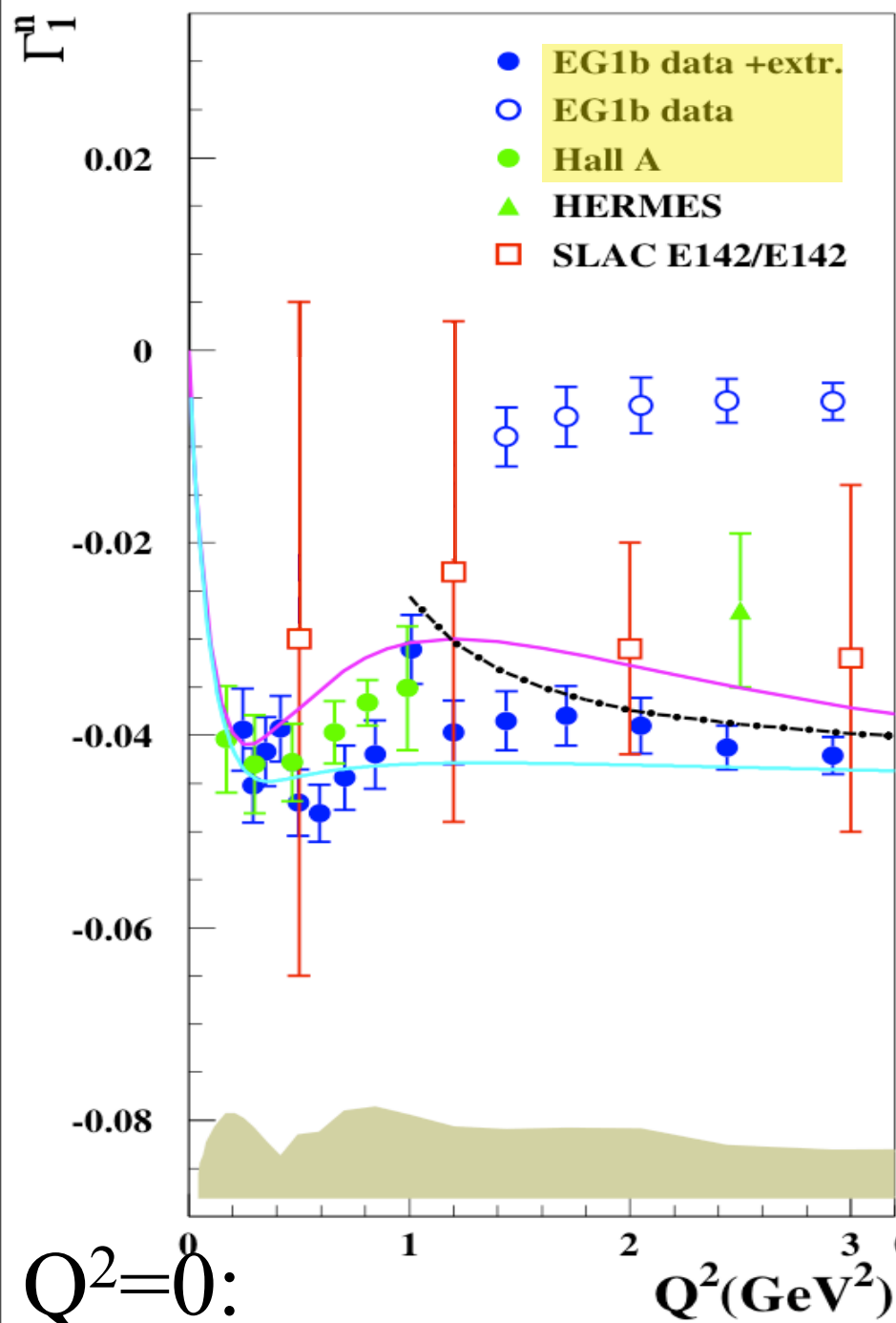
$Q^2=0$ :  
Mainz, Bonn  
BNL

Intermediate  $Q^2$ :  
Jlab Hall A, B & C

Large  $Q^2$ :  
CERN, SLAC,  
DESY (Hermes)



# Existing data (neutron)



$Q^2=0$ :  
Mainz, Bonn  
BNL

Intermediate  $Q^2$ :  
Jlab Hall A, B & C

Large  $Q^2$ :  
CERN, SLAC,  
DESY (Hermes)





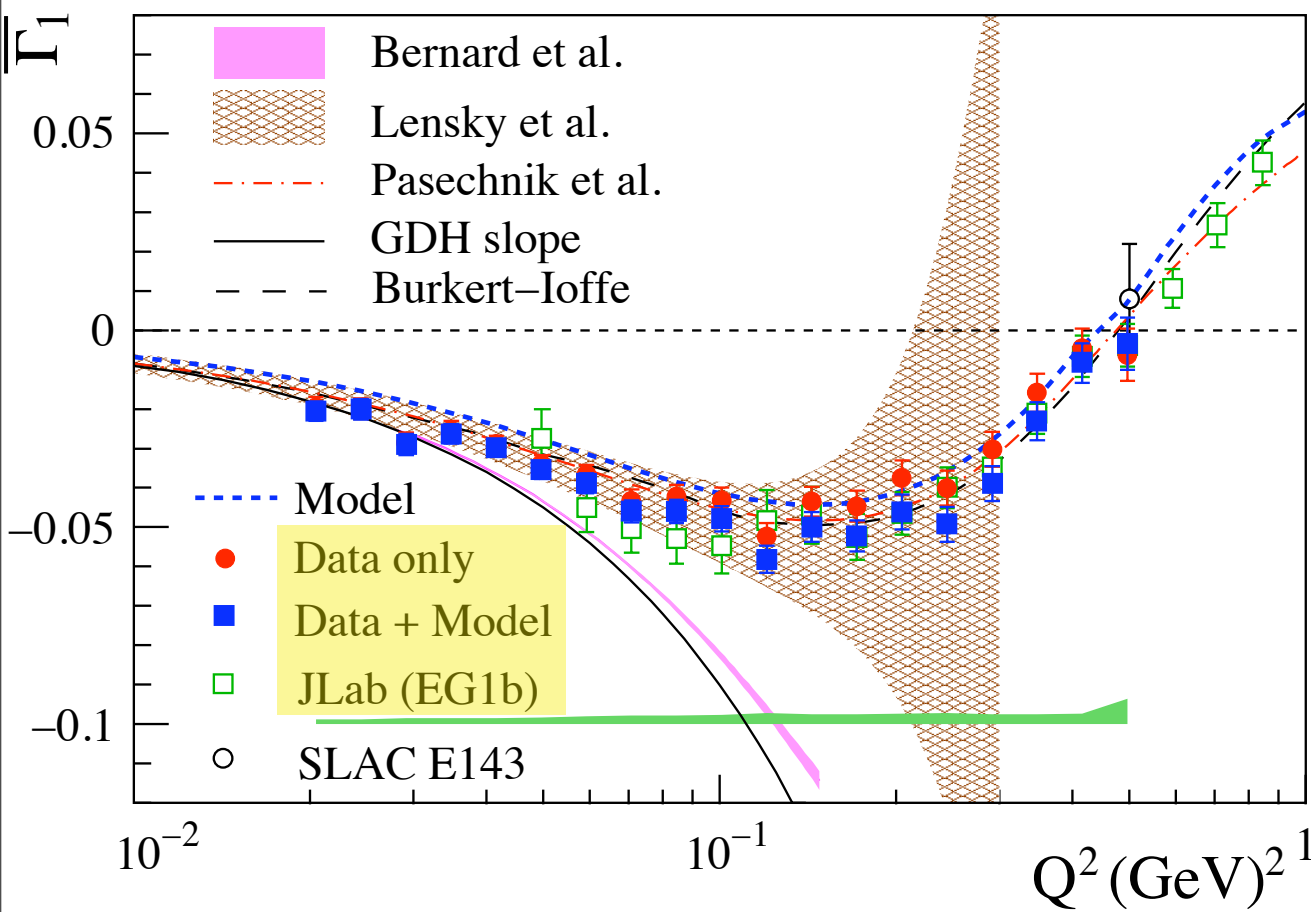
GDH at low  $Q^2$  in:

- \*JLab Hall A: E97-110, neutron( $^3\text{He}$ ), E08-027 (proton)
- \*JLab Hall B: EG4, proton & neutron(D)

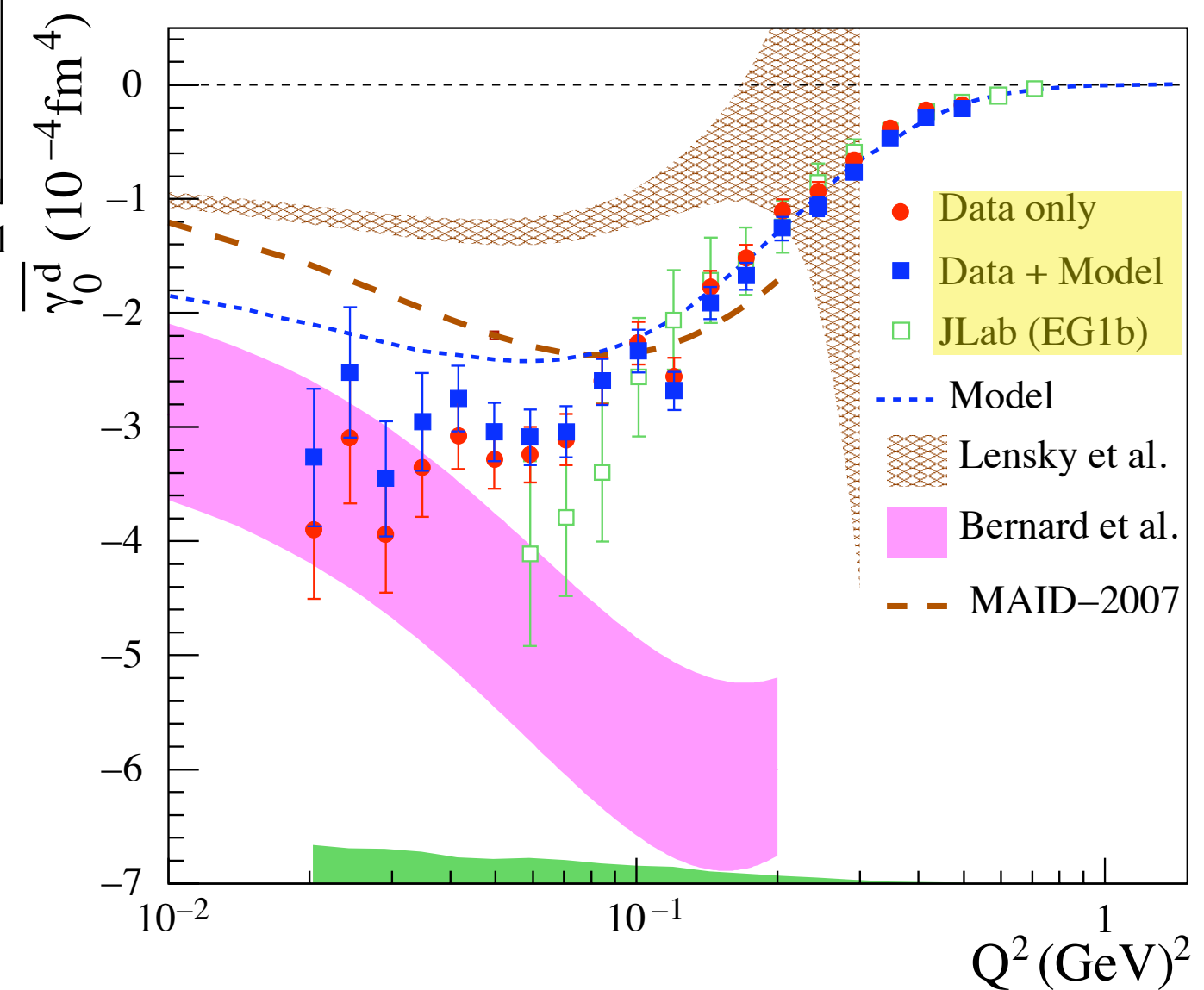
Bridge the remaining gap:



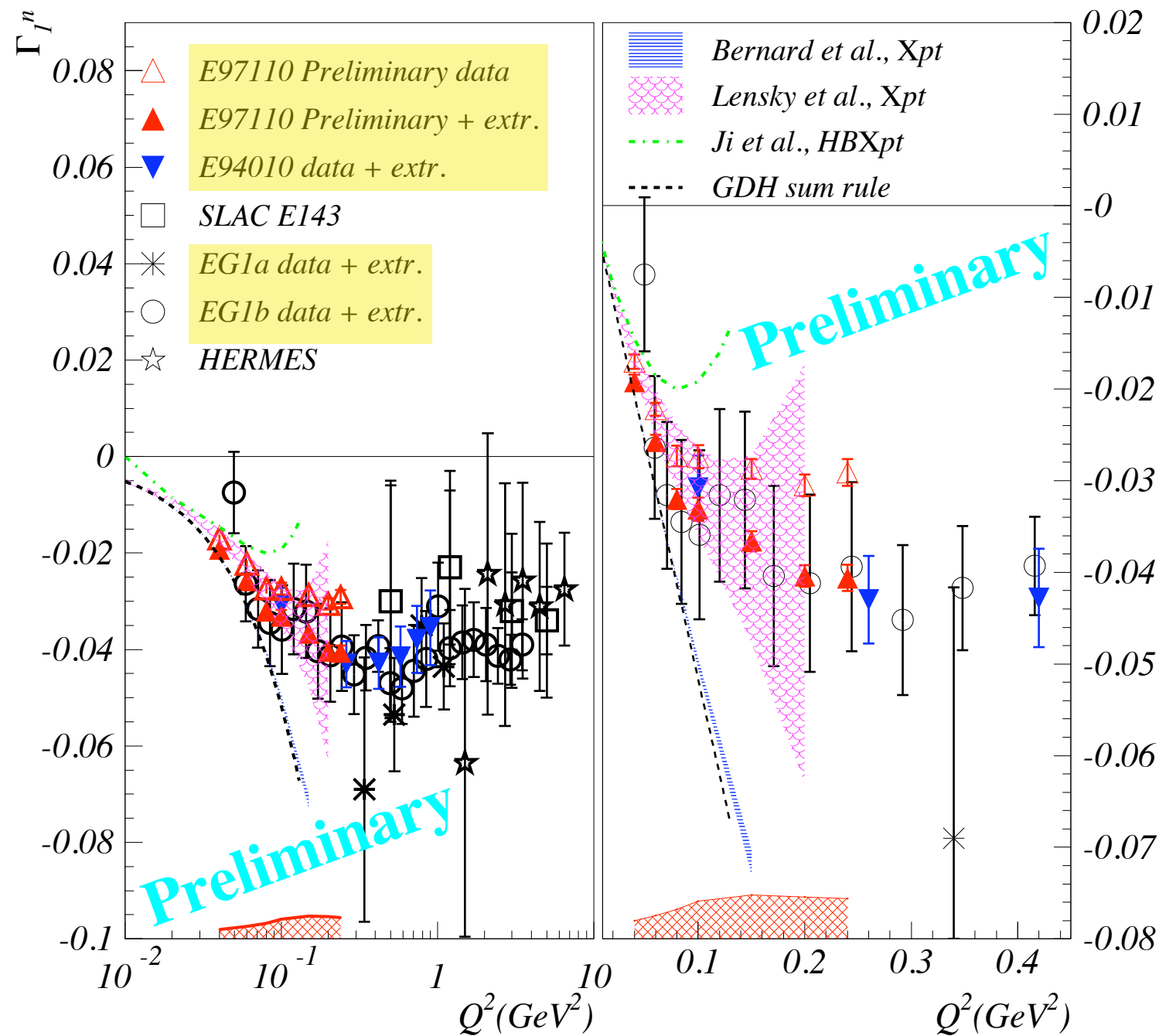
# EG4 Deuteron results on $\int g_1 dx$ and polarizabilities



**Just Published.**  
*Adhikari et al. PRL 120, 062501 (2018)*



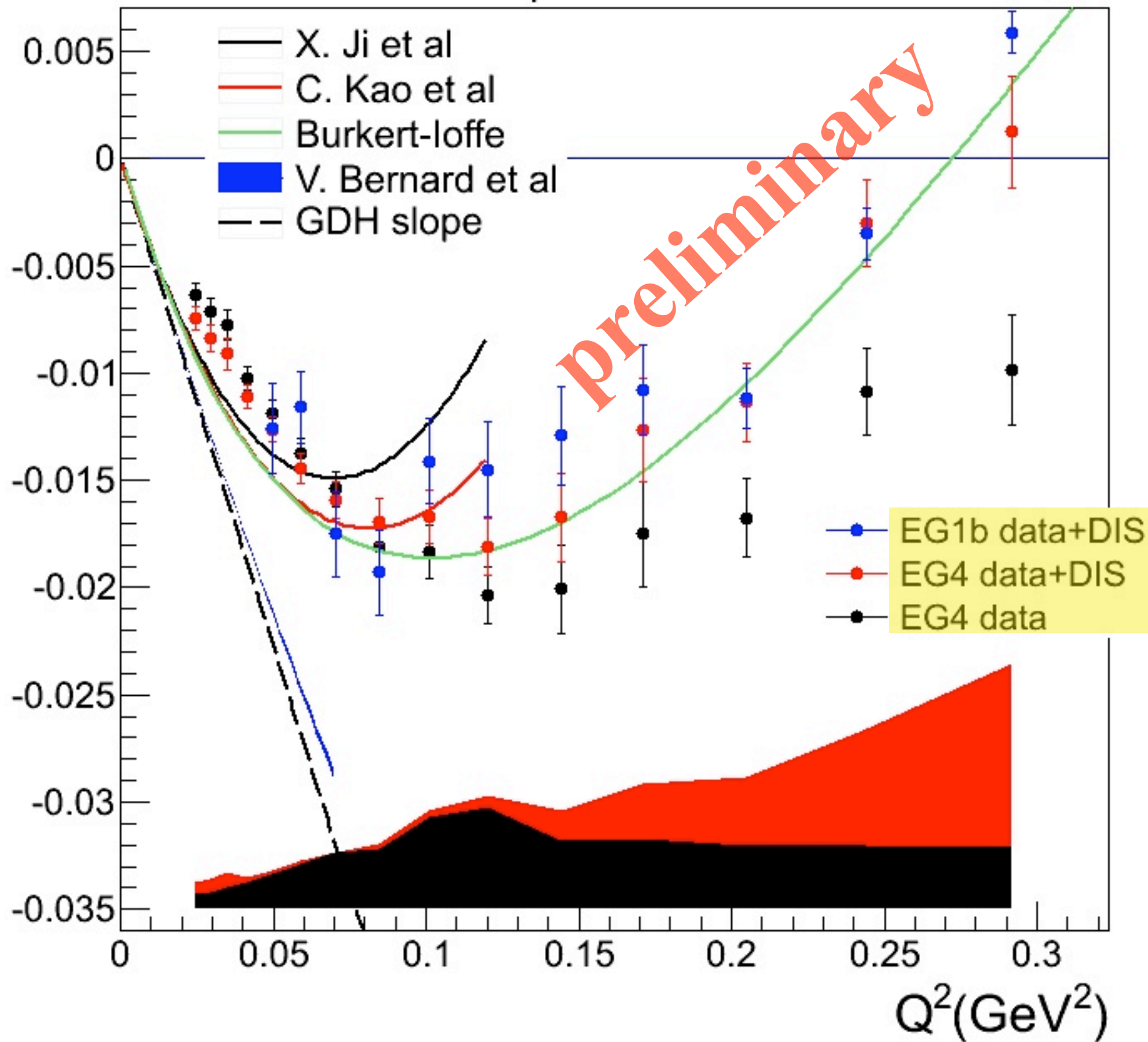
# E97-110 preliminary neutron(<sup>3</sup>He) results on $\int g_1 dx$



**Near final  
(draft paper in June)**

# EG4 preliminary proton results on $J_g dx$

$$\Gamma_1^p(Q^2)$$



What do we learn from these measurements?

# Test of $\chi_{pt}$

Ref.	$\Gamma_1^p$	$\Gamma_1^n$	$\Gamma_1^{p-n}$	$\Gamma_1^{p+n}$	$\gamma_0^p$	$\gamma_0^n$	$\gamma_0^{p-n}$	$\gamma_0^{p+n}$	$\delta_{LT}^n$	$d_2^n$
Ji 1999	X	X	A	X	-	-	-	-	-	-
Bernard 2002	X	X	A	X	X	A	X	X	X	X
Kao 2002	-	-	-	-	X	A	X	X	X	X
Bernard 2012	X	X	A	X	X	A	X	X	X	-
Lensky 2014	X	A	A	A	A	X	X	X	$\sim$ A	A

# Test of $\chi$ pt

No significant low-x contribution  
(More robust observables)



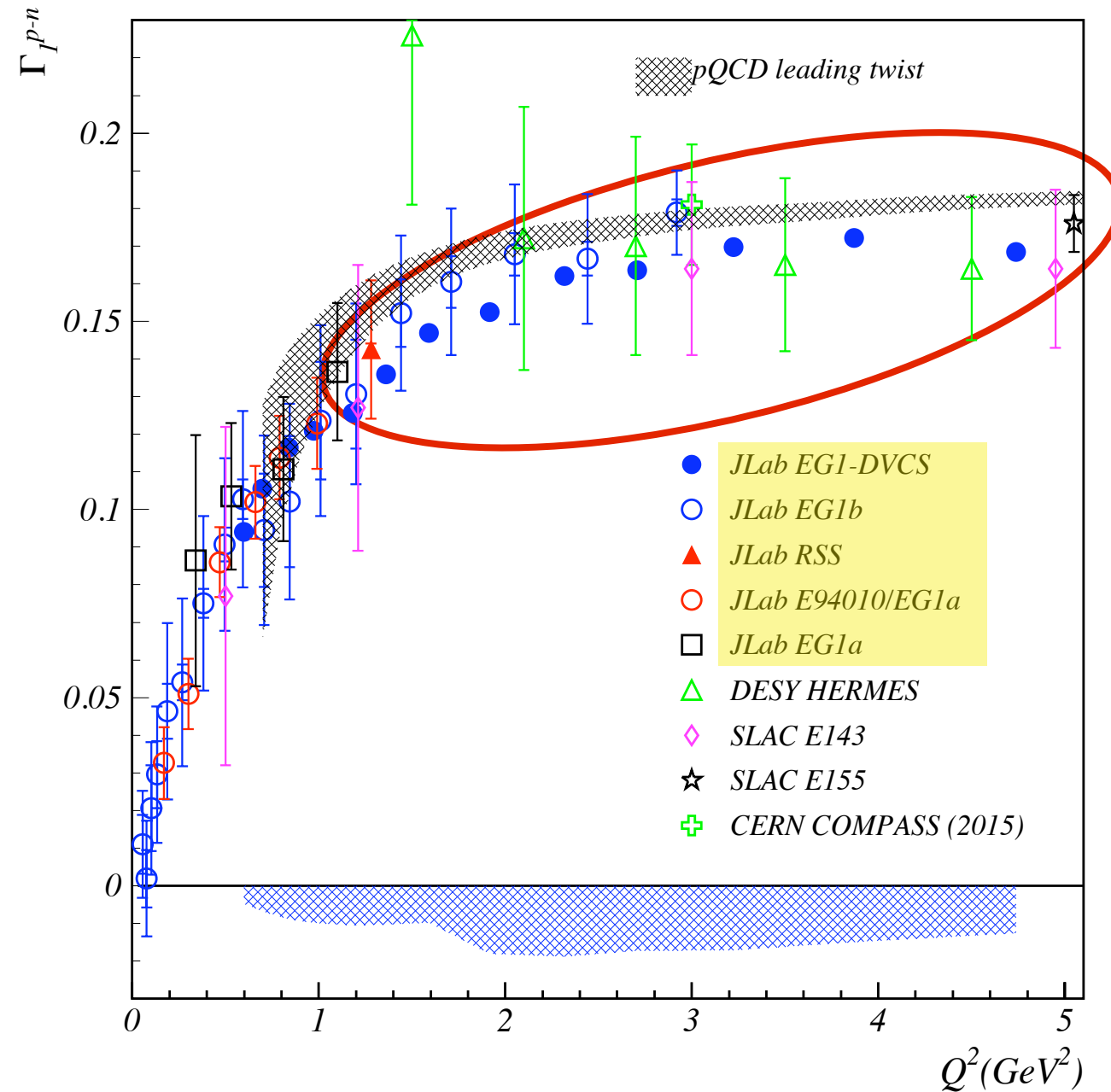
Ref.	$\Gamma_1^p$	$\Gamma_1^n$	$\Gamma_1^{p-n}$	$\Gamma_1^{p+n}$	$\gamma_0^p$	$\gamma_0^n$	$\gamma_0^{p-n}$	$\gamma_0^{p+n}$	$\delta_{LT}^n$	$d_2^n$
Ji 1999	X	X	A	X	-	-	-	-	-	-
Bernard 2002	X	X	A	X	X	A	X	X	X	X
Kao 2002	-	-	-	-	X	A	X	X	X	X
Bernard 2012	X	X	A	X	X	A	X	X	X	-
Lensky 2014	X	A	A	A	A	X	X	X	$\sim$ A	A



No  $\Delta_{1232}$  contributions  
(More robust  $\chi$ pt calculations)

# ”Study transition from hadronic to partonic description of strong force”

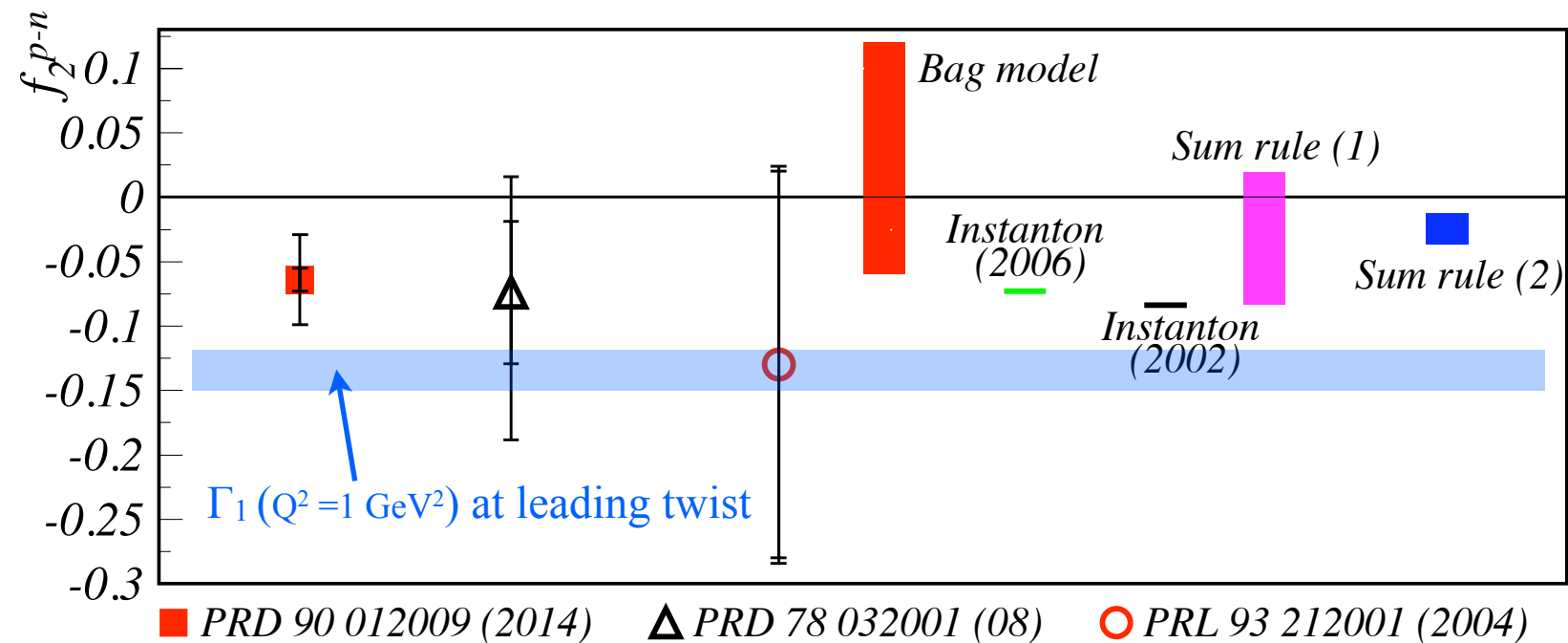
Ex. Bjorken sum data:





”Study transition from hadronic to partonic description of strong force”

Twist-4  $f_2$ : Next to leading twist.  
Extraction at  $Q^2 = 1 \text{ GeV}^2$ .



$f_2$  is large (about half of leading twist at  $Q^2 = 1 \text{ GeV}^2$ ) in accordance to intuition.

Twist-6 is small. Twist-8 is of similar size as  $f_2$  but opposite sign.

Overall, higher twist contribution small at  $Q^2 = 1 \text{ GeV}^2$ .

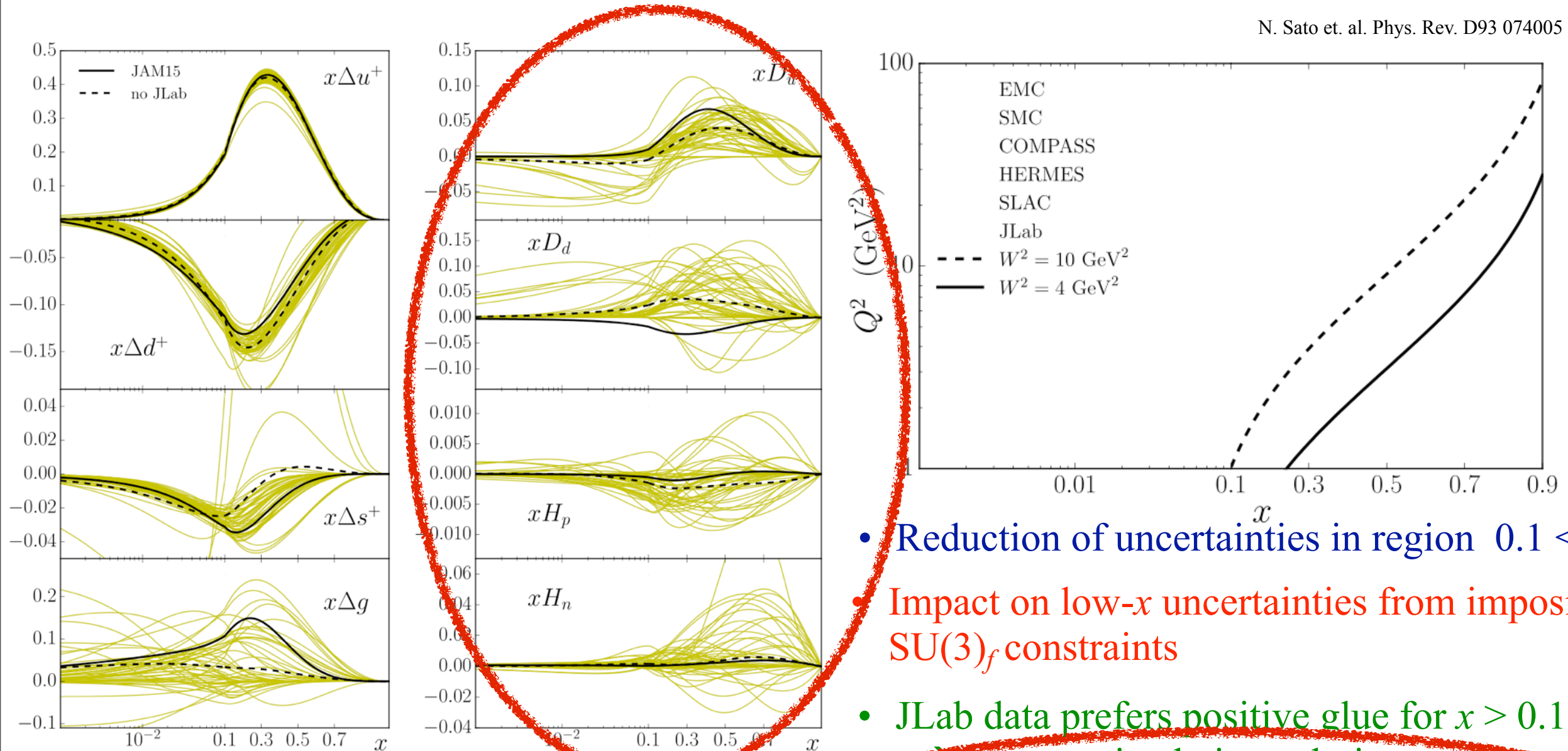
⇒ Elusive higher twists

## JAM15 Analysis – Impact of JLab Data

$$g_1(x, Q^2) = g_1^{\text{LT+TMC}}(\Delta u^+, \Delta d^+, \Delta g, \dots) + g_1^{\text{T3+TMC}}(D_u, D_d) + g_1^{\text{T4}}(H_{p,n})$$

$$g_2(x, Q^2) = g_2^{\text{LT+TMC}}(\Delta u^+, \Delta d^+, \Delta g, \dots) + g_2^{\text{T3+TMC}}(D_u, D_d)$$

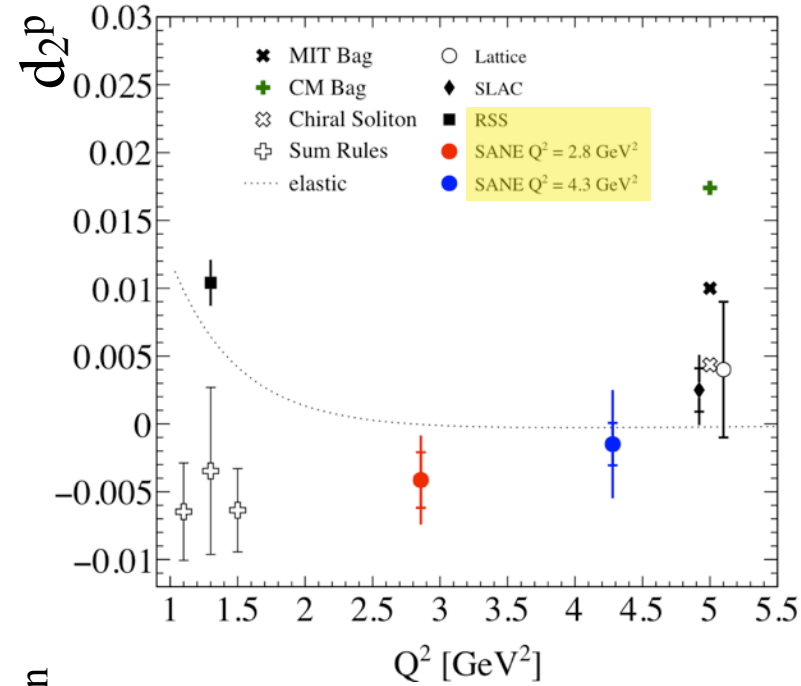
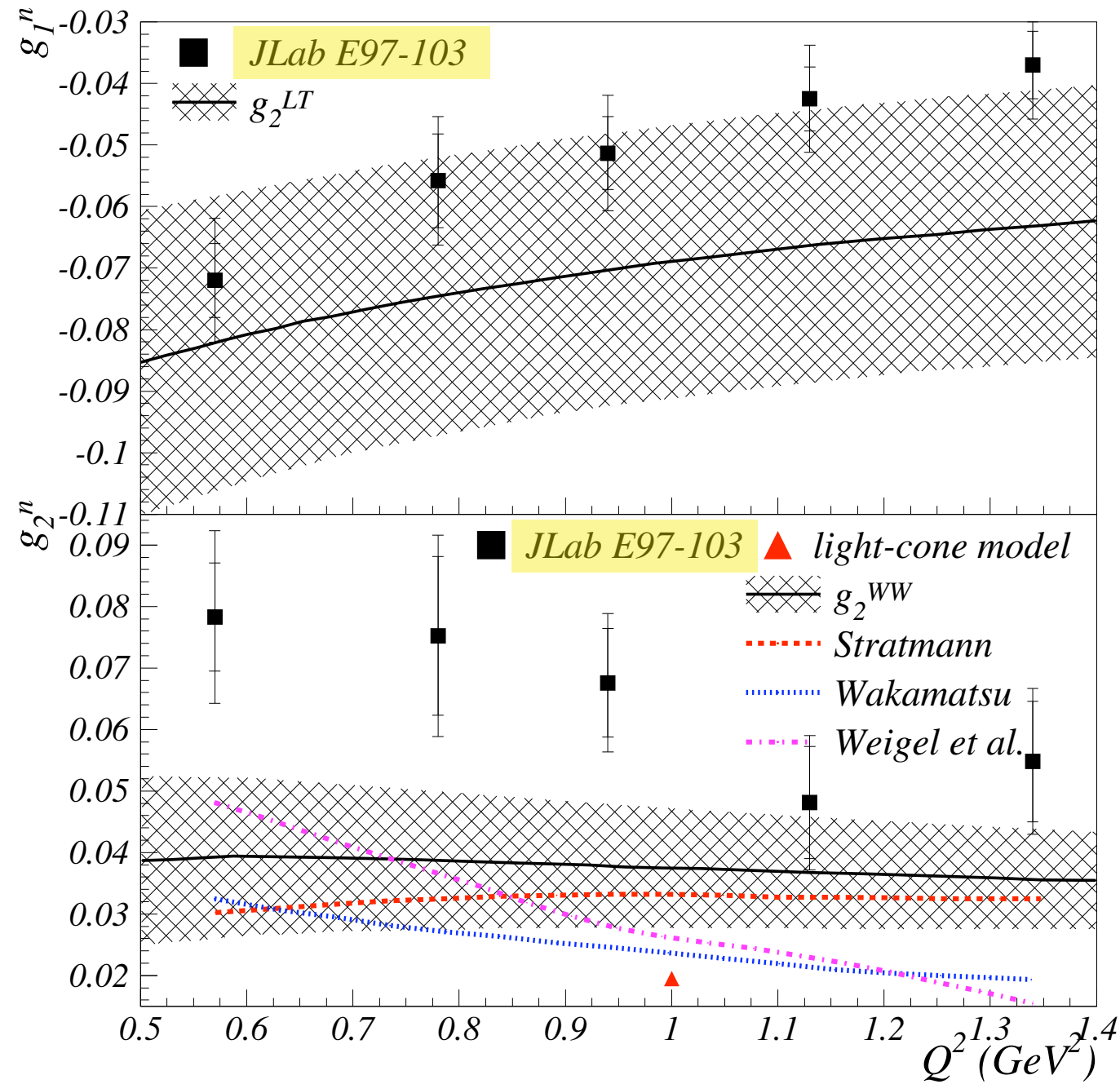
N. Sato et. al. Phys. Rev. D93 074005 (2016)



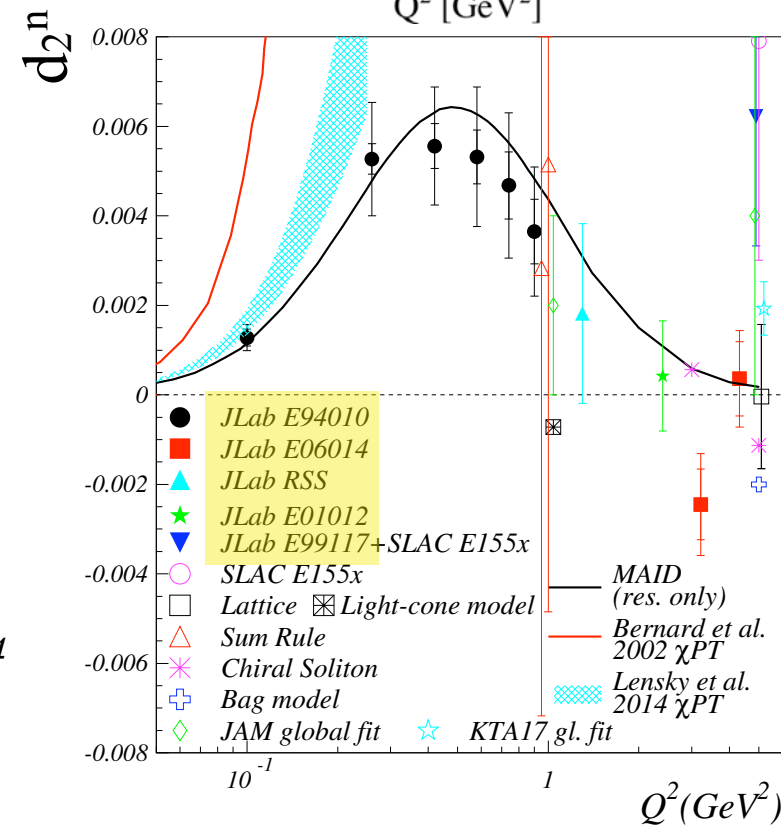
- Reduction of uncertainties in region  $0.1 < x < 0.7$
- Impact on low- $x$  uncertainties from imposing  $SU(3)_f$  constraints
- JLab data prefers positive glue for  $x > 0.1$   
 → constrained via evolution
- Non-zero twist-3 quark distributions ; twist-4 consistent with zero

# "Study transition from hadronic to partonic description of strong force"

Dedicated higher-twist measurements: Hall A E97-103, E01012, E06014, Hall C SANE



SANE results on arXiv last Thursday (arXiv:1805:08835)





# Is the bridge between the hadronic and partonic banks built yet?



**Hadrons  
(low  $Q^2$ )**

**Partons  
(High  $Q^2$ )**

# Is the bridge built?

- Precise mapping of the low and intermediate  $Q^2$  regions.

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- Analytic and Massive perturbation theories, Schwinger-Dyson equations:

Pasechnik, Soffer, Teryaev, Phys.Rev. D 82 076007 (2010)

Natale, Nucl.Phys.Proc.Suppl. 199 (2010) 178

Shirkov, Phys. Part. Nucl. Lett. 10 (2013) 186

Work motivated by  
JLab's Bjorken  
sum measurements



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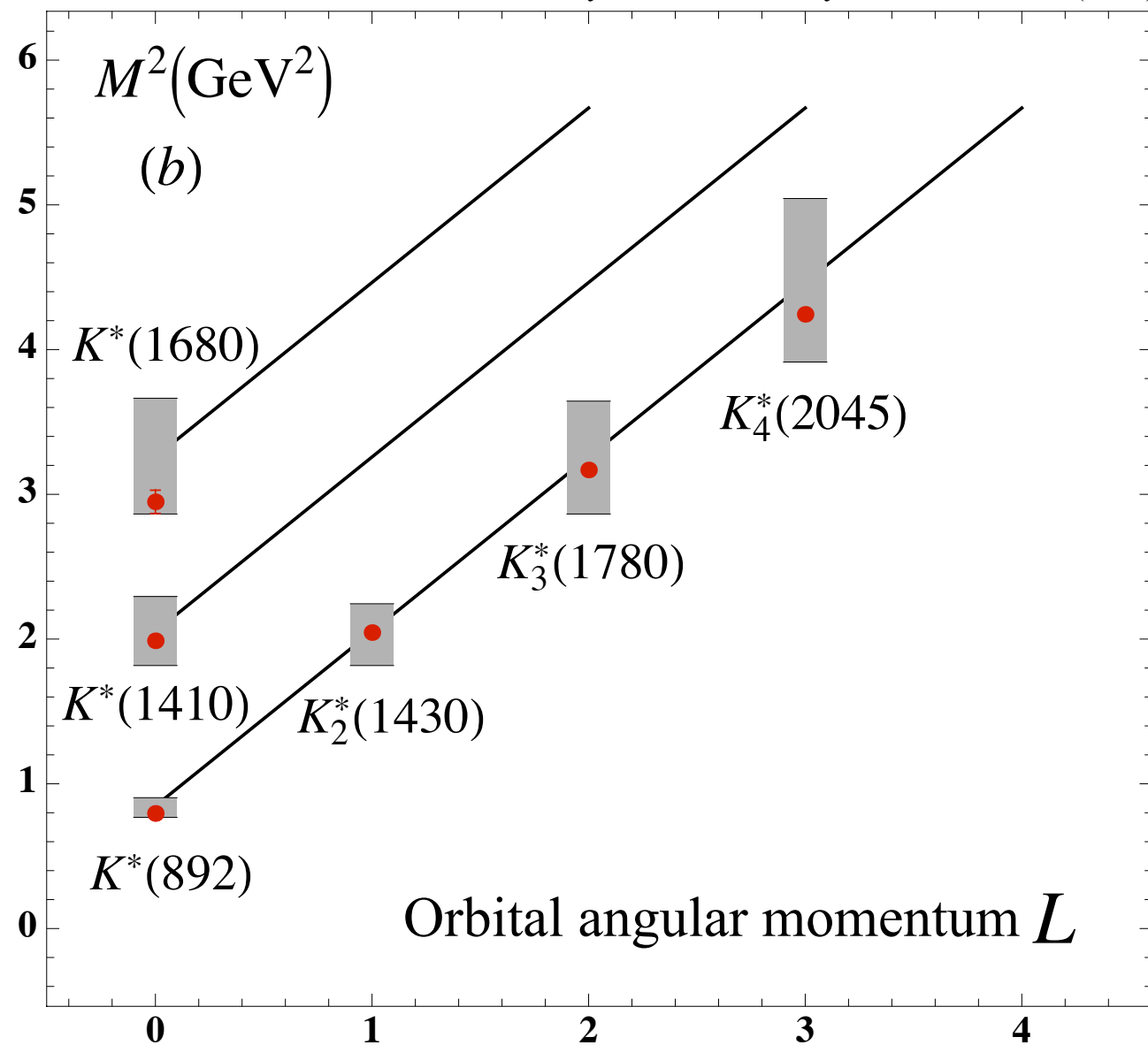
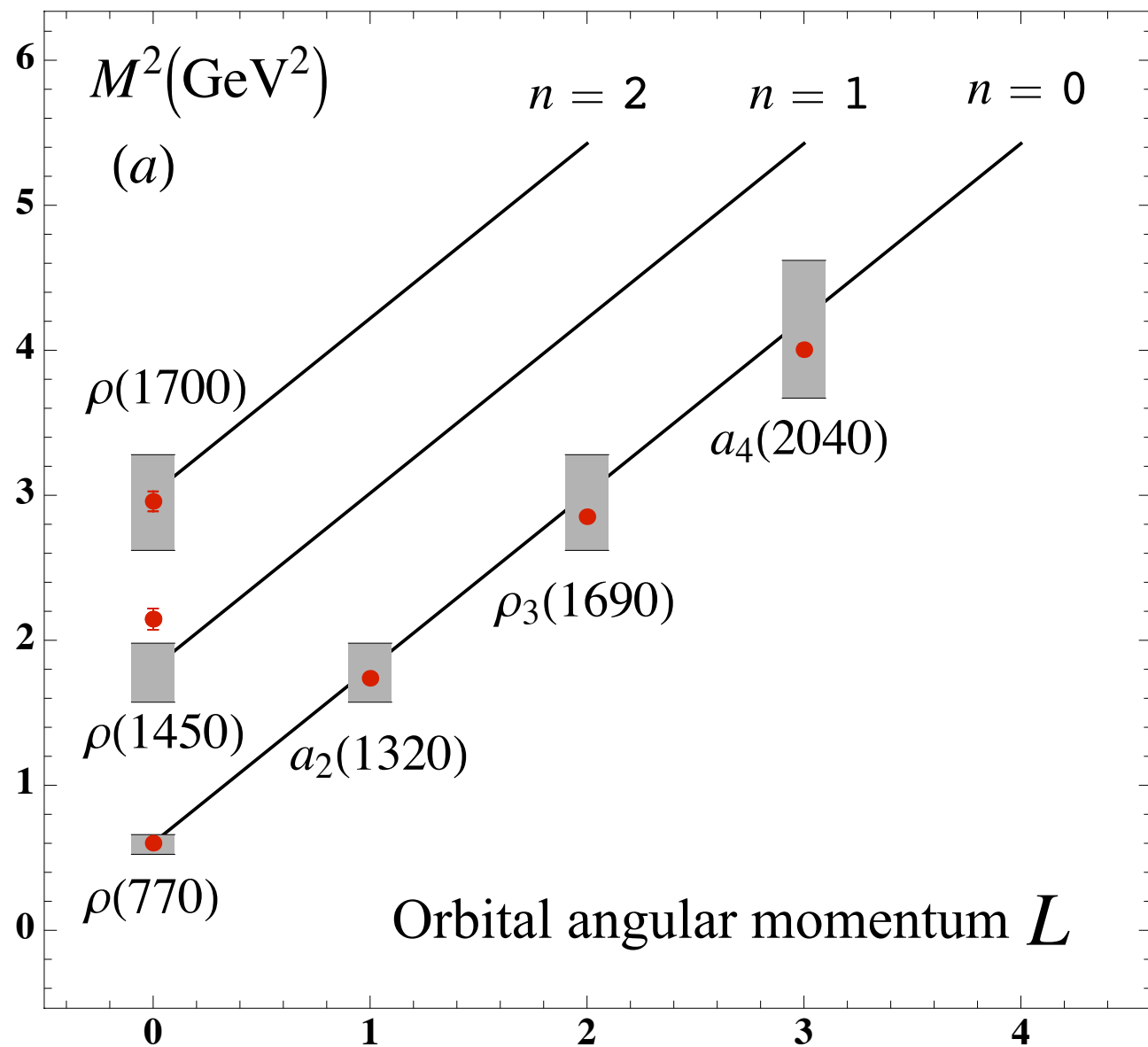
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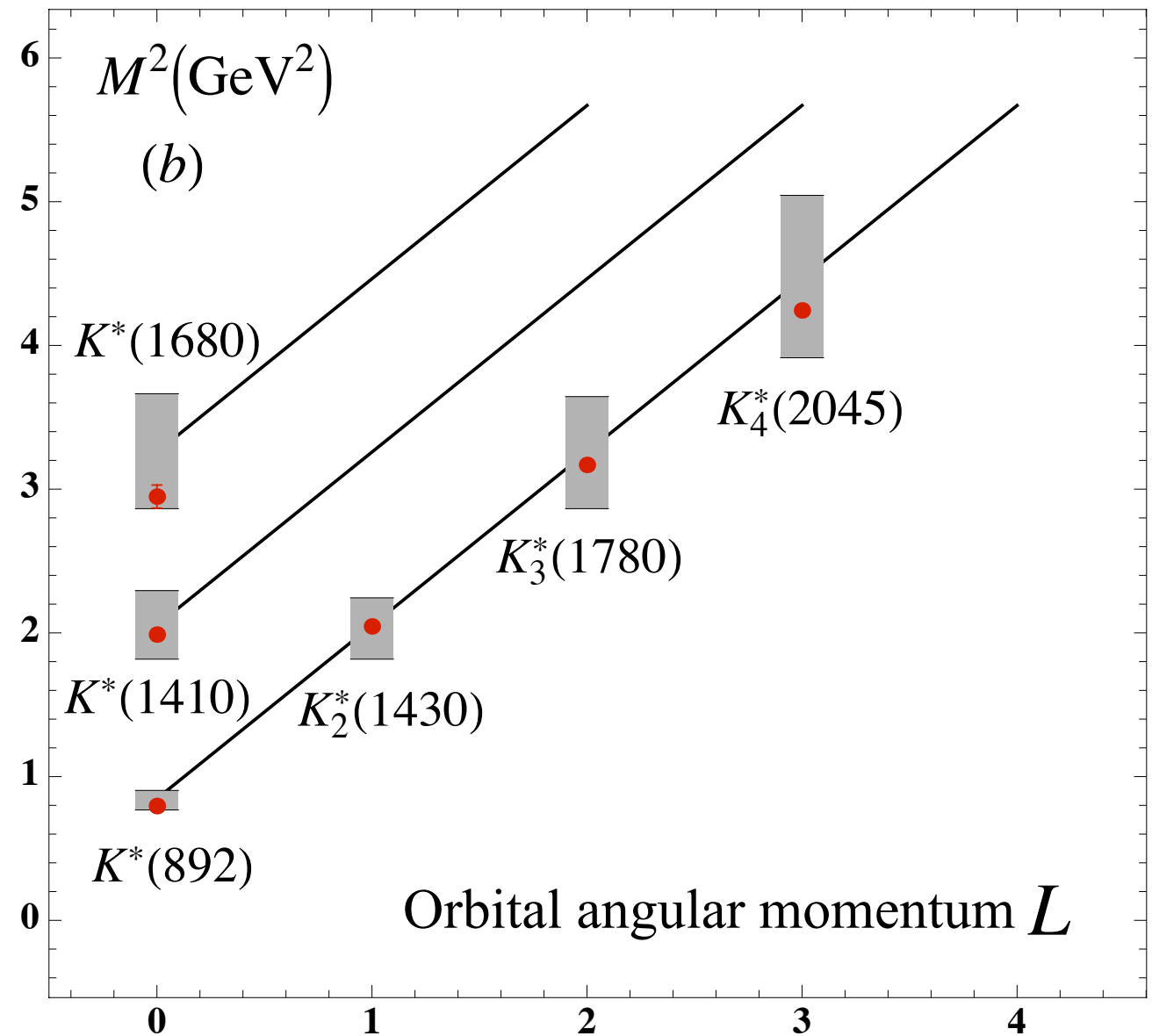
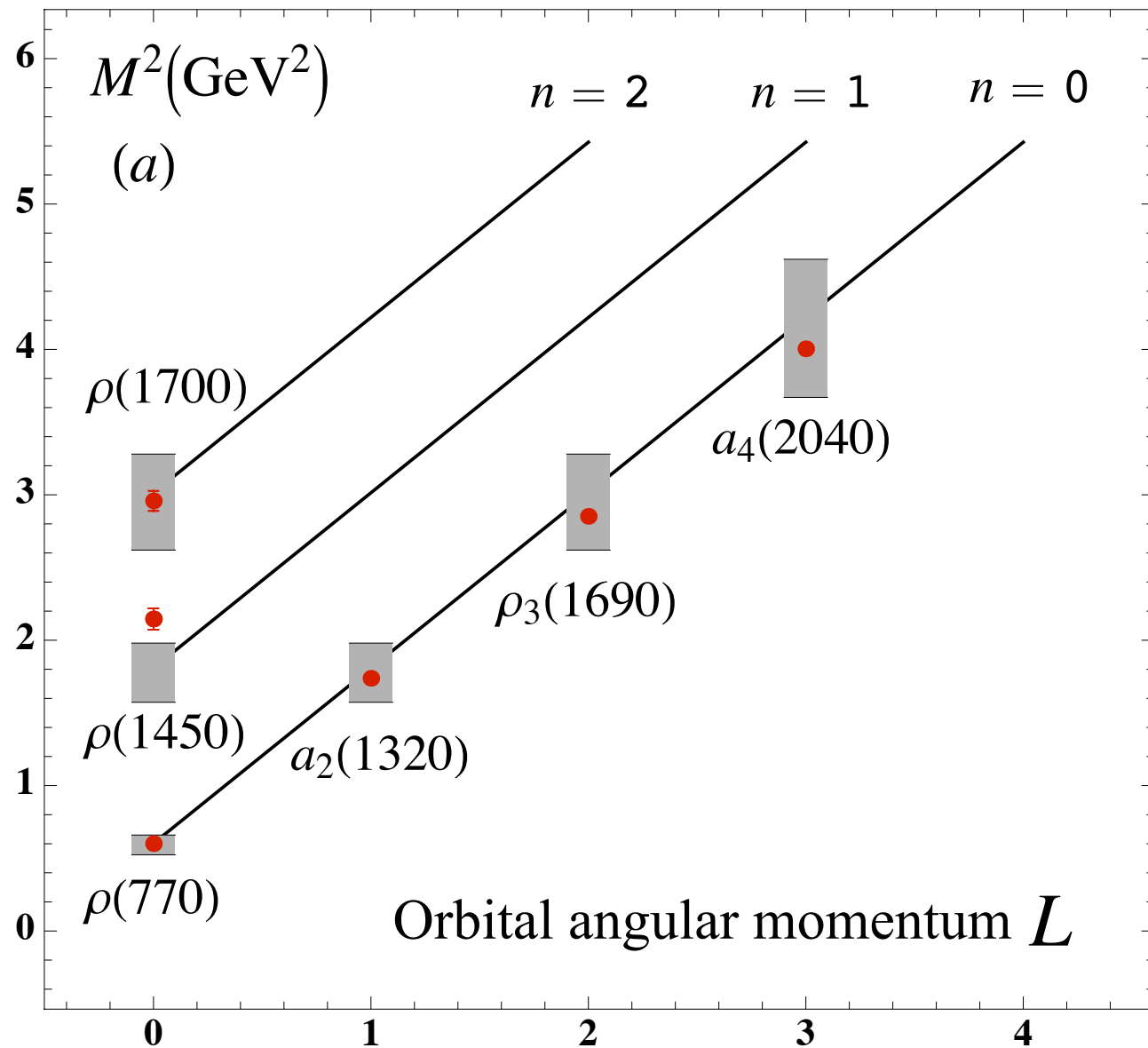
Work motivated by  
JLab's Bjorken  
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- Jlab Bjorken sum data: AdS/QCD calculation of  $\alpha_s(Q^2)$ . Matching it to pQCD prediction allow to analytically determinate hadron spectrum from  $\Lambda_s$



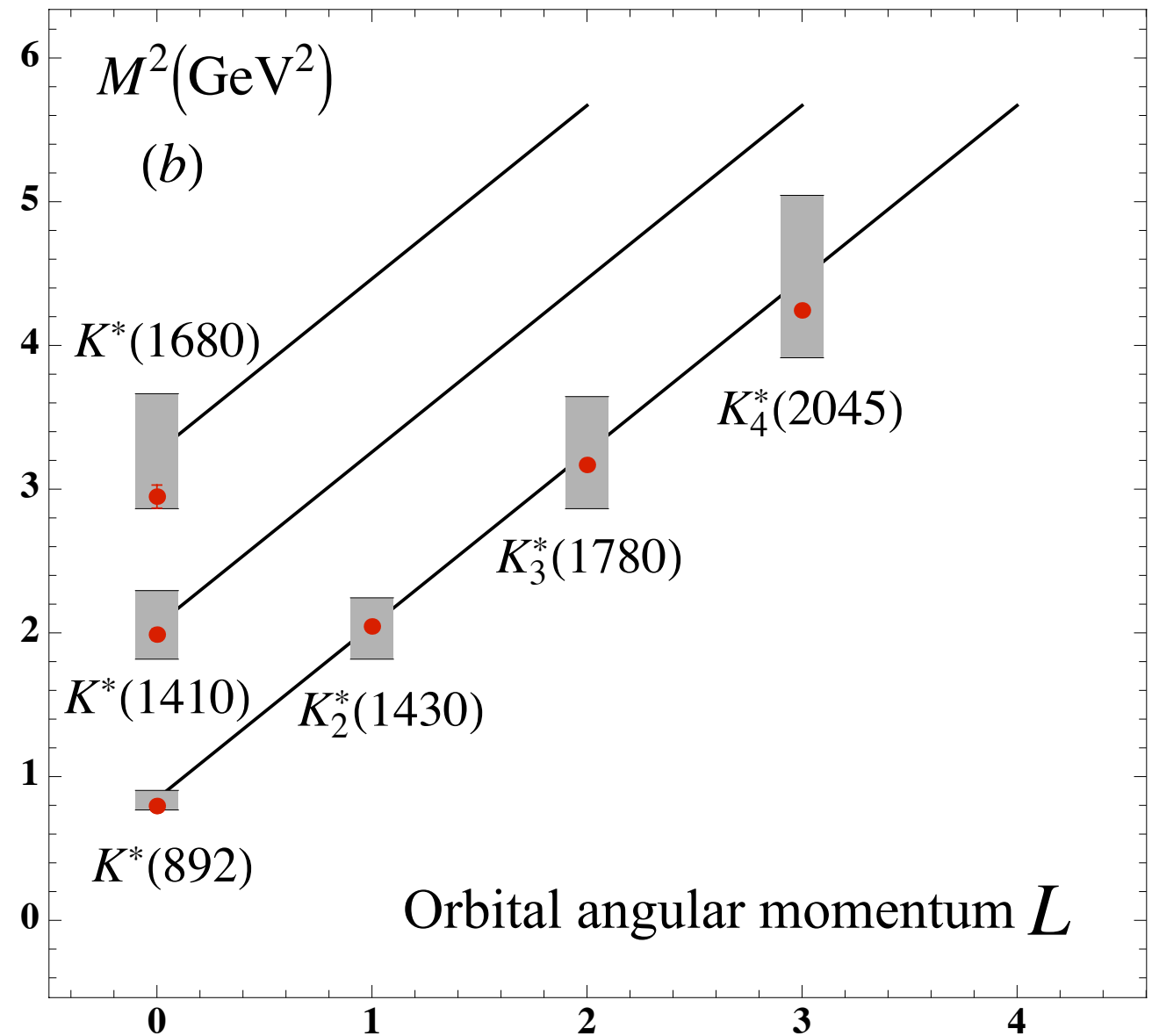
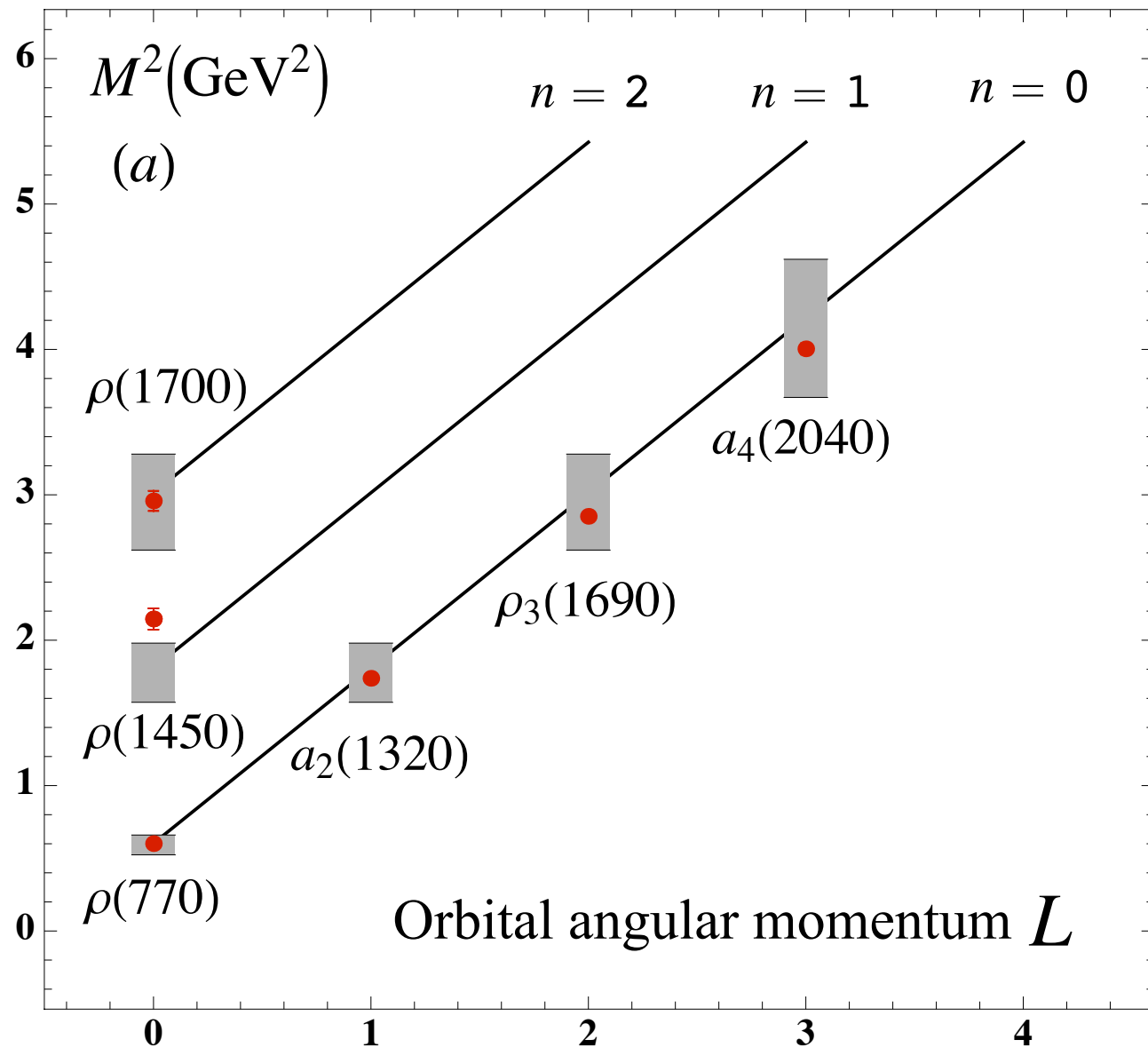





- : AdS/QCD predictions with  $\Lambda_s$  from PDG as (only) input.
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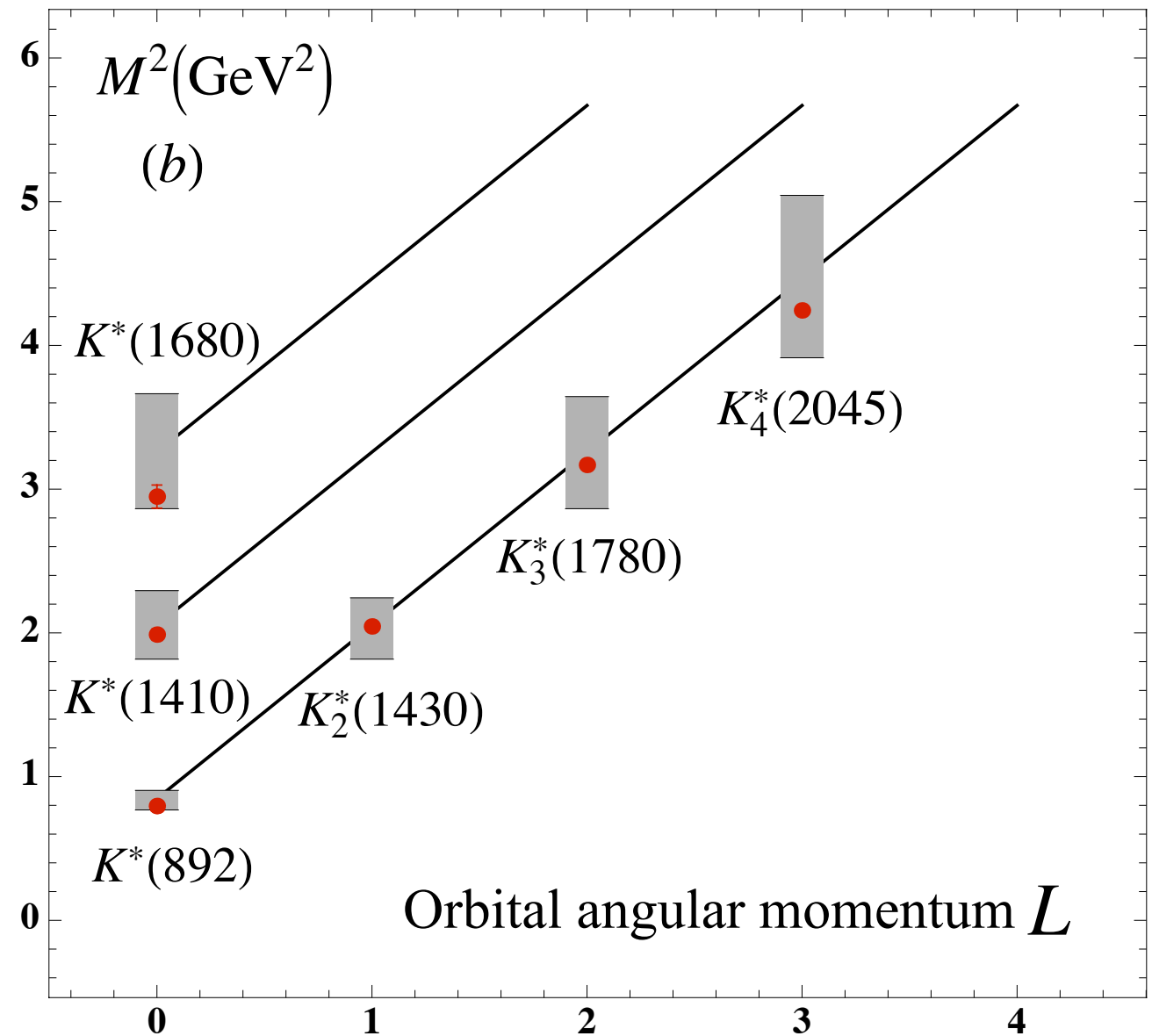
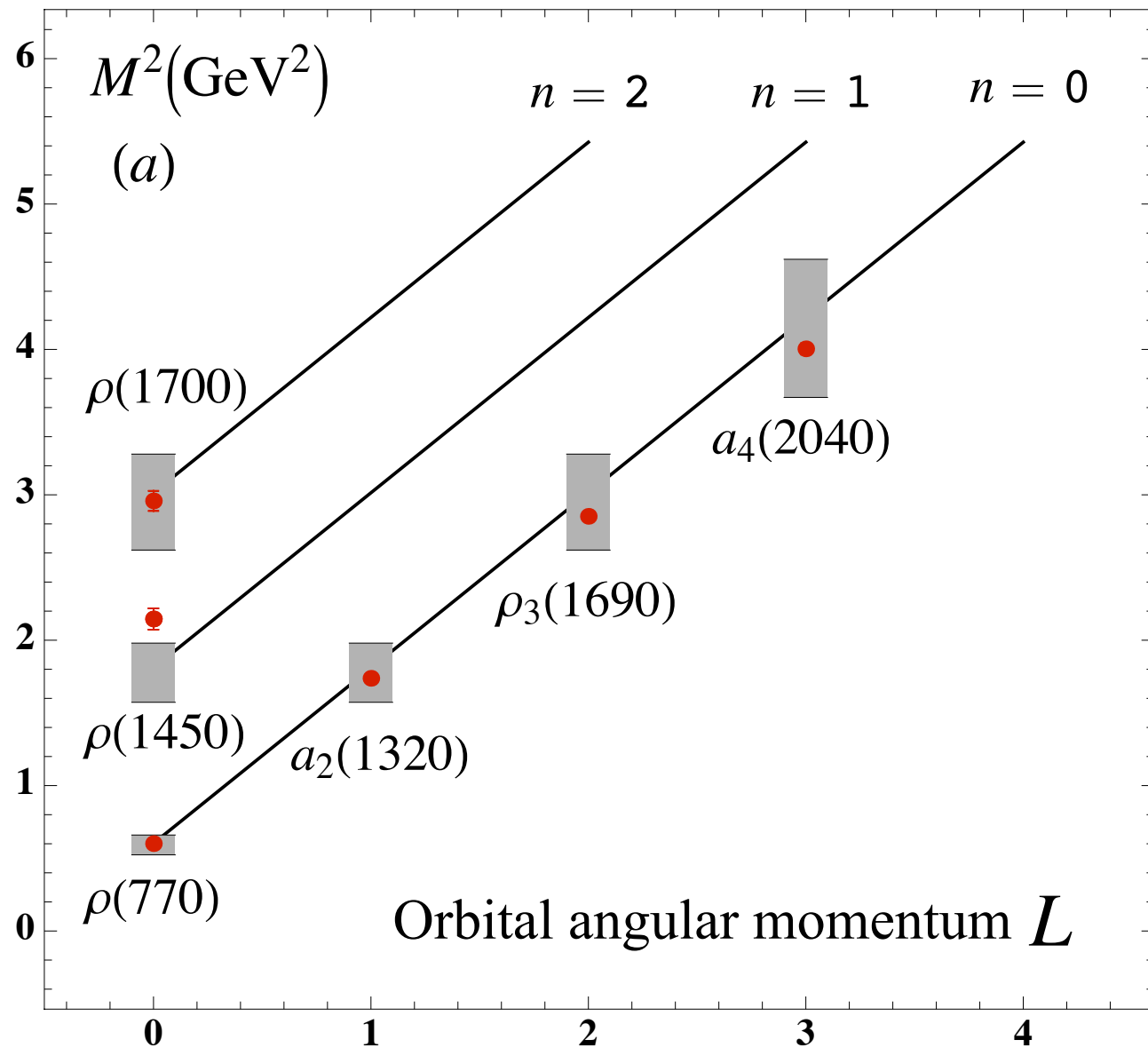
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AdS/QCD: Semi-classical approximation of QCD.)



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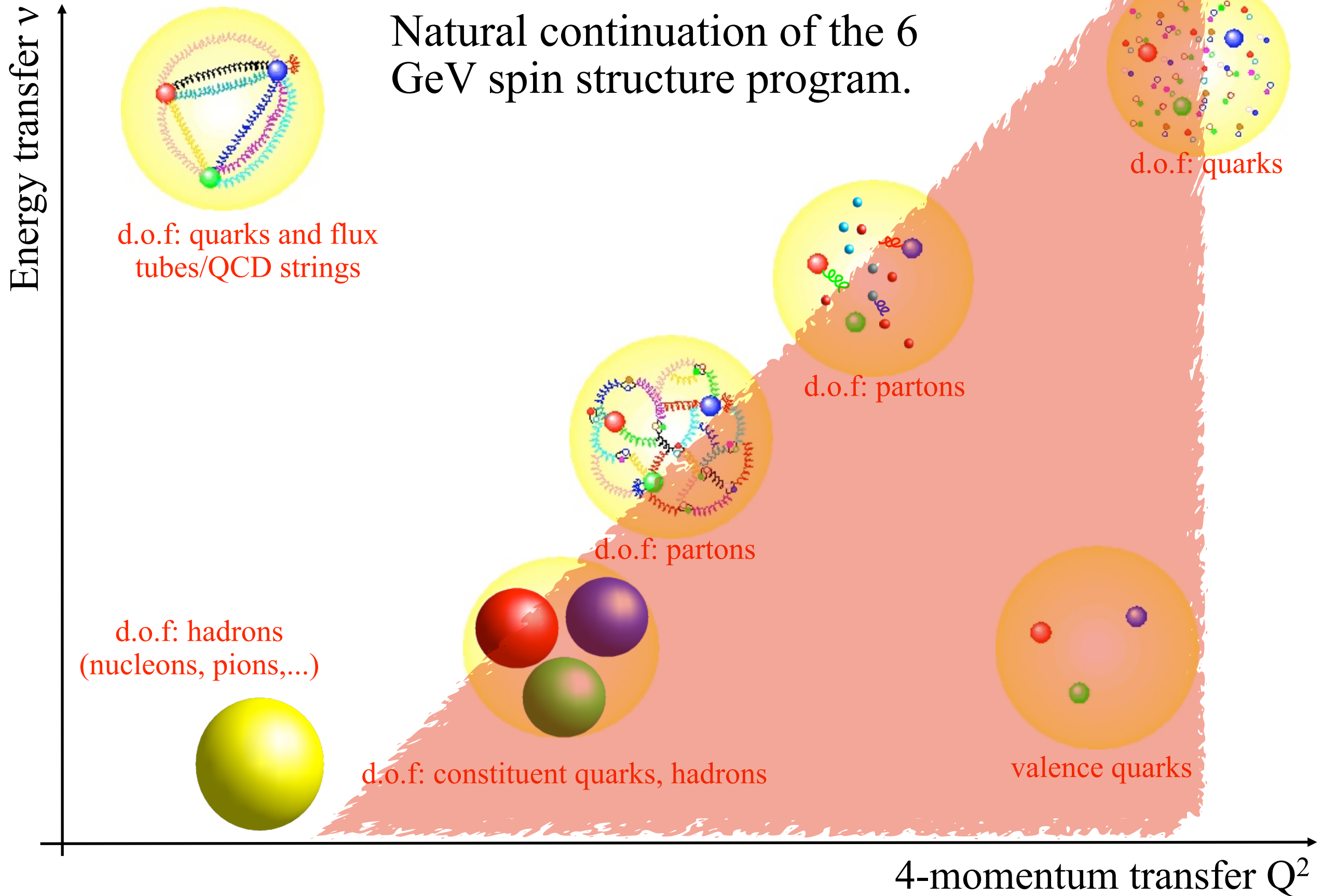
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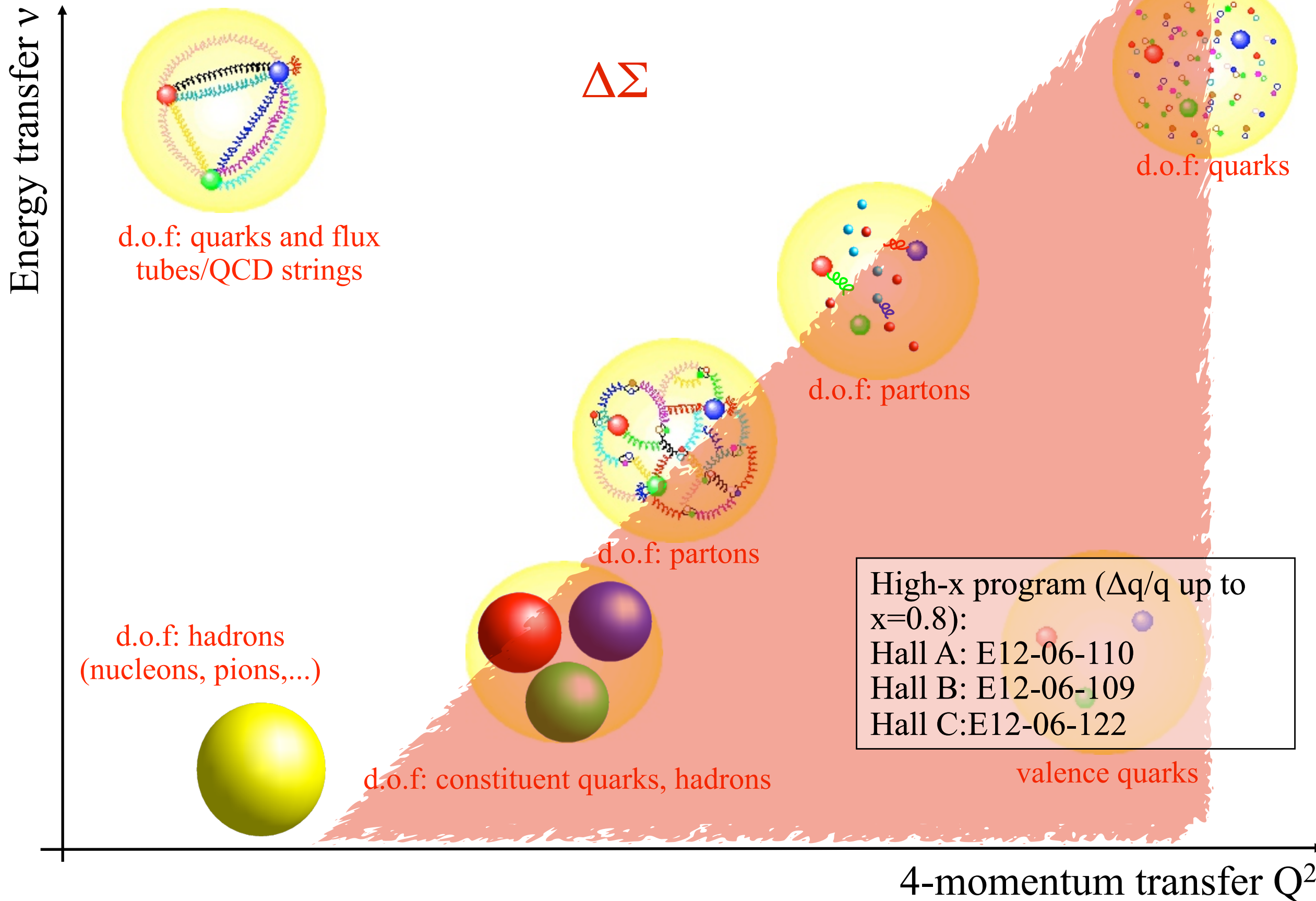


# Short term Future: JLab at 12 GeV

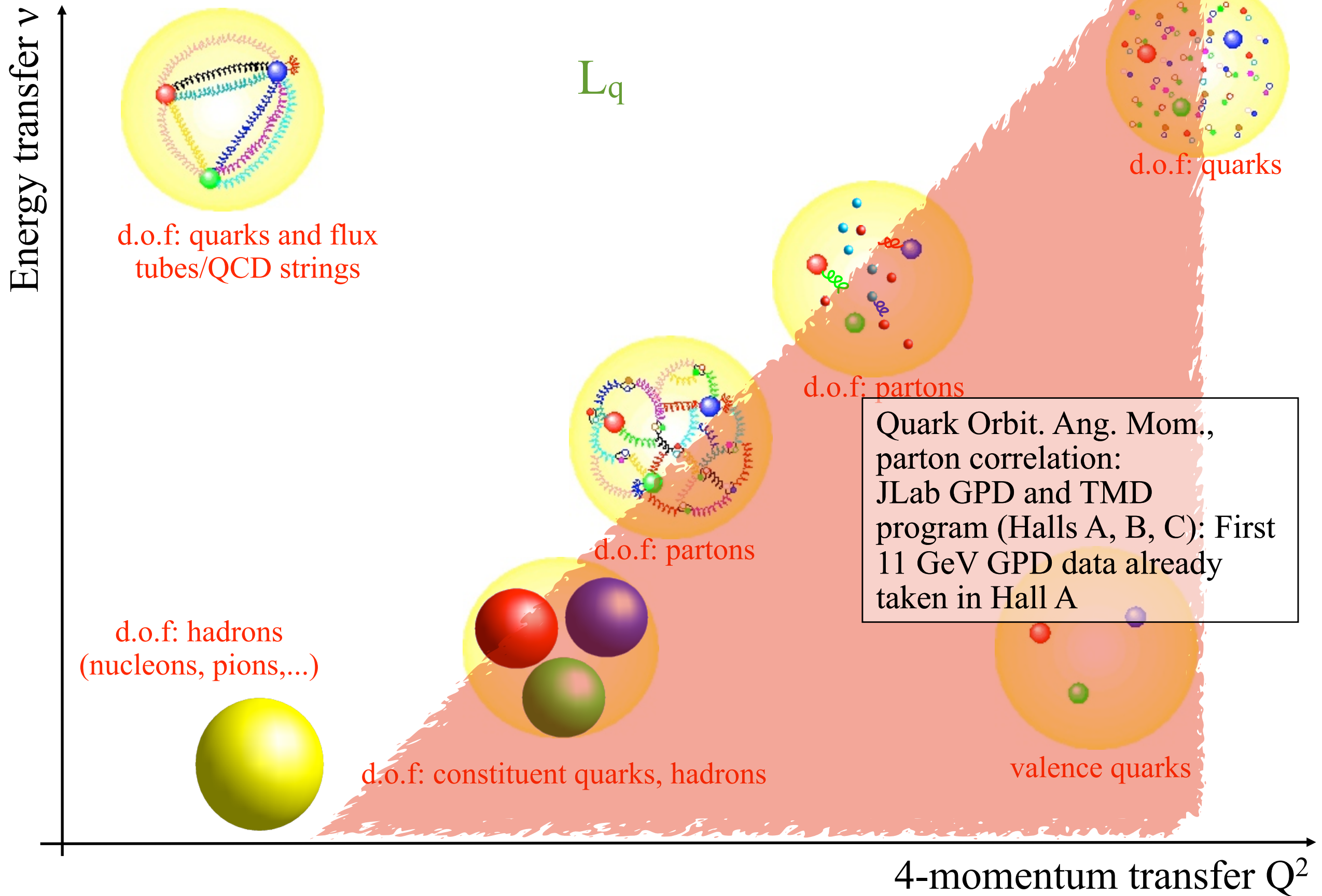
Natural continuation of the 6 GeV spin structure program.



# Short term Future: JLab at 12 GeV

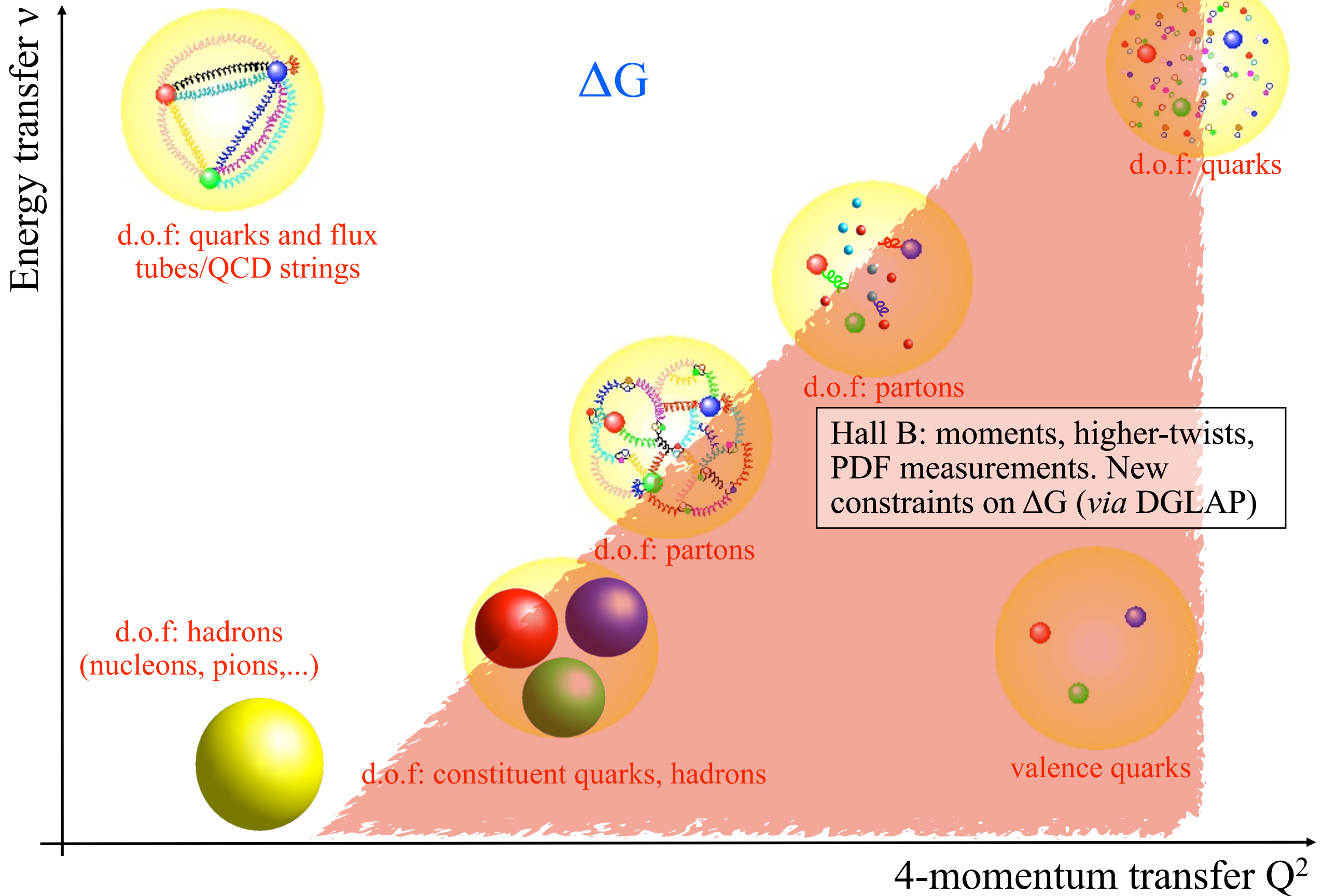


# Short term Future: JLab at 12 GeV

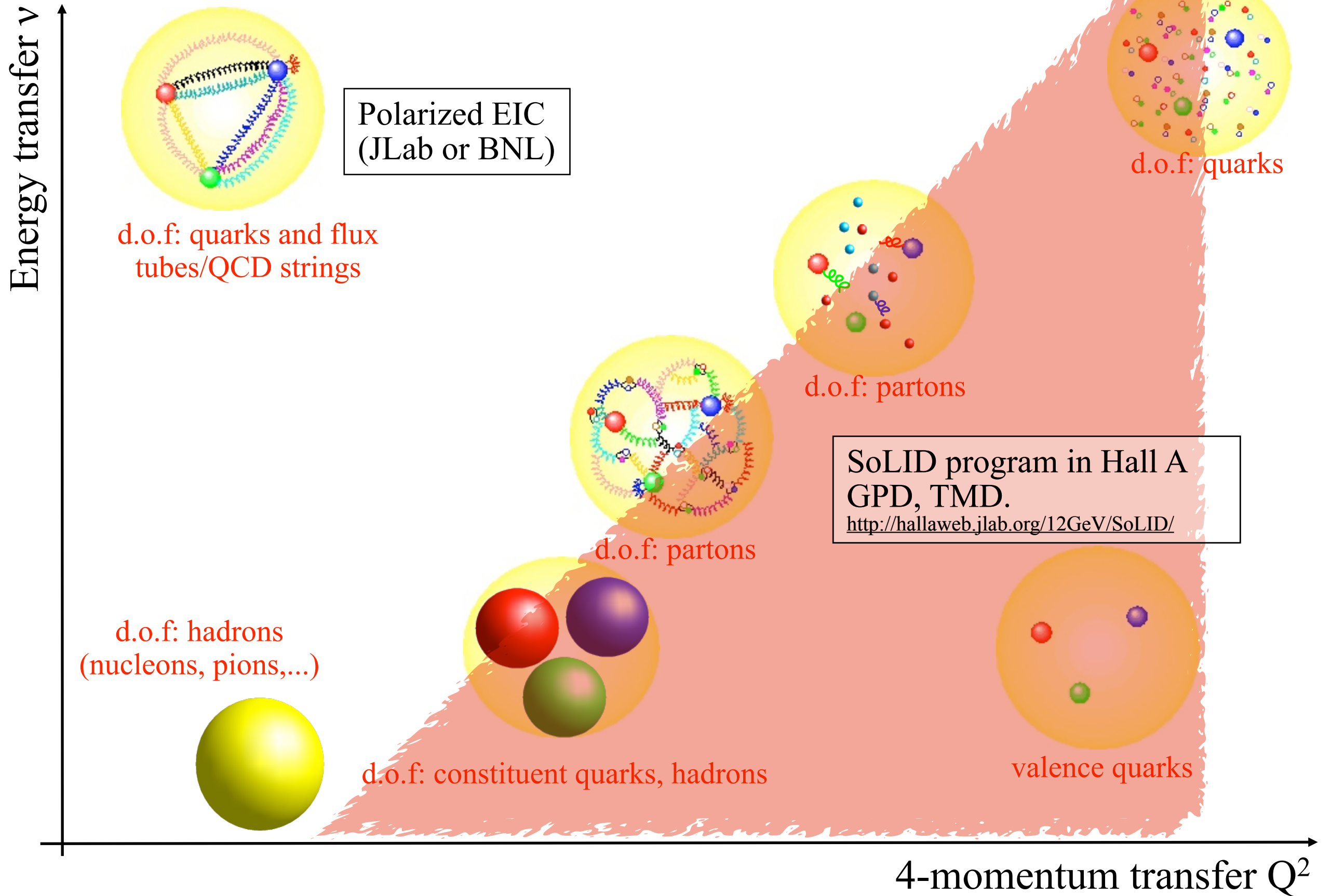




# Short term Future: JLab at 12 GeV



# Longer term Future



Thank You!