

Single-top production in the Standard Model and beyond

Nikolaos Kidonakis

- Higher-order soft-gluon corrections
- t -channel and s -channel production
- tW production
- tZ production via anomalous couplings



College of Science and Mathematics
Department of Physics

CIPANP 2018



Higher-order corrections

QCD corrections are very significant for single-top production

Soft-gluon corrections are important
and they approximate exact results very well

We calculate/resum these soft corrections at NNLL accuracy
for the double-differential cross section

Finite-order expansions

Approximate NNLO (aNNLO) and $N^3\text{LO}$ ($aN^3\text{LO}$) predictions
for cross sections and differential distributions

Soft-gluon corrections

partonic processes

$$f_1(p_1) + f_2(p_2) \rightarrow t(p_t) + X$$

define

$$s = (p_1 + p_2)^2, \quad t = (p_1 - p_t)^2, \quad u = (p_2 - p_t)^2$$

and $s_4 = s + t + u - \sum m^2$

At partonic threshold $s_4 \rightarrow 0$

$$\text{Soft corrections} \left[\frac{\ln^k(s_4/m_t^2)}{s_4} \right]_+$$

For the order α_s^n corrections $k \leq 2n - 1$

Resum these soft corrections for the double-differential cross section

At NNLL accuracy we need two-loop soft anomalous dimensions

Soft-gluon Resummation

moments of the partonic cross section with moment variable N :

$$\hat{\sigma}(N) = \int (ds_4/s) e^{-Ns_4/s} \hat{\sigma}(s_4)$$

factorized expression for the cross section in $4 - \epsilon$ dimensions

$$\begin{aligned} \sigma^{f_1 f_2 \rightarrow tX}(N, \epsilon) &= H_{IL}^{f_1 f_2 \rightarrow tX}(\alpha_s(\mu_R)) S_{LI}^{f_1 f_2 \rightarrow tX}\left(\frac{m_t}{N\mu_F}, \alpha_s(\mu_R)\right) \\ &\quad \times \prod J_{\text{in}}(N, \mu_F, \epsilon) \prod J_{\text{out}}(N, \mu_F, \epsilon) \end{aligned}$$

$H_{IL}^{f_1 f_2 \rightarrow tX}$ is hard function and $S_{LI}^{f_1 f_2 \rightarrow tX}$ is soft function

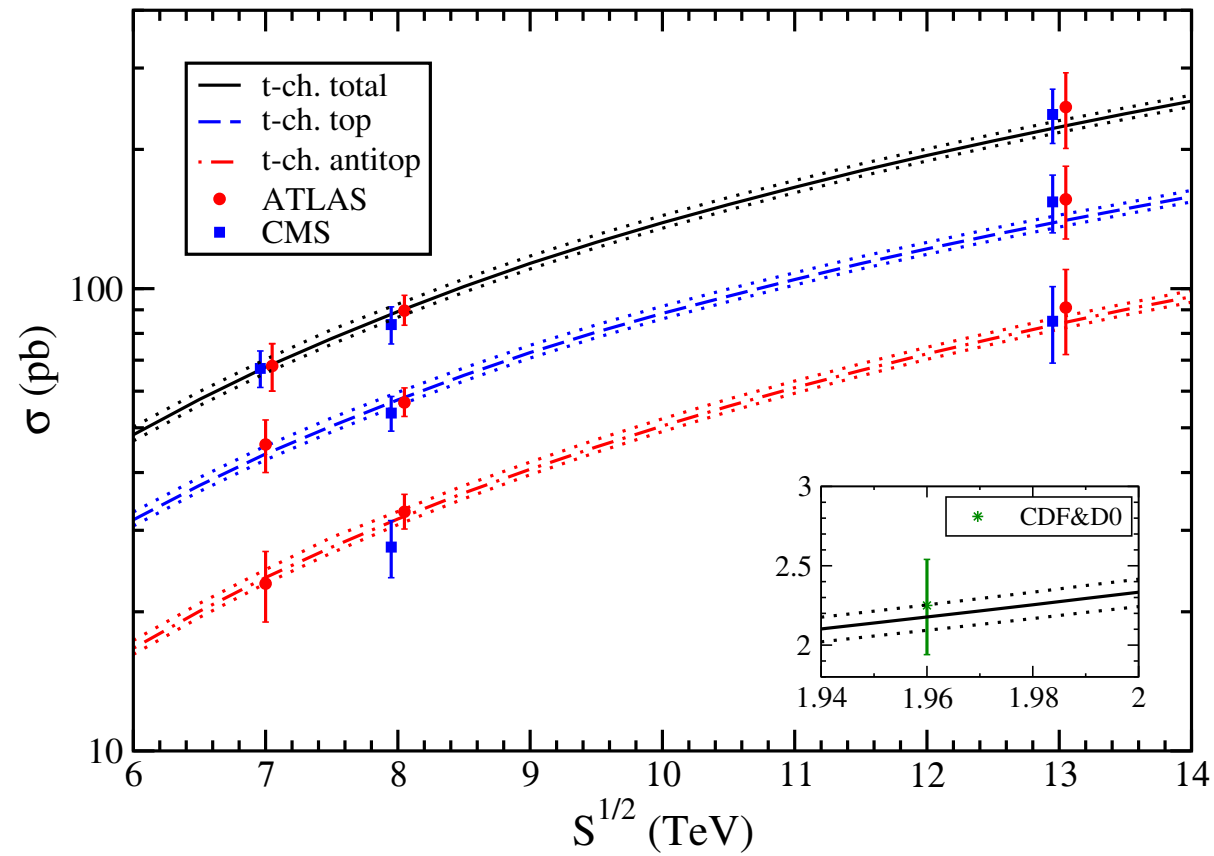
S_{LI} satisfies the renormalization group equation

$$\left(\mu \frac{\partial}{\partial \mu} + \beta(g_s) \frac{\partial}{\partial g_s}\right) S_{LI} = -(\Gamma_S^\dagger)_{LK} S_{KI} - S_{LK} (\Gamma_S)_{KI}$$

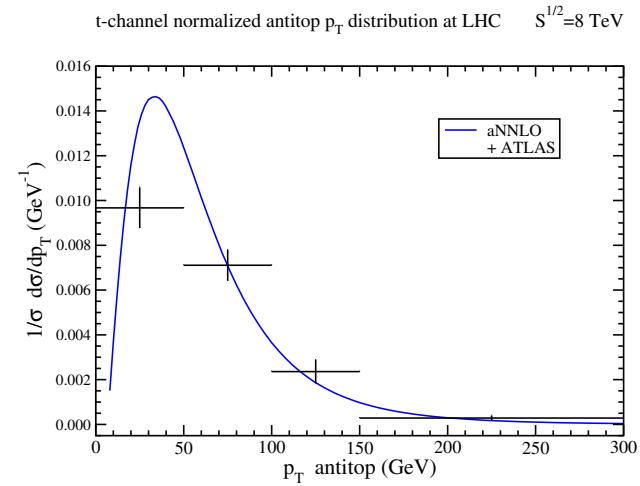
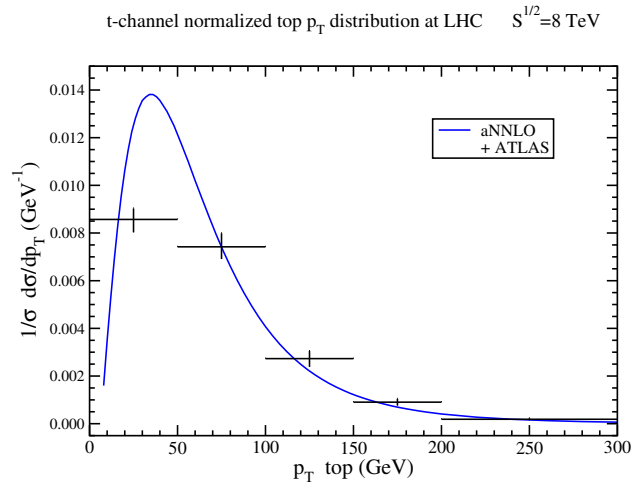
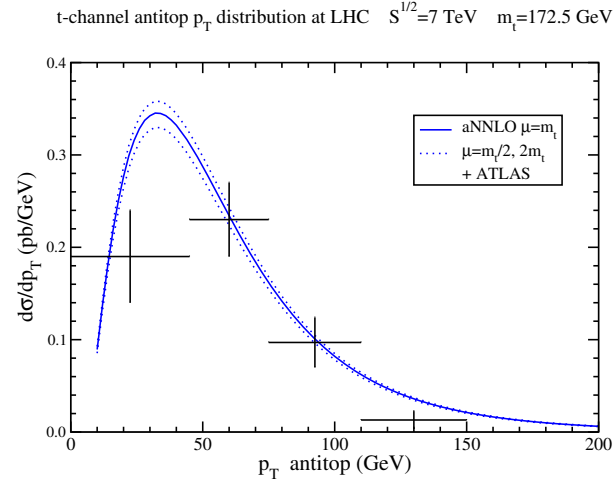
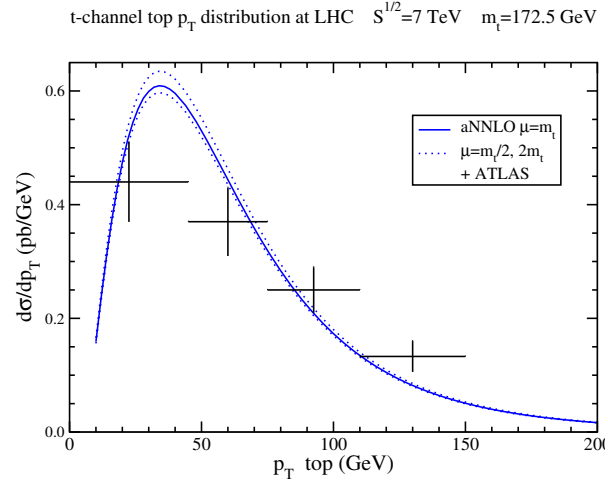
Soft anomalous dimension Γ_S controls the evolution of the soft function which gives the exponentiation of logarithms of N

t-channel production at aNNLO

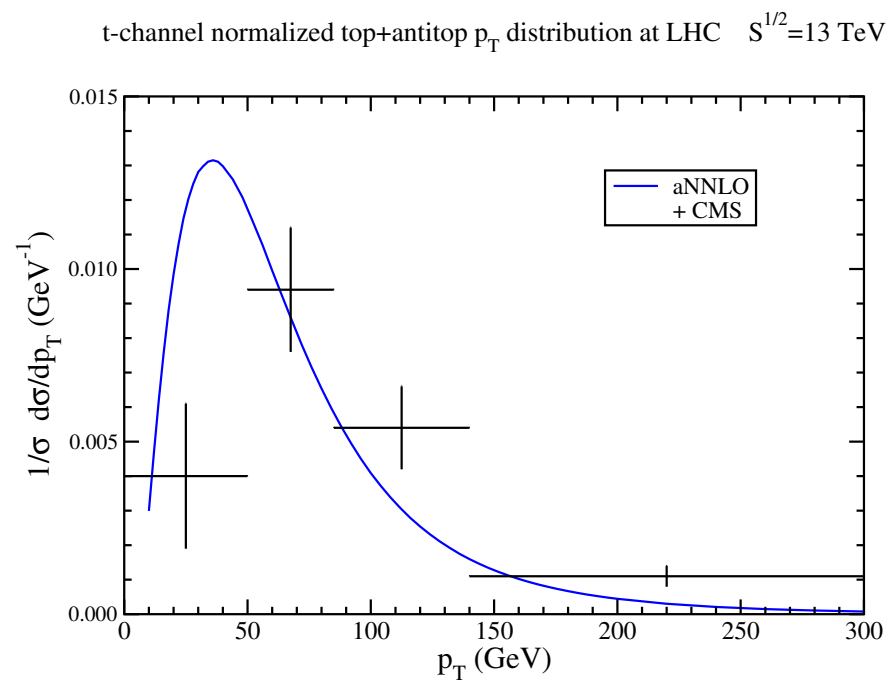
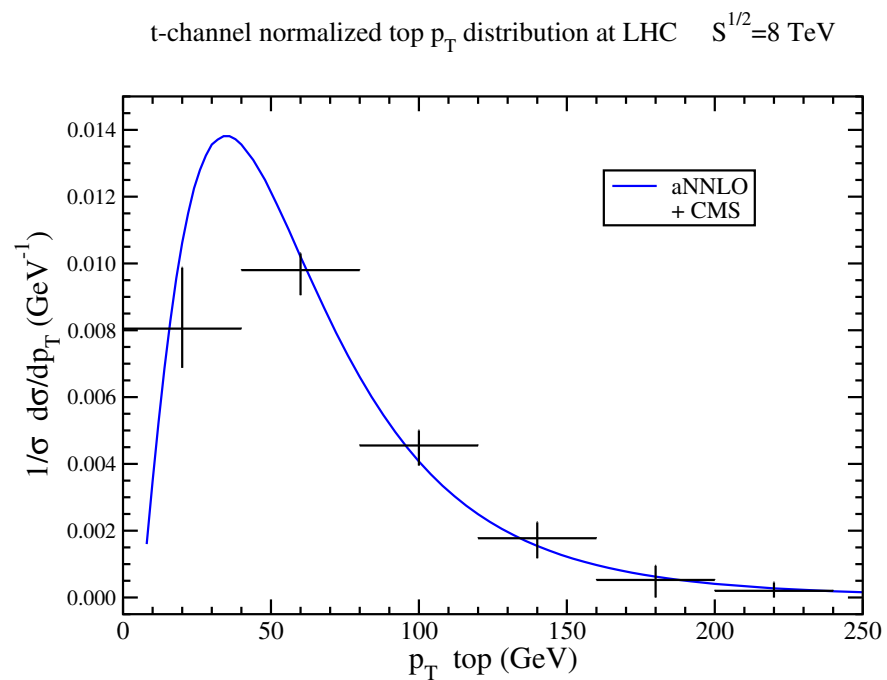
Single-top *t*-channel aNNLO cross sections $m_t=172.5$ GeV



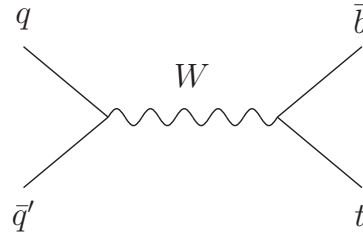
Top p_T distributions in t -channel production at the LHC



Top p_T distributions in t -channel production at the LHC



s-channel production



At one loop

$$\Gamma_{S11}^{s(1)} = C_F \left[\ln \left(\frac{s - m_t^2}{m_t \sqrt{s}} \right) - \frac{1}{2} \right] \quad \Gamma_{S12}^{s(1)} = \frac{C_F}{2N} \ln \left(\frac{u(u - m_t^2)}{t(t - m_t^2)} \right) \quad \Gamma_{S21}^{s(1)} = \ln \left(\frac{u(u - m_t^2)}{t(t - m_t^2)} \right)$$

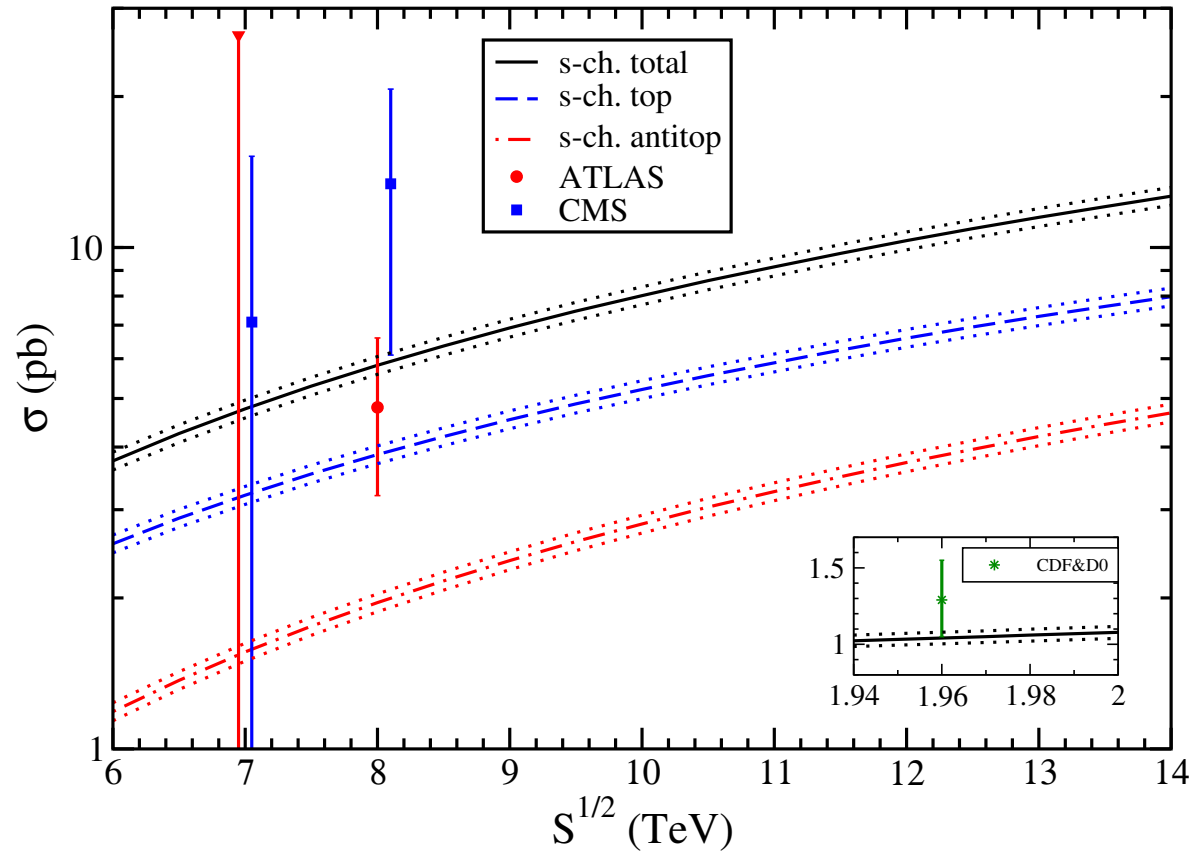
$$\Gamma_{S22}^{s(1)} = C_F \ln \left(\frac{s - m_t^2}{m_t \sqrt{s}} \right) - \frac{1}{N} \ln \left(\frac{u(u - m_t^2)}{t(t - m_t^2)} \right) + \frac{N}{2} \ln \left(\frac{u(u - m_t^2)}{s(s - m_t^2)} \right) - \frac{C_F}{2}$$

At two loops

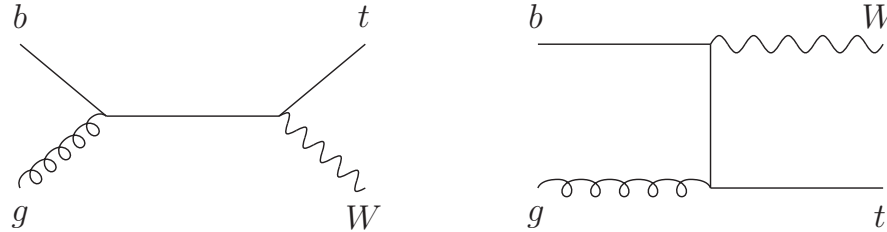
$$\Gamma_{S11}^{s(2)} = \left[C_A \left(\frac{67}{36} - \frac{\zeta_2}{2} \right) - \frac{5}{18} n_f \right] \Gamma_{S11}^{s(1)} + C_F C_A \frac{(1 - \zeta_3)}{4}$$

s -channel production at aNNLO

Single-top s -channel aNNLO cross sections $m_t=172.5$ GeV



Associated tW production



At one loop

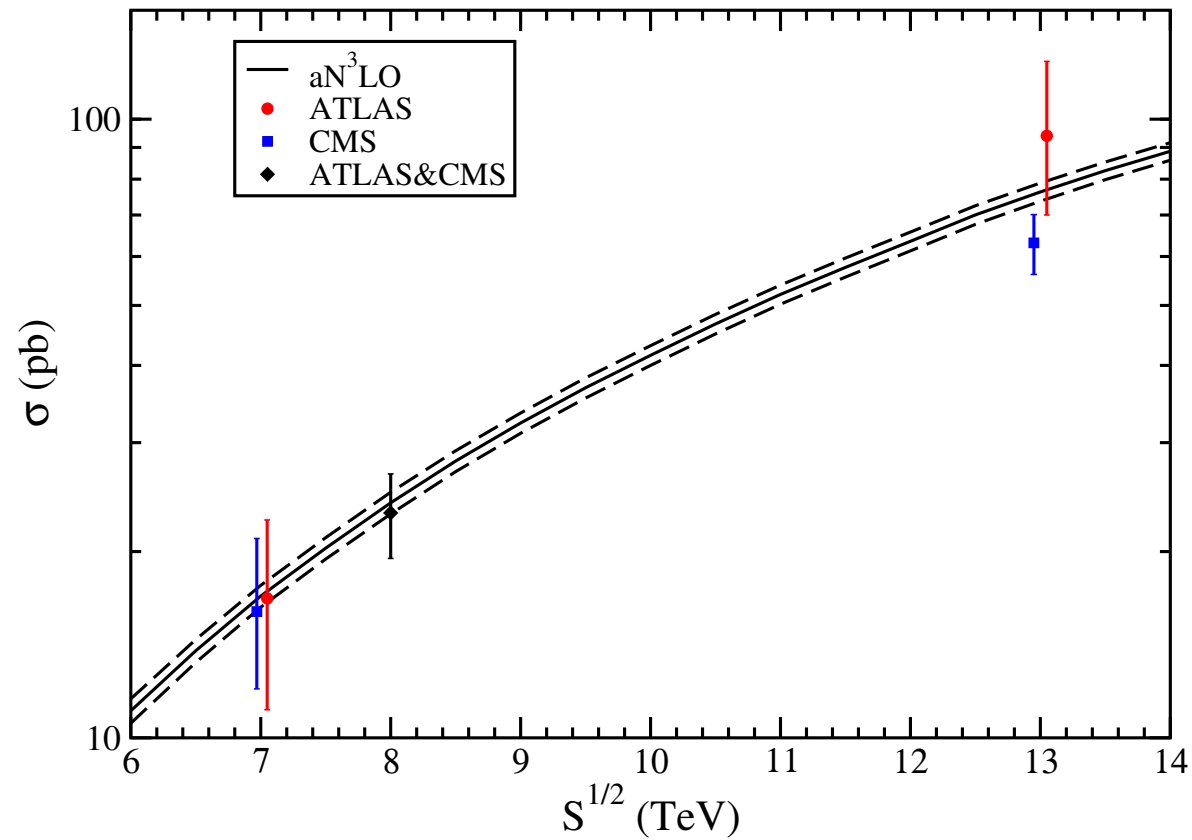
$$\Gamma_S^{tW^- (1)} = C_F \left[\ln \left(\frac{m_t^2 - t}{m_t \sqrt{s}} \right) - \frac{1}{2} \right] + \frac{C_A}{2} \ln \left(\frac{m_t^2 - u}{m_t^2 - t} \right)$$

At two loops

$$\Gamma_S^{tW^- (2)} = \left[C_A \left(\frac{67}{36} - \frac{\zeta_2}{2} \right) - \frac{5}{18} n_f \right] \Gamma_S^{tW^- (1)} + C_F C_A \frac{(1 - \zeta_3)}{4}$$

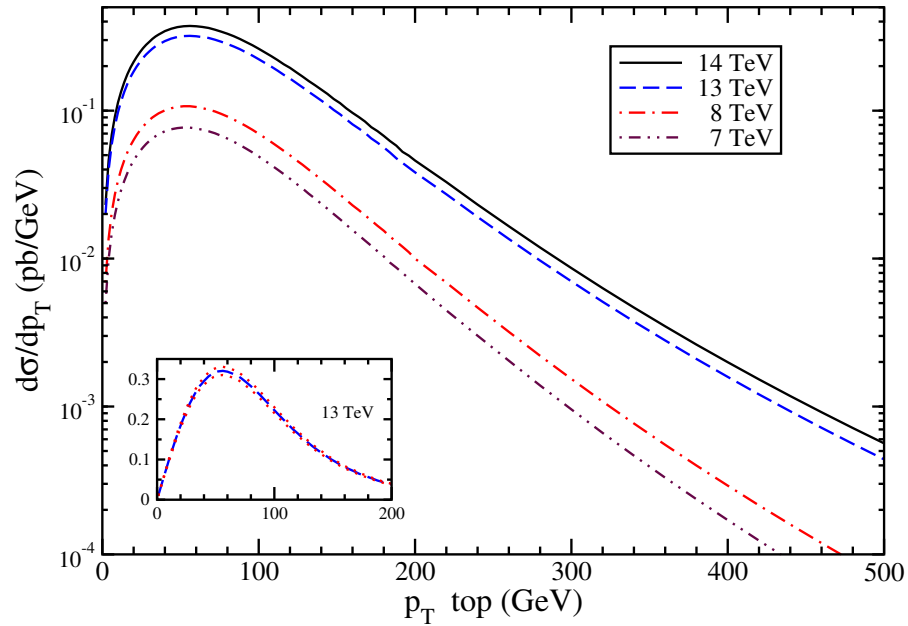
tW production at aN³LO

$tW^- + \bar{t}W^+$ aN³LO cross section $m_t=172.5$ GeV

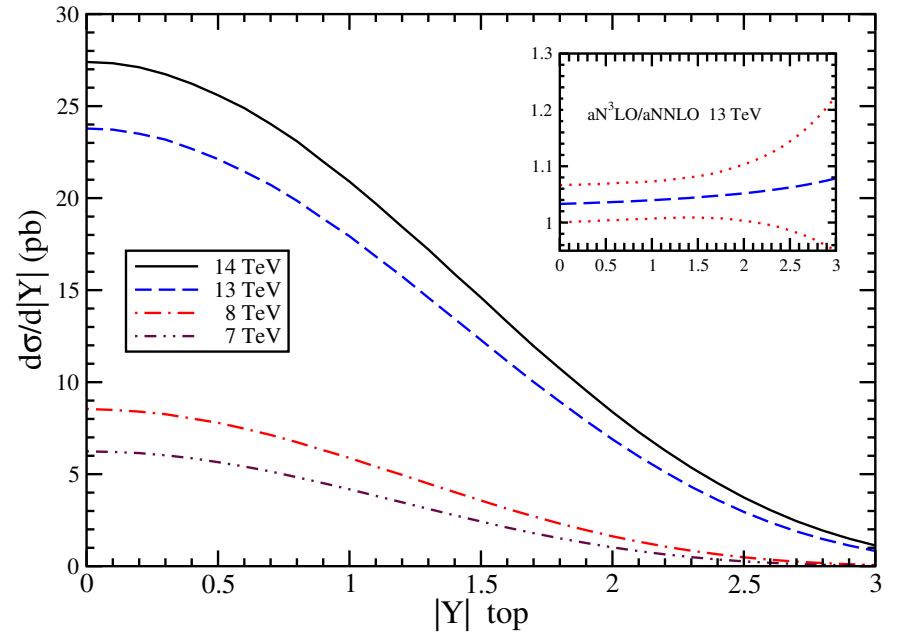


Top quark p_T and rapidity distributions in tW production

Top p_T distribution in tW production at LHC aN³LO $m_t=173.3$ GeV

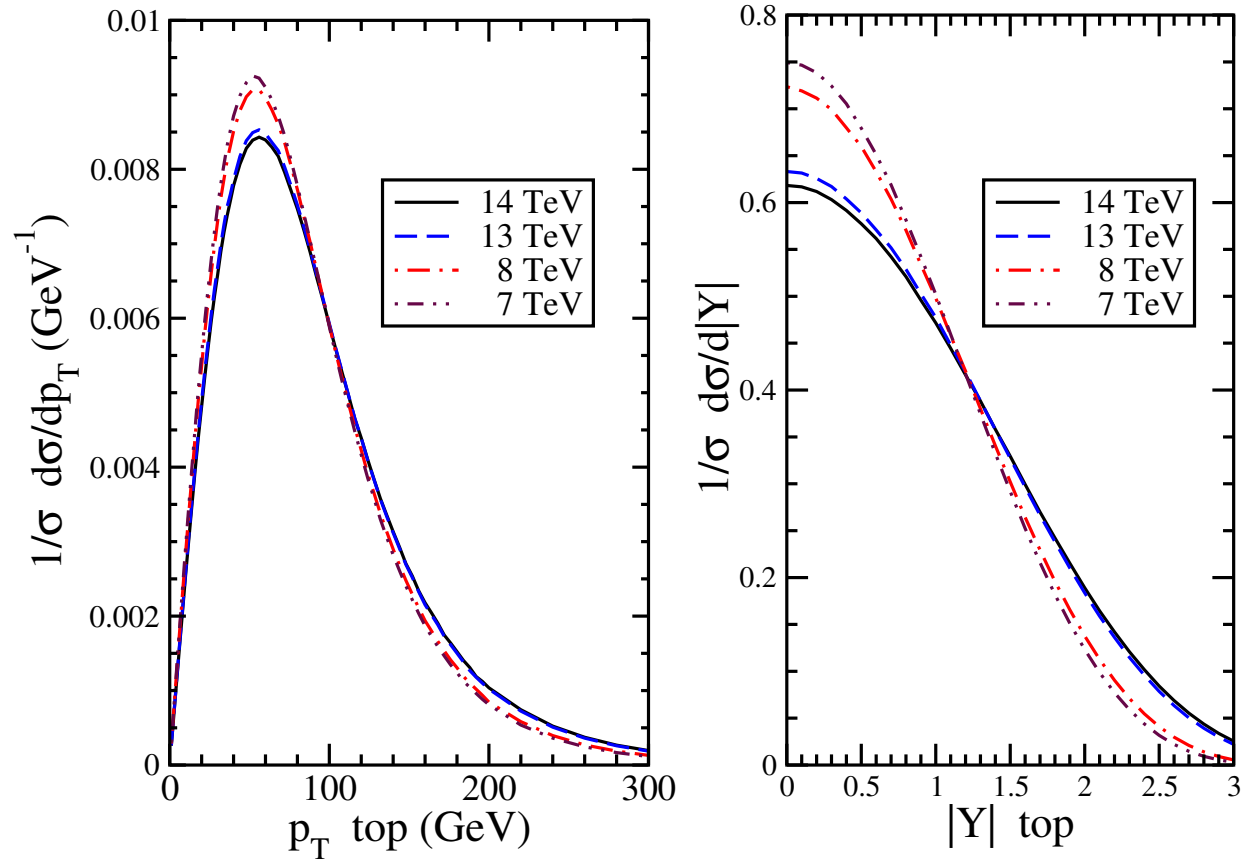


Top rapidity distribution in tW production at LHC aN³LO $m_t=173.3$ GeV

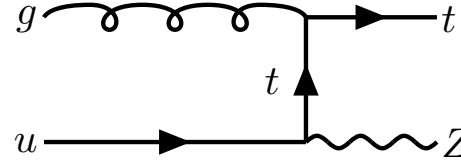
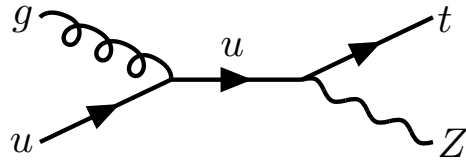


Normalized top quark distributions in tW production

Normalized top p_T distribution tW aN³LO Normalized rapidity distribution

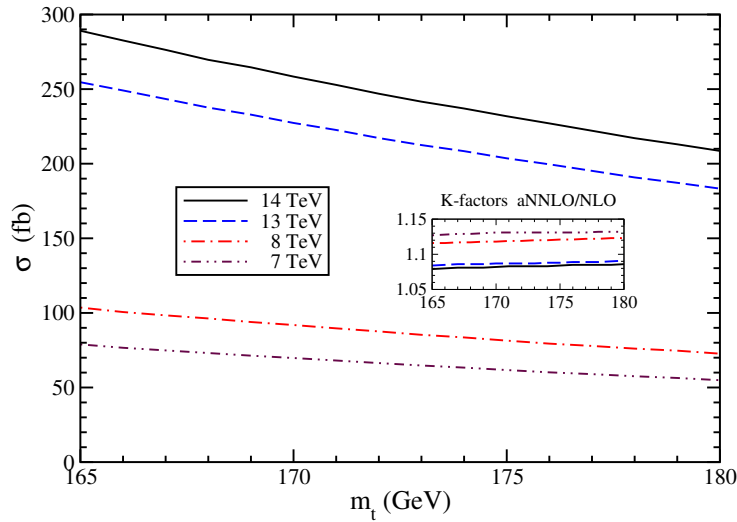


tZ production via anomalous couplings

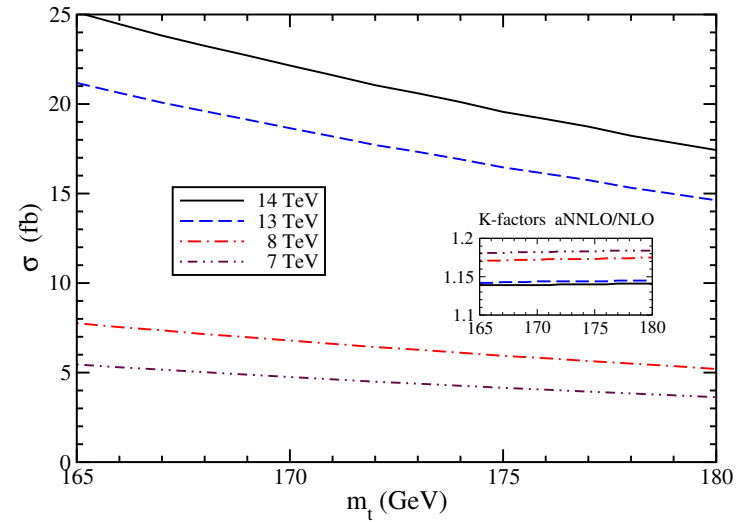


$$\Delta\mathcal{L}^{eff} = \frac{1}{\Lambda} \kappa_{tqZ} e \bar{t} (i/2) (\gamma_\mu \gamma_\nu - \gamma_\nu \gamma_\mu) q F_Z^{\mu\nu} + h.c.$$

g u → t Z at LHC aNNLO $k_{tZ}=0.01$

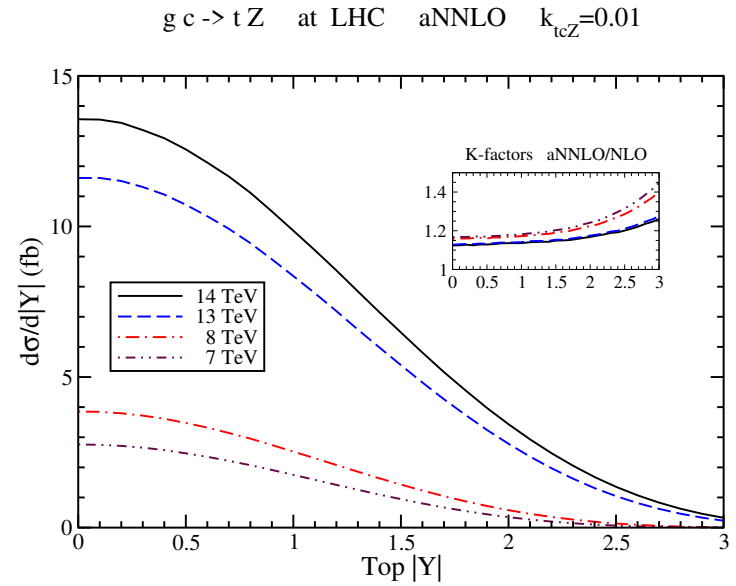
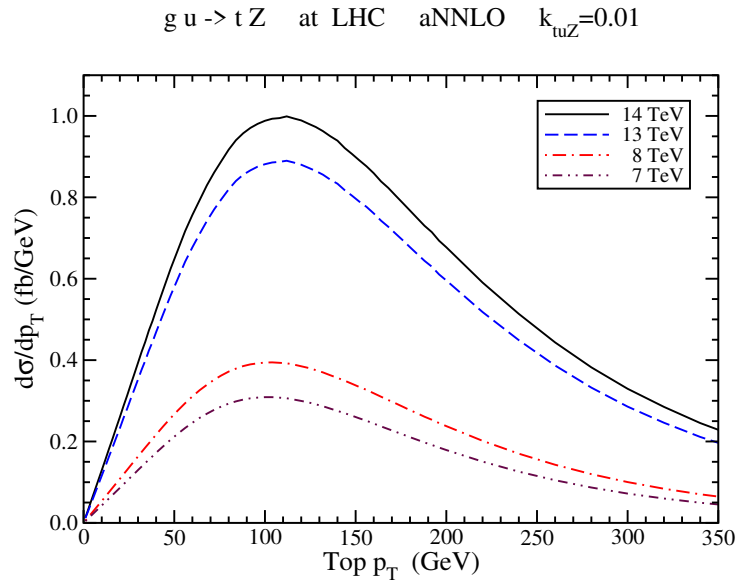


g c → t Z at LHC aNNLO $k_{tZ}=0.01$



tZ production via anomalous couplings

Top-quark p_T and rapidity distributions



Summary

- cross sections and distributions for single-top production
- soft-gluon corrections
- t -channel at aNNLO
- s -channel at aNNLO
- tW production at aN³LO
- excellent agreement with LHC and Tevatron data
- tZ production via anomalous couplings
- high-order corrections are very significant