

CIPANP 2018 - Thirteenth Conference on the Intersections of Particle and Nuclear Physics
Palm Springs, May 29 - June 3 2018

Neutrino-less double beta decay in chiral Effective Field Theory

Vincenzo Cirigliano

Los Alamos National Laboratory



Outline

- Effective Field Theory (EFT) framework for $0\nu\beta\beta$
- $0\nu\beta\beta$ from light Majorana ν exchange
 - *A new leading short-range contribution to the neutrino potential*
 - Quick tour of higher order corrections

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729, to appear in Physical Review C

V. Cirigliano, W. Dekens, M. Graesser, E. Mereghetti, S. Pastore, J. de Vries, U. van Kolck
1802.10097, Phys.Rev.Lett. 120 (2018) no.20, 202001

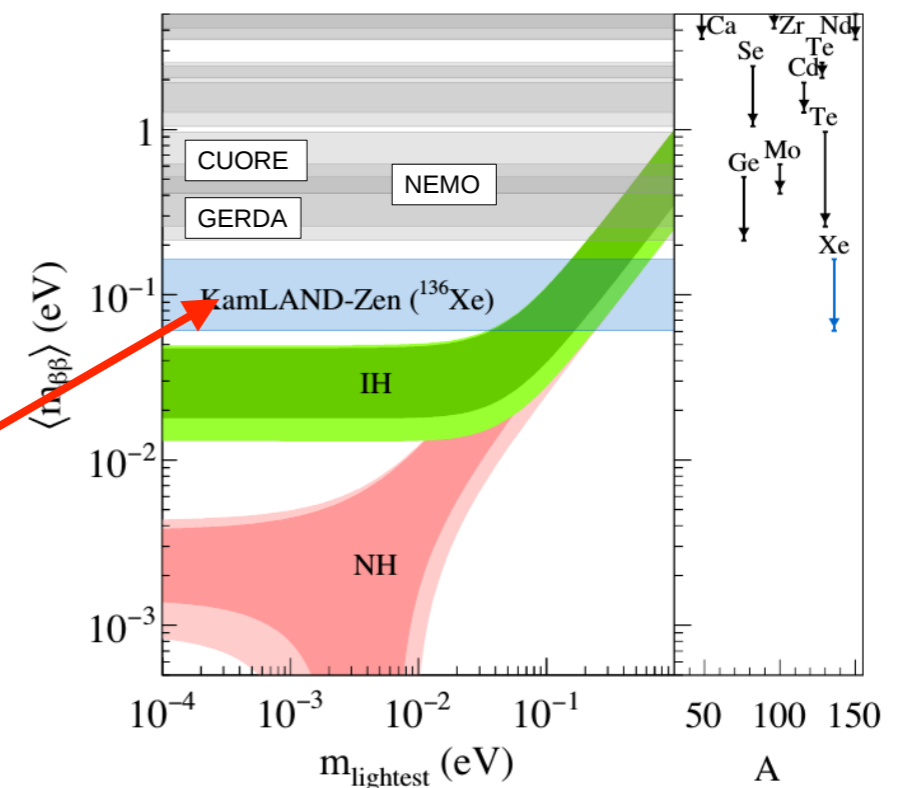
EFT framework for $0\nu\beta\beta$

$$(N, Z) \rightarrow (N - 2, Z + 2) + e^- + e^-$$

- Ton-scale $0\nu\beta\beta$ searches will probe LNV from a variety of mechanisms
- Impact of $0\nu\beta\beta$ results most efficiently analyzed in EFT framework:

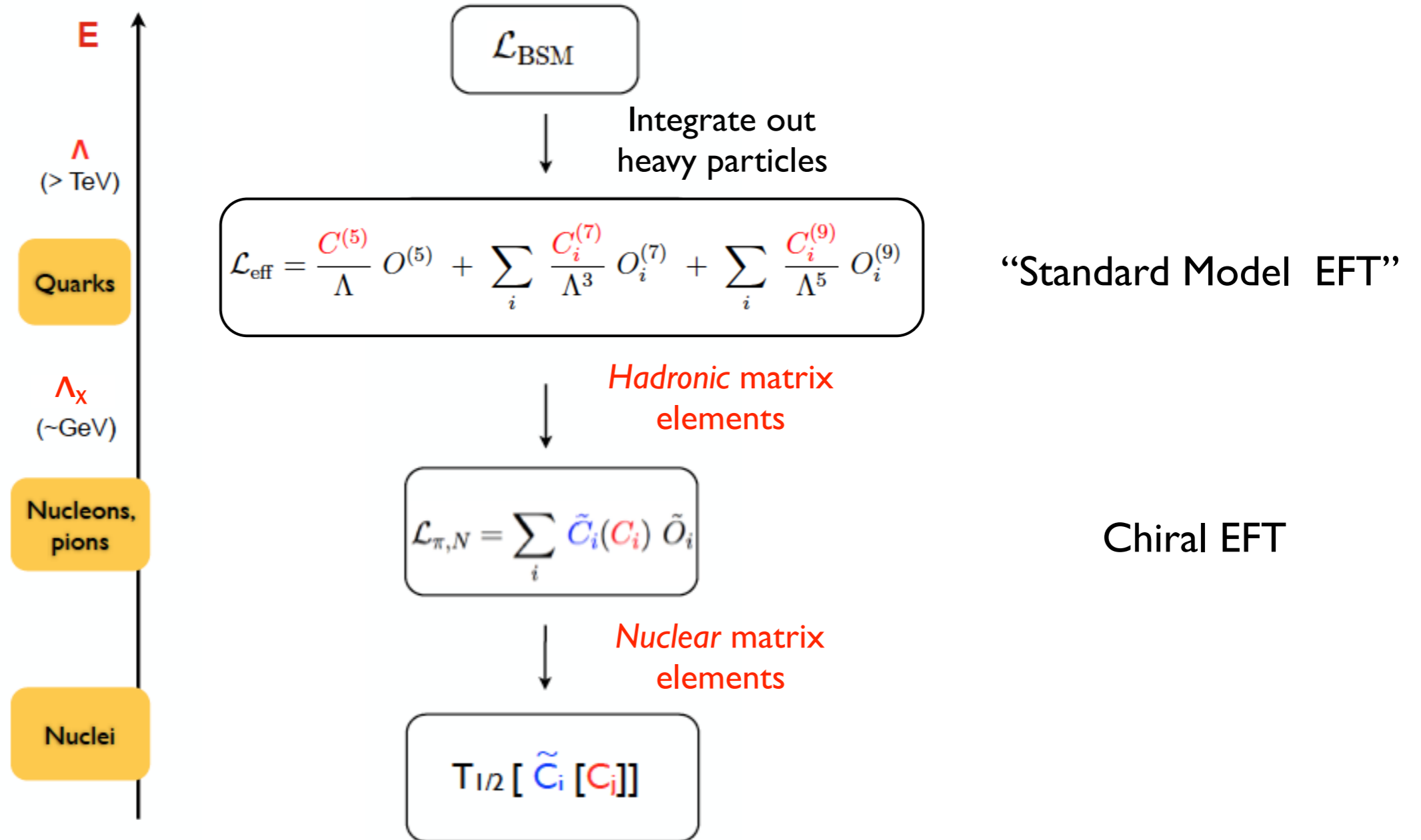
1. Classify sources of Lepton Number Violation and relate $0\nu\beta\beta$ to other LNV processes (such as $pp \rightarrow eejj$ at the LHC)

2. Organize contributions to hadronic and nuclear matrix elements in systematic expansion \Rightarrow controllable uncertainties



KamLAND-Zen coll., '16

EFT framework for $0\nu\beta\beta$

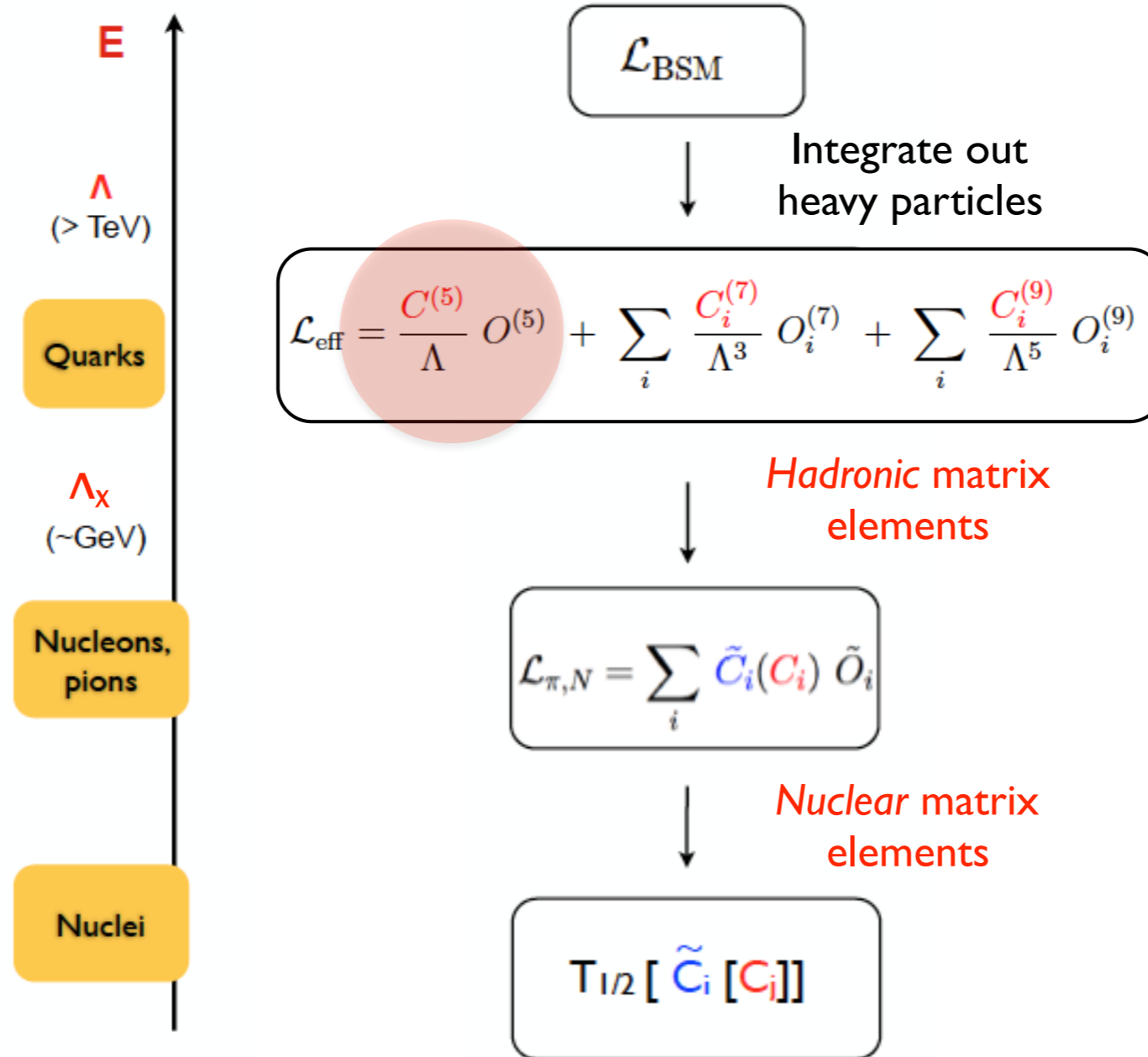


Chain of EFT +
lattice QCD & many-body methods

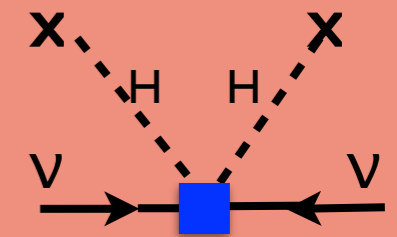


$$T_{1/2} [\tilde{C}_i [C_j]] \sim (m_W/\Lambda)^A (\Lambda_X/m_W)^B (k_F/\Lambda_X)^C$$

EFT framework for $0\nu\beta\beta$



Focus on dim-5 operator
 $O^{(5)} \sim LLHH$
 (Majorana mass for ν)



For dim-7,9 and general analysis see
 VC, W. Dekens, M. Graesser, E. Mereghetti, J. de Vries
 1708.09390 and 1806.xxxxx

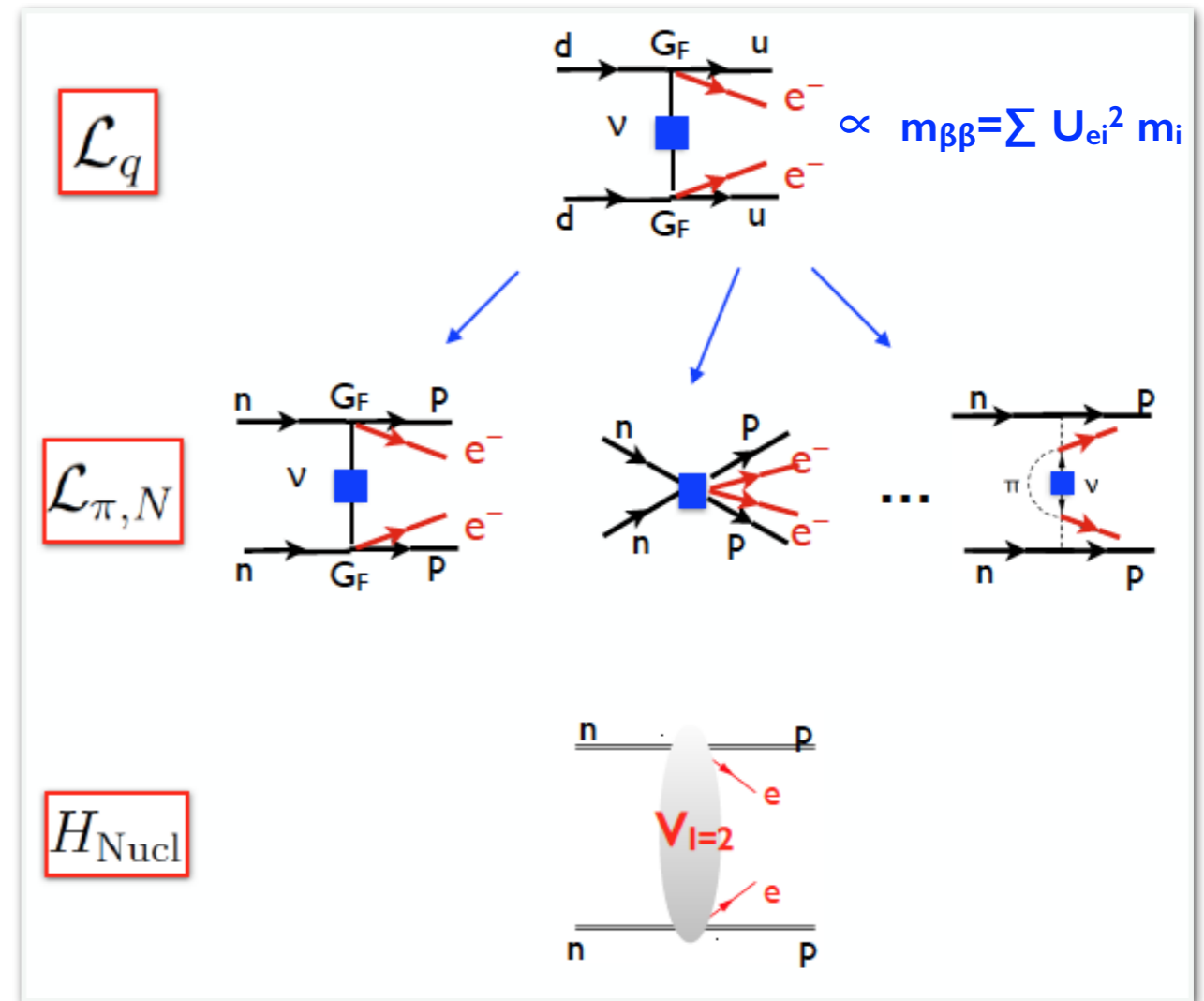
Chain of EFT +
 lattice QCD & many-body methods



$$T_{1/2} [\tilde{C}_i [C_j]] \sim (m_W/\Lambda)^A (\Lambda_\chi/m_W)^B (k_F/\Lambda_\chi)^C$$

From quarks to nuclei

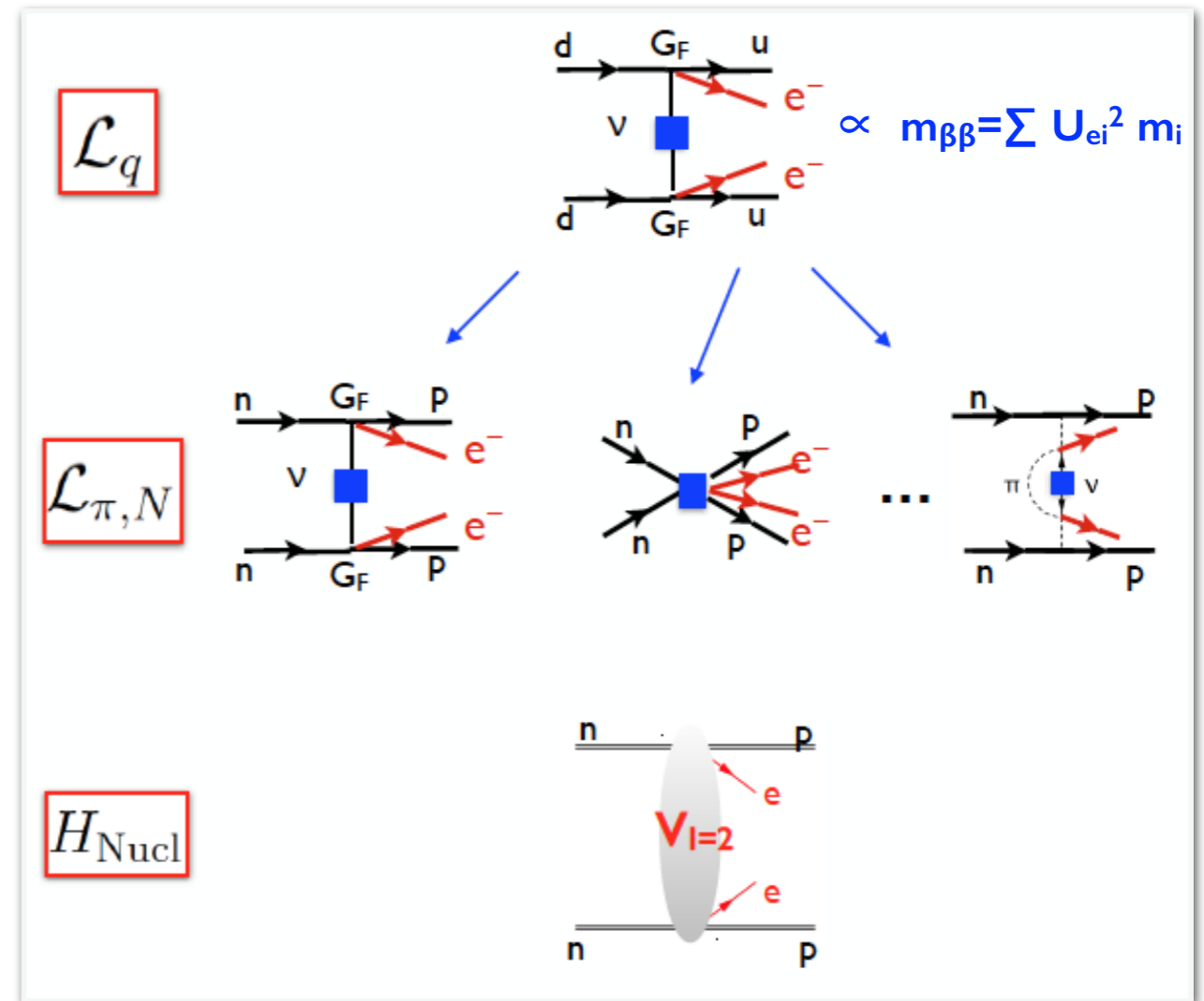
- At $E \sim \Lambda_\chi \sim m_N \sim \text{GeV}$ integrate out hard V 's and gluons ($E, |\mathbf{p}| > \Lambda_\chi$)
- Map $\Delta L=2$ Lagrangian onto π, N operators, organized according to power-counting in Q/Λ_χ ($Q \sim k_F \sim m_\pi$)
- Integrate out soft and potential V 's and π 's with $(E, |\mathbf{p}|) \sim Q$ and $(E, |\mathbf{p}|) \sim (Q^2/m_N, Q) \rightarrow$ obtain nuclear hamiltonian



$$H_{\text{Nucl}} = H_0 + \sqrt{2}G_F V_{ud} \bar{N} (g_V \delta^{\mu 0} - g_A \delta^{\mu i} \sigma^i) \tau^+ N \bar{e}_L \gamma_\mu \nu_L + 2G_F^2 V_{ud}^2 m_{\beta\beta} \bar{e}_L e_L^c V_{I=2}$$

From quarks to nuclei

- At $E \sim \Lambda_\chi \sim m_N \sim \text{GeV}$ integrate out hard V 's and gluons ($E, |\mathbf{p}| > \Lambda_\chi$)
- Map $\Delta L=2$ Lagrangian onto π, N operators, organized according to power-counting in Q/Λ_χ ($Q \sim k_F \sim m_\pi$)
- Integrate out soft and potential V 's and π 's with $(E, |\mathbf{p}|) \sim Q$ and $(E, |\mathbf{p}|) \sim (Q^2/m_N, Q) \rightarrow$ obtain nuclear hamiltonian

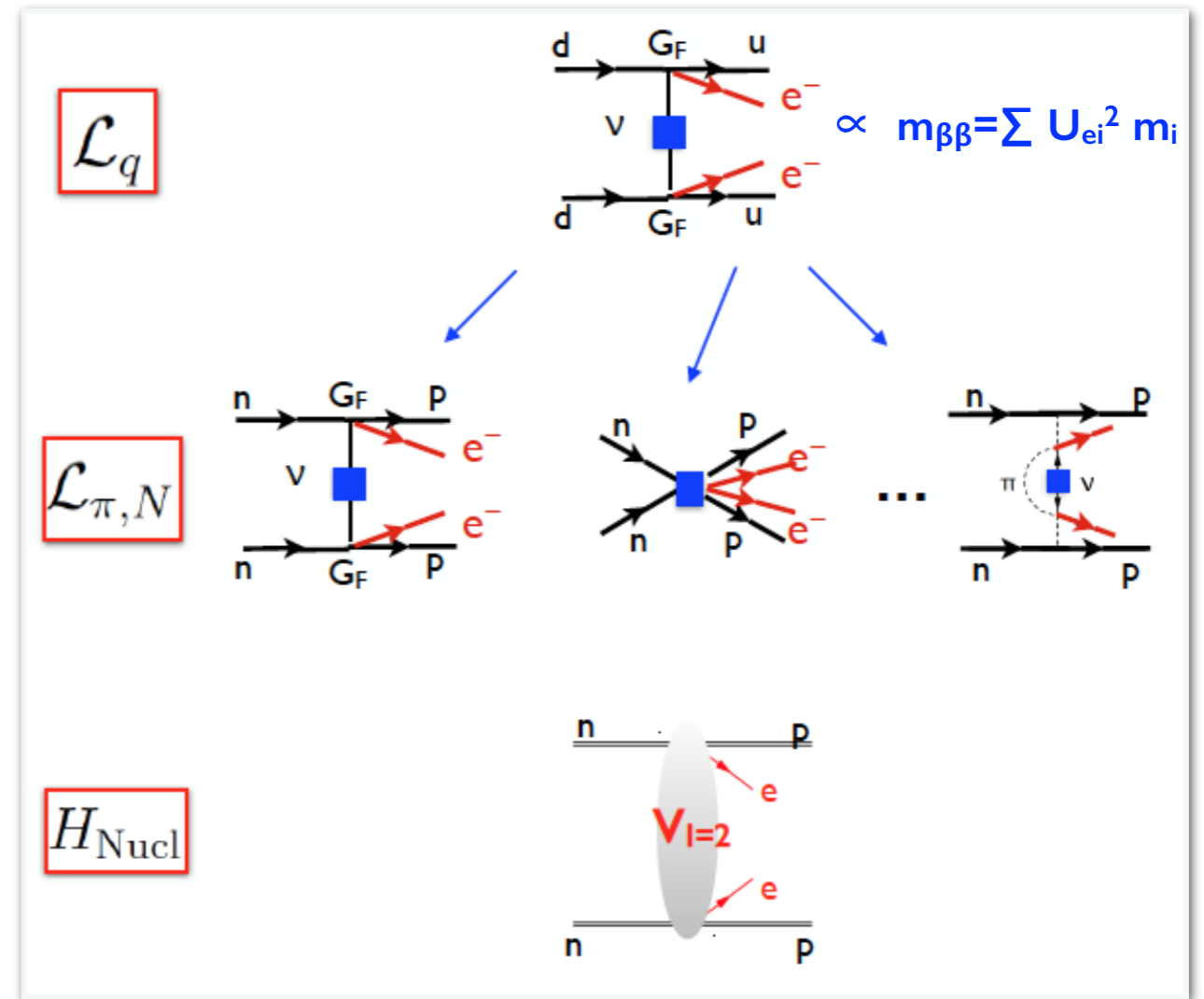


$$H_{\text{Nucl}} = H_0 + \sqrt{2} G_F V_{ud} \bar{N} (g_V \delta^{\mu 0} - g_A \delta^{\mu i} \sigma^i) \tau^+ N \bar{e}_L \gamma_\mu \nu_L + 2 G_F^2 V_{ud}^2 m_{\beta\beta} \bar{e}_L e_L^c V_{I=2}$$

“Ultra-soft” (e, ν) with $|\mathbf{p}|, E \ll k_F$
cannot be integrated out

From quarks to nuclei

- At $E \sim \Lambda_\chi \sim m_N \sim \text{GeV}$ integrate out hard V 's and gluons ($E, |\mathbf{p}| > \Lambda_\chi$)
- Map $\Delta L=2$ Lagrangian onto π, N operators, organized according to power-counting in Q/Λ_χ ($Q \sim k_F \sim m_\pi$)
- Integrate out soft and potential V 's and π 's with $(E, |\mathbf{p}|) \sim Q$ and $(E, |\mathbf{p}|) \sim (Q^2/m_N, Q) \rightarrow$ obtain nuclear hamiltonian

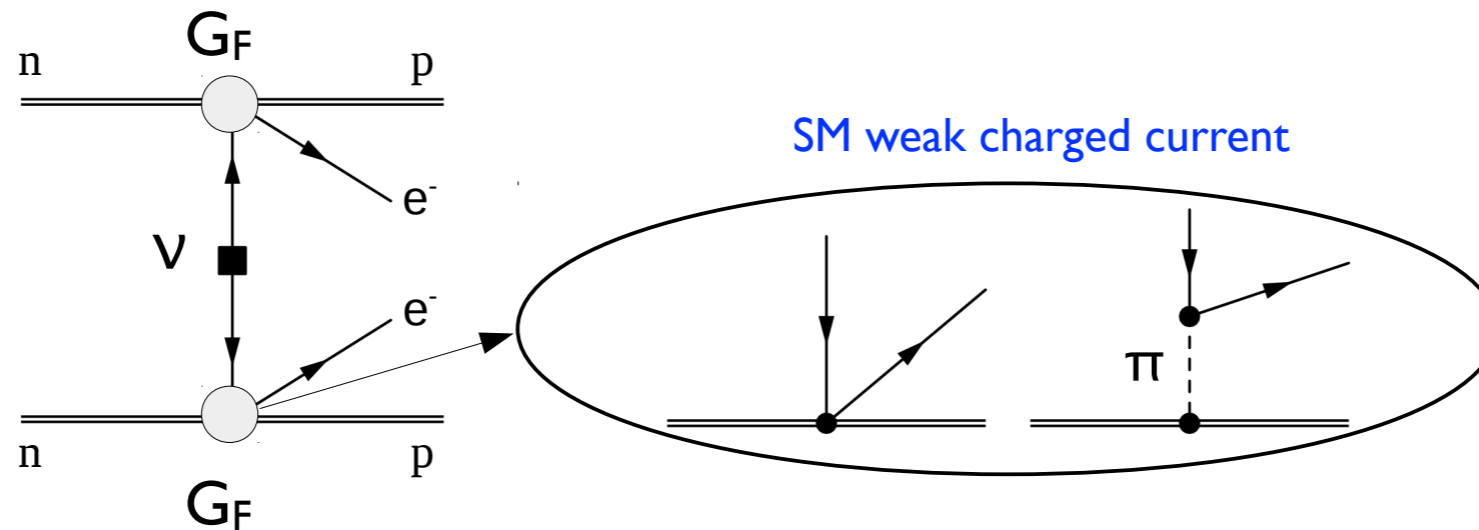


$$H_{\text{Nucl}} = H_0 + \sqrt{2}G_F V_{ud} \bar{N} (g_V \delta^{\mu 0} - g_A \delta^{\mu i} \sigma^i) \tau^+ N \bar{e}_L \gamma_\mu \nu_L + 2G_F^2 V_{ud}^2 m_{\beta\beta} \bar{e}_L e_L^c V_{I=2}$$

“Ultra-soft” (e, ν) with $|\mathbf{p}|, E \ll k_F$ cannot be integrated out

“Isotensor” $0\nu\beta\beta$ potential mediates $nn \rightarrow pp$. It can be identified to a given order in Q/Λ_χ by computing 2-nucleon amplitude

Leading order $0\nu\beta\beta$ potential

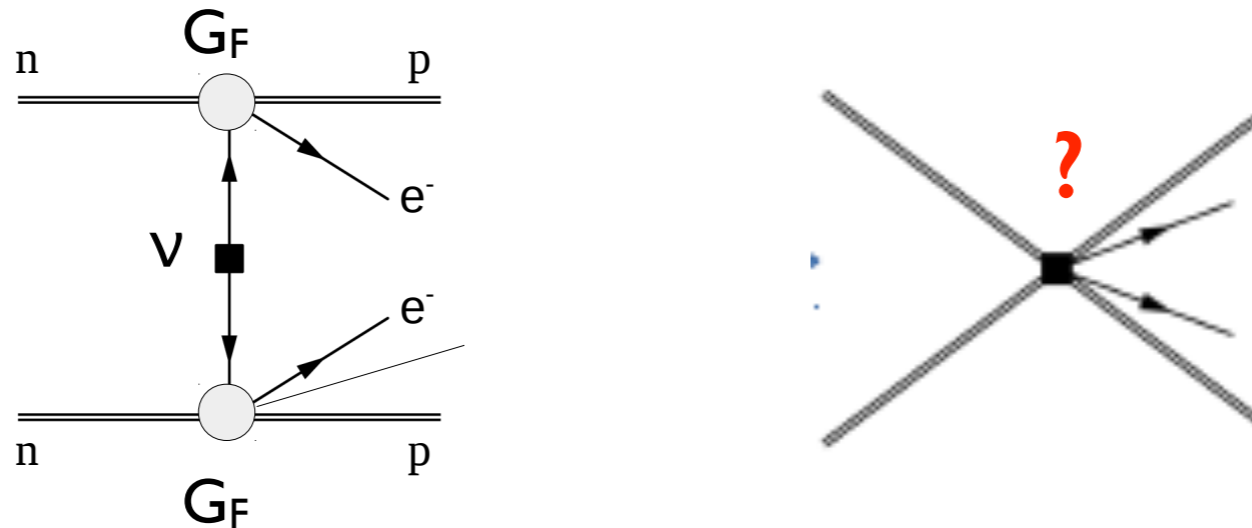


- Tree-level exchange of Majorana neutrinos

$$V_{\nu,0}^{(a,b)} = \tau^{(a)} + \tau^{(b)} + \frac{1}{q^2} \left\{ 1 - g_A^2 \left[\sigma^{(a)} \cdot \sigma^{(b)} - \sigma^{(a)} \cdot \mathbf{q} \sigma^{(b)} \cdot \mathbf{q} \frac{2m_\pi^2 + q^2}{(q^2 + m_\pi^2)^2} \right] \right\}$$

Hadronic
input: g_A

Leading order $0\nu\beta\beta$ potential



- Tree-level exchange of Majorana neutrinos

$$V_{\nu,0}^{(a,b)} = \tau^{(a)+}\tau^{(b)+} \frac{1}{q^2} \left\{ 1 - g_A^2 \left[\sigma^{(a)} \cdot \sigma^{(b)} - \sigma^{(a)} \cdot \mathbf{q} \sigma^{(b)} \cdot \mathbf{q} \frac{2m_\pi^2 + q^2}{(q^2 + m_\pi^2)^2} \right] \right\} \quad \text{Hadronic input: } g_A$$

- Symmetries allow non-derivative contact term

$$V_{\nu,CT}^{(a,b)} = -2 g_\nu \tau^{(a)+}\tau^{(b)+}$$

$g_\nu \sim 1/(4\pi F_\pi)^2$ in NDA /
Weinberg counting
(and hence sub-leading)
But is it?

Scaling of contact term in $0\nu\beta\beta$

- Study UV divergences in $nn \rightarrow ppee$ amplitude, with LO strong potential

$$V_{\text{strong}}(r) = \tilde{C} \delta^{(3)}(\mathbf{r}) + \frac{g_A^2 m_\pi^2}{16\pi F_\pi^2} \frac{e^{-m_\pi r}}{4\pi r}$$

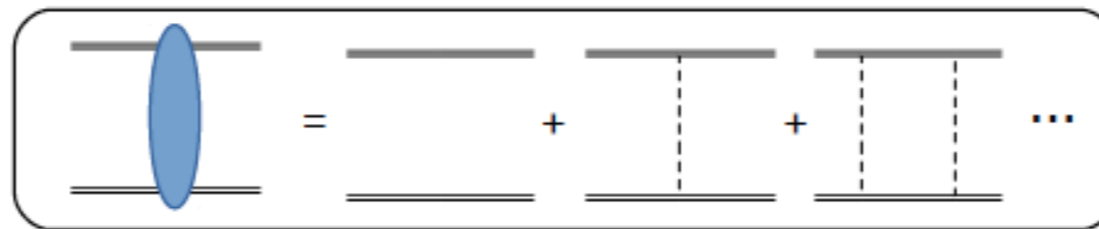
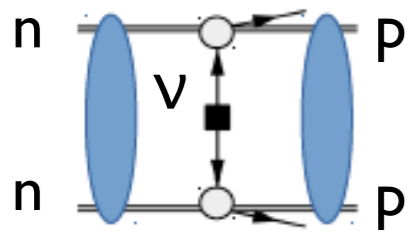
$\tilde{C} \sim 1/F_\pi^2$
from fit to a_{NN}

Scaling of contact term in $0\nu\beta\beta$

- Study UV divergences in $nn \rightarrow ppee$ amplitude, with LO strong potential

$$V_{\text{strong}}(r) = \tilde{C} \delta^{(3)}(\mathbf{r}) + \frac{g_A^2 m_\pi^2}{16\pi F_\pi^2} \frac{e^{-m_\pi r}}{4\pi r}$$

$\tilde{C} \sim 1/F_\pi^2$
from fit to a_{NN}



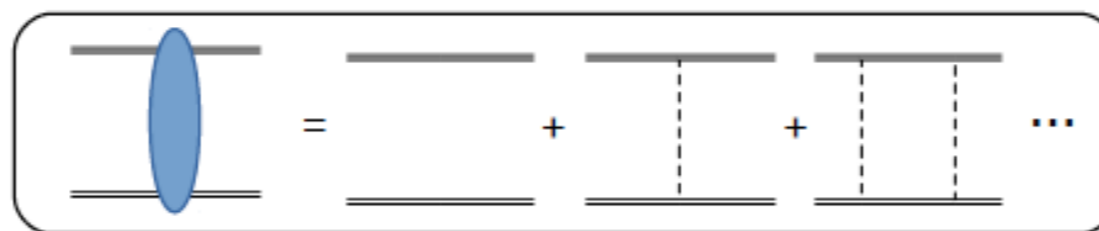
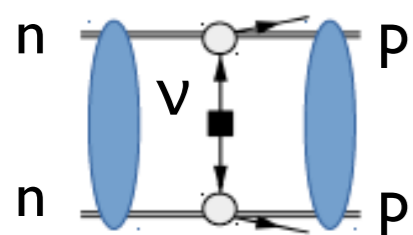
finite

Scaling of contact term in $0\nu\beta\beta$

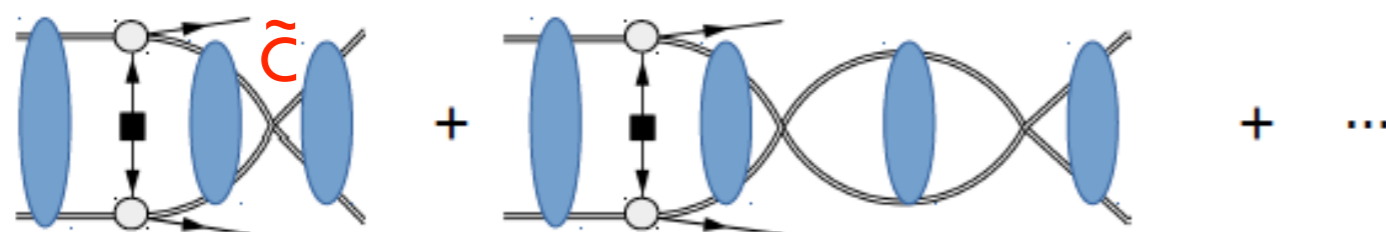
- Study UV divergences in $nn \rightarrow ppee$ amplitude, with LO strong potential

$$V_{\text{strong}}(r) = \tilde{C} \delta^{(3)}(\mathbf{r}) + \frac{g_A^2 m_\pi^2}{16\pi F_\pi^2} \frac{e^{-m_\pi r}}{4\pi r}$$

$\tilde{C} \sim 1/F_\pi^2$
from fit to a_{NN}



finite



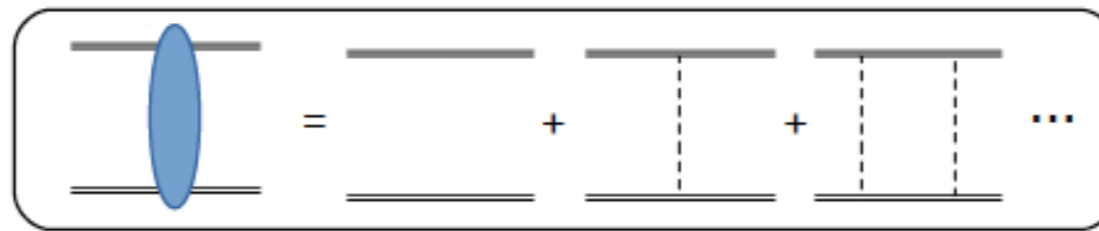
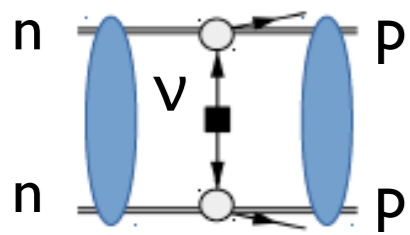
finite

Scaling of contact term in $0\nu\beta\beta$

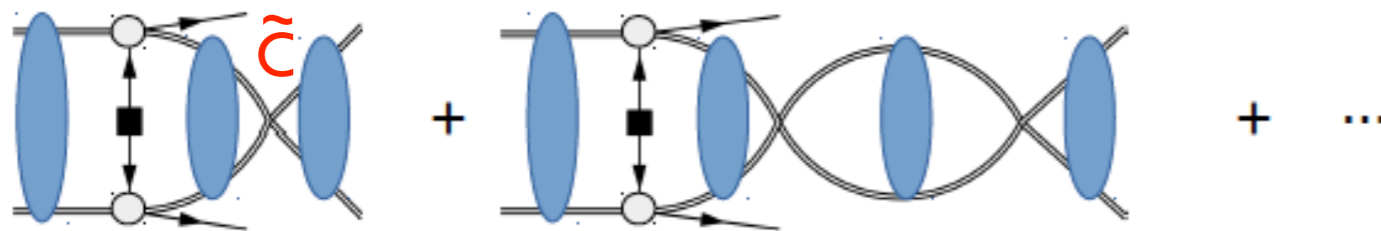
- Study UV divergences in $nn \rightarrow ppee$ amplitude, with LO strong potential

$$V_{\text{strong}}(r) = \tilde{C} \delta^{(3)}(\mathbf{r}) + \frac{g_A^2 m_\pi^2}{16\pi F_\pi^2} \frac{e^{-m_\pi r}}{4\pi r}$$

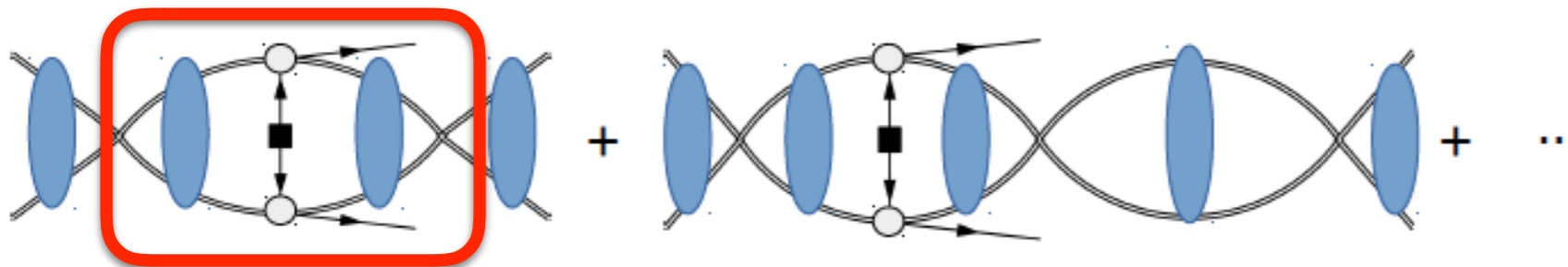
$\tilde{C} \sim 1/F_\pi^2$
from fit to a_{NN}



finite



finite



2-loop diagram is
UV divergent!

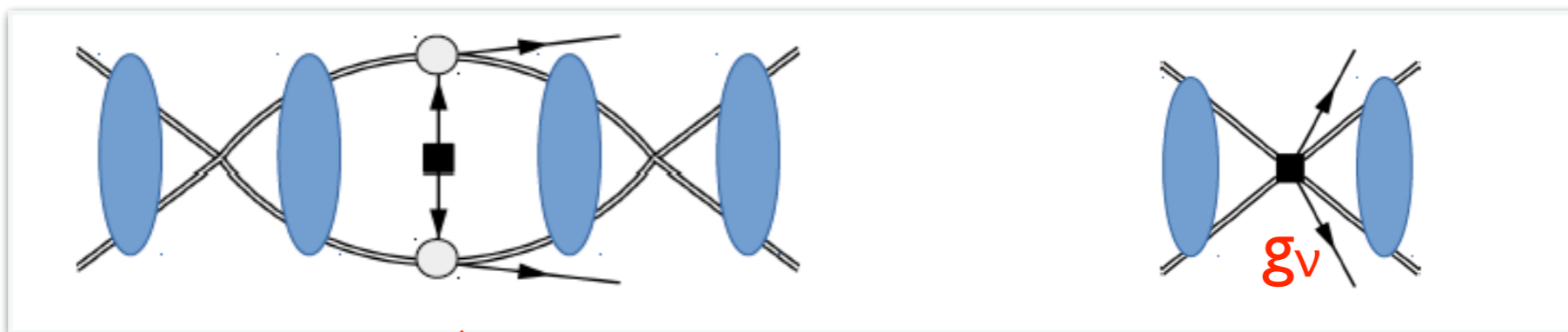
Scaling of contact term in $0\nu\beta\beta$

- Study UV divergences in $nn \rightarrow ppee$ amplitude, with LO strong potential

$$V_{\text{strong}}(r) = \tilde{C} \delta^{(3)}(\mathbf{r}) + \frac{g_A^2 m_\pi^2}{16\pi F_\pi^2} \frac{e^{-m_\pi r}}{4\pi r}$$

$\tilde{C} \sim 1/F_\pi^2$
from fit to a_{NN}

- Renormalization requires contact LNV operator at LO!



$$\sim \frac{1}{2}(1 + 2g_A^2) \left(\frac{m_N \tilde{C}}{4\pi} \right)^2 \left(\frac{1}{4-d} + \log \mu^2 \right)$$

- The coupling scales as $g_V \sim 1/F_\pi^2 \gg 1/(4\pi F_\pi)^2$, same order as $1/q^2$ from tree-level neutrino exchange

If you don't like Feynman diagrams...

- Same conclusion obtained by solving the Schroedinger equation

- Use smeared delta function to regulate short range strong potential:

$$\tilde{C} \rightarrow \tilde{C} (R_S) \sim 1/F_{\pi}^2$$

$$\delta^{(3)}(\mathbf{r}) \rightarrow \frac{1}{\pi^{3/2} R_S^3} e^{-\frac{r^2}{R_S^2}}$$

- Compute amplitude

$$A_{\nu} = \int d^3\mathbf{r} \psi_{\mathbf{p}'}^{-}(\mathbf{r}) V_{\nu}(\mathbf{r}) \psi_{\mathbf{p}}^{+}(\mathbf{r})$$

If you don't like Feynman diagrams...

- Same conclusion obtained by solving the Schroedinger equation

- Use smeared delta function to regulate short range strong potential:

$$\tilde{C} \rightarrow \tilde{C}(R_S) \sim 1/F_\pi^2$$

$$\delta^{(3)}(\mathbf{r}) \rightarrow \frac{1}{\pi^{3/2} R_S^3} e^{-\frac{r^2}{R_S^2}}$$

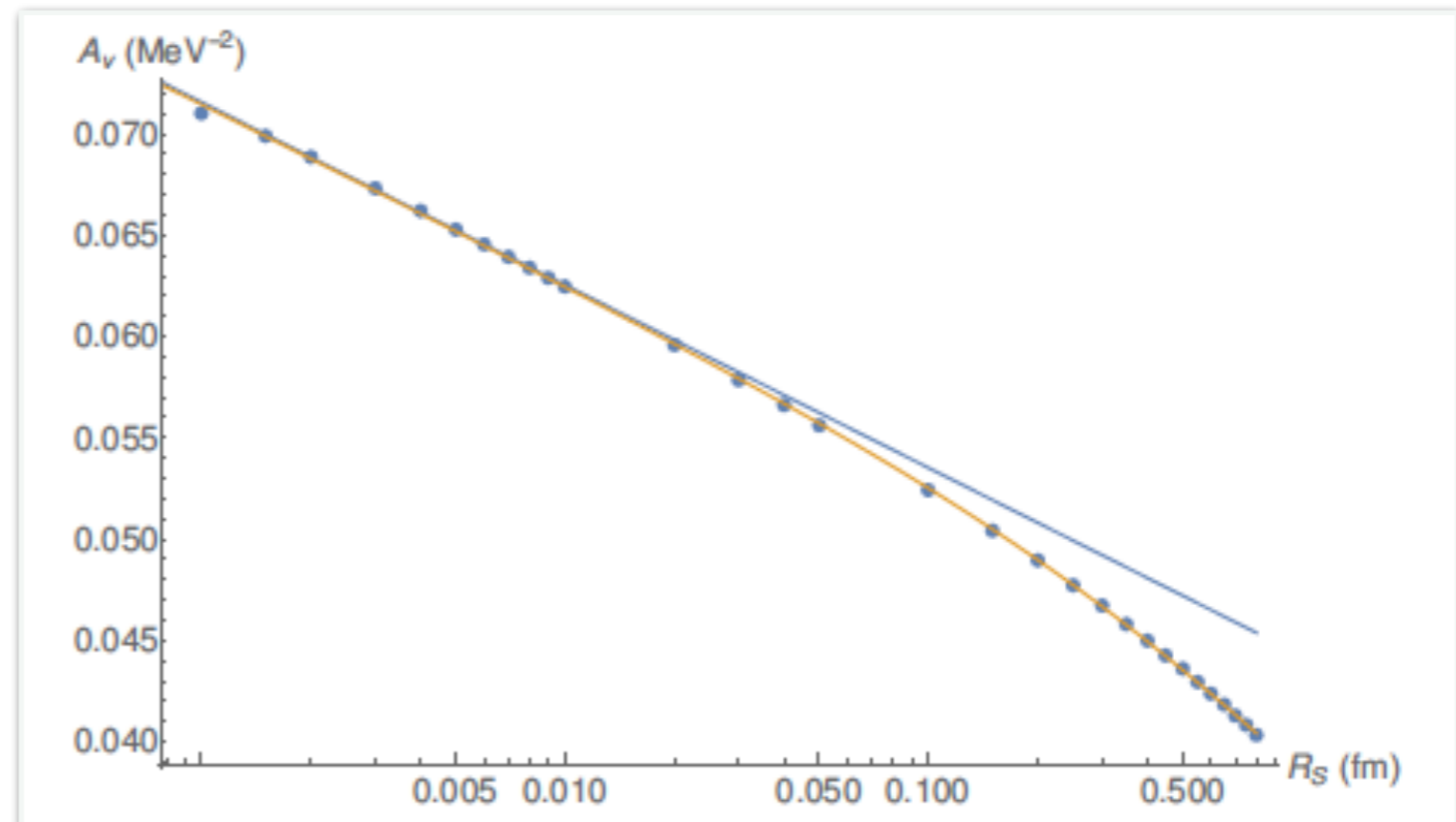
- Compute amplitude

$$A_\nu = \int d^3\mathbf{r} \psi_{\mathbf{p}'}^-(\mathbf{r}) V_\nu(\mathbf{r}) \psi_{\mathbf{p}}^+(\mathbf{r})$$

- Logarithmic dependence on $R_S \Rightarrow$

need LO counterterm

$g_\nu \sim 1/F_\pi^2 \log R_S$ to obtain physical, regulator-independent result



Estimating finite part of g_V

I) Match χ EFT & **lattice QCD** calculation of hadronic amplitude $nn \rightarrow pp$

$$S_{\text{eff}}^{\Delta L=2} = \frac{i8G_F^2 V_{ud}^2 m_{\beta\beta}}{2!} \int d^4x \bar{e}_L(x) e_L^c(x) \int d^4y S(x-y) T\left(\bar{u}_L \gamma_\mu d_L(x) \bar{u}_L \gamma_\mu d_L(y)\right) g^{\mu\nu}$$

Scalar massless propagator



Estimating finite part of g_V

1) Match χ EFT & **lattice QCD** calculation of hadronic amplitude $nn \rightarrow pp$

$$S_{\text{eff}}^{\Delta L=2} = \frac{i8G_F^2 V_{ud}^2 m_{\beta\beta}}{2!} \int d^4x \bar{e}_L(x) e_L^c(x) \int d^4y S(x-y) T\left(\bar{u}_L \gamma_\mu d_L(x) \bar{u}_L \gamma_\mu d_L(y)\right) g^{\mu\nu}$$

Scalar massless propagator

$(J_+ \times J_+)$ vs $(J_{EM} \times J_{EM})_{I=2}$

2) **Chiral symmetry** relates g_V to $I=2$ electromagnetic LECs (hard ν vs γ)

$$Q_L = \frac{\tau^z}{2}, Q_R = \frac{\tau^z}{2}$$

$$e^2 C_1 \left(\bar{N} Q_L N \bar{N} Q_L N - \frac{\text{Tr}[Q_L^2]}{6} \bar{N} \tau N \cdot \bar{N} \tau N + L \rightarrow R \right)$$

$$e^2 C_2 \left(\bar{N} Q_L N \bar{N} Q_R N - \frac{\text{Tr}[Q_L Q_R]}{6} \bar{N} \tau N \cdot \bar{N} \tau N + L \rightarrow R \right)$$

$$Q_L = u^\dagger Q_L u$$

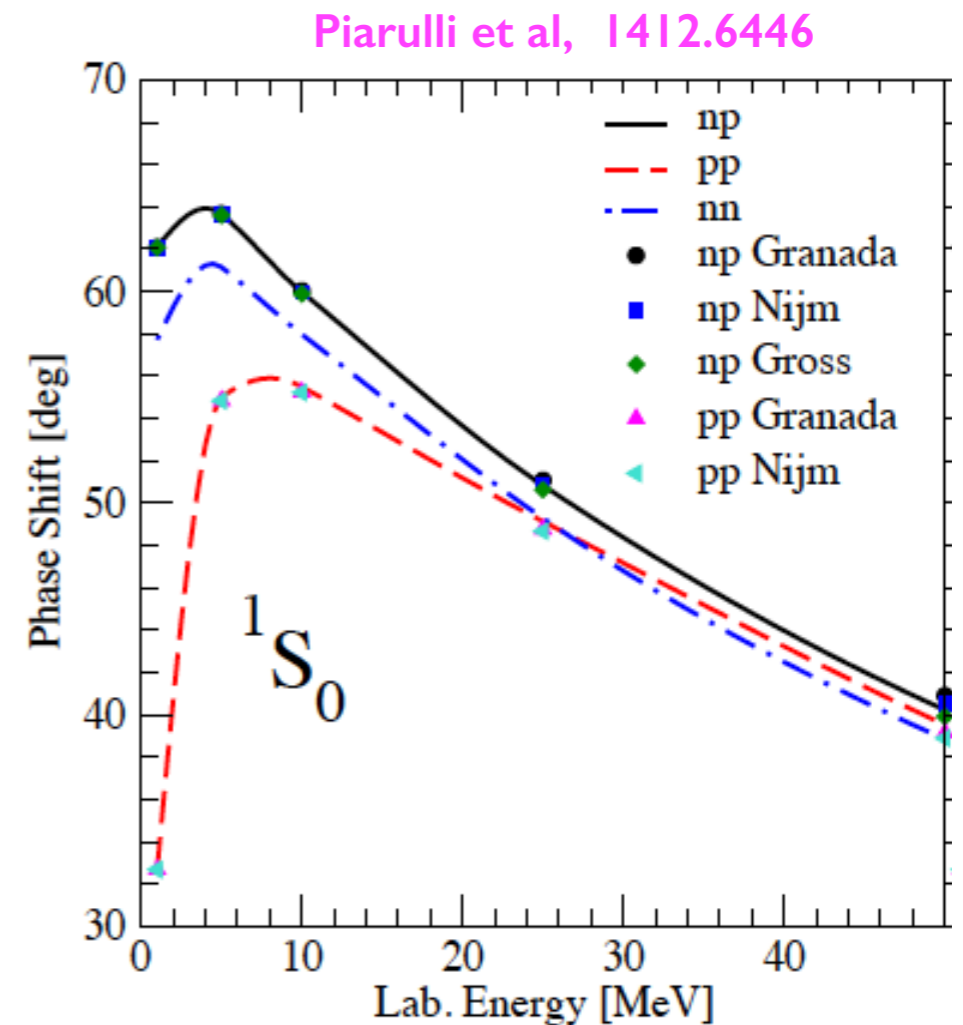
$$Q_R = u Q_R u^\dagger$$

$$u = 1 + \frac{i\pi \cdot \tau}{2F_\pi} + \dots$$

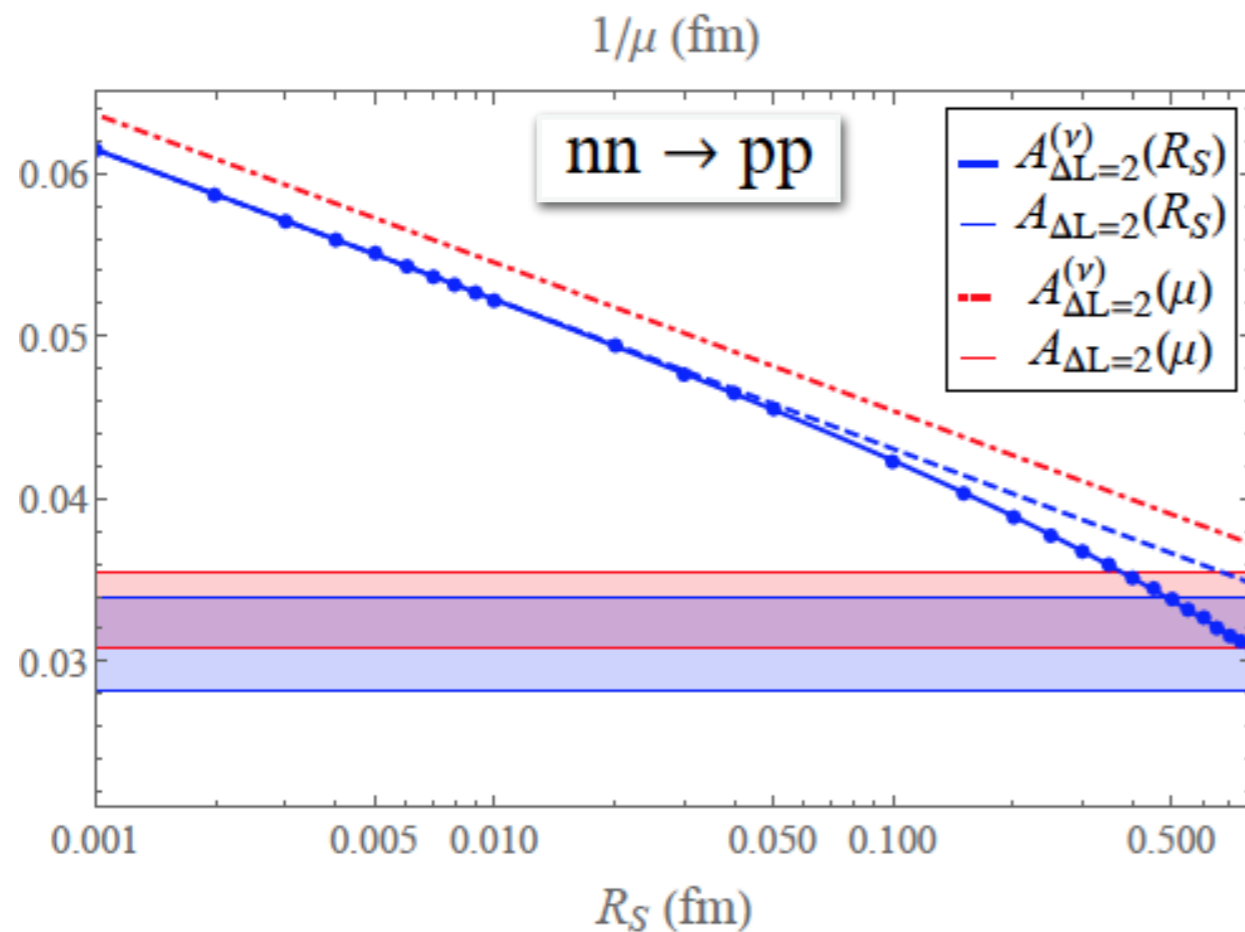
Two $I=2$ NN non-derivative operators: chiral symmetry $\Rightarrow g_V = C_1$

$0\nu\beta\beta$ vs EM isospin breaking

- NN observables cannot disentangle C_1 from C_2 (need pions), but provide **data-based estimate of C_1+C_2**
- $C_1 + C_2$ controls IB combination of 1S_0 scattering lengths **$a_{nn} + a_{pp} - 2 a_{np}$**
- Fit to data, including Coulomb potential, pion EM mass splitting, and contact terms confirms that **$C_1 + C_2 \sim 1/F_\pi^2 \gg 1/(4\pi F_\pi)^2$**



Estimating numerical impact (I)

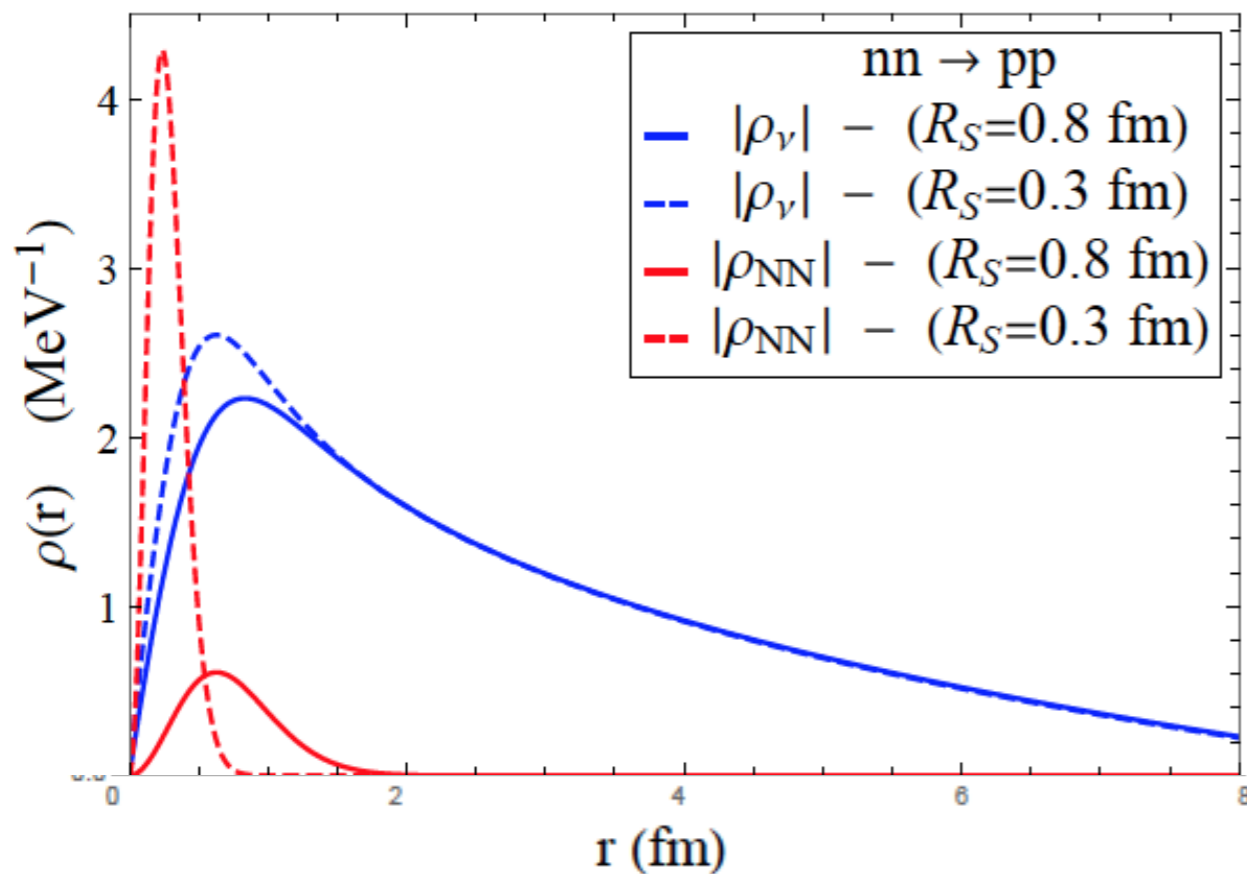


- Assume $C_1=C_2$ and hence $g_v=(C_1+C_2)/2$ at some scale R_S
- $A_{NN}+A_V$ is R_S (or μ) independent and $A_{NN}/A_V \sim 10\%$ (30%) at $R_S \sim 0.8$ fm (0.3 fm) **
- ** Actual correction will be different because in general $C_1 \neq C_2$

Estimating numerical impact (I)

nn → pp

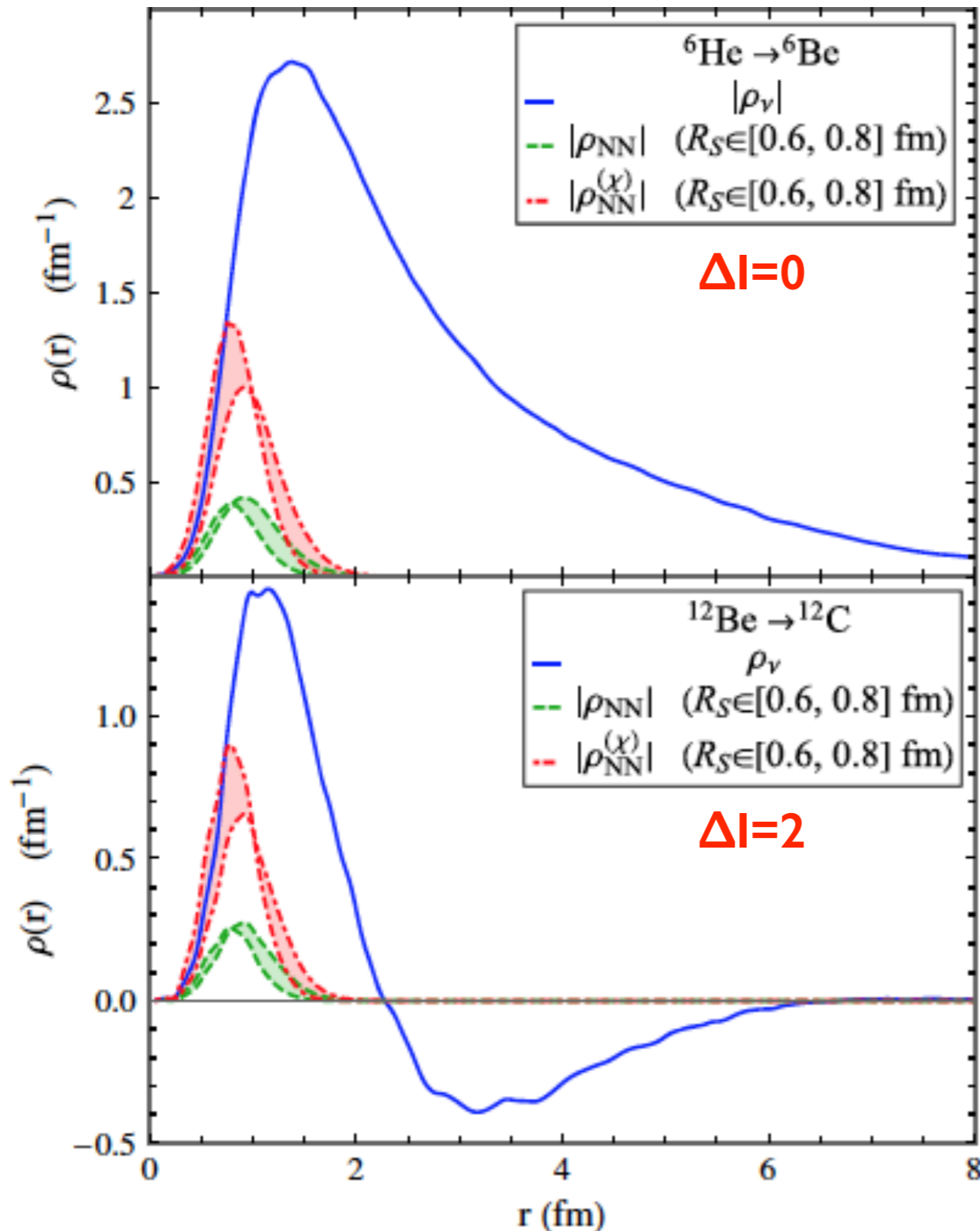
$\Delta I=0$



$$A = \int dr \rho(r)$$

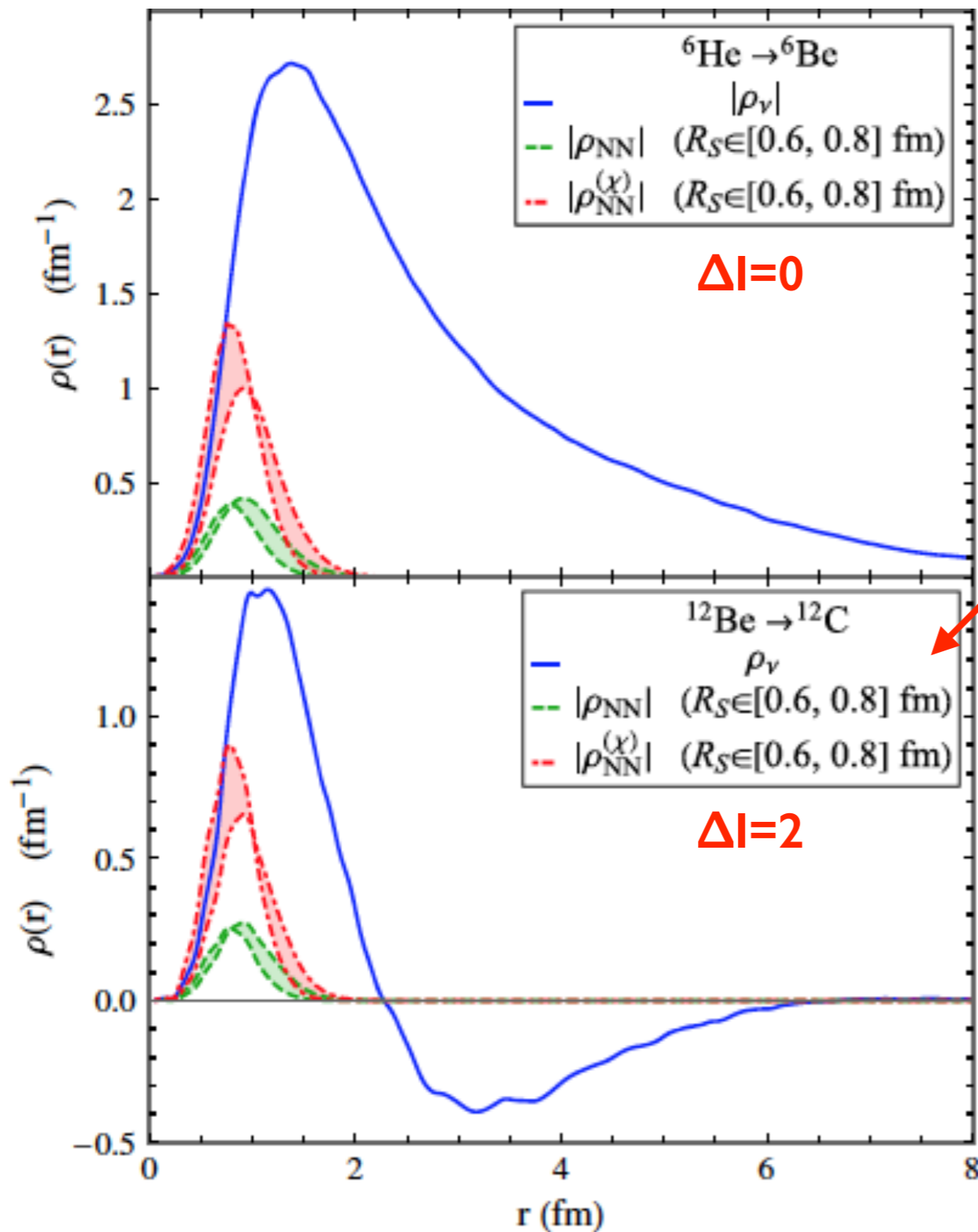
- Assume $C_1=C_2$ and hence $g_V=(C_1+C_2)/2$ at some scale R_S
- $A_{NN}+A_V$ is R_S (or μ) independent and $A_{NN}/A_V \sim 10\%$ (30%) at $R_S \sim 0.8$ fm (0.3 fm) **
- ** Actual correction will be different because in general $C_1 \neq C_2$
- To gain insight on this result, look at “matrix-element density” as function of inter-nucleon distance

Estimating numerical impact (2)



- What about nuclei?
- **For light nuclei:** used wavefunctions obtained via Variational Monte Carlo from AV18 (NN) + U9 (NNN) potentials
- Hybrid calculation at this stage: can't expect R_S -independence
- $g_v \sim (C_1 + C_2)/2$ taken from fit to NN data (**ours** vs **Piarulli et al. 1606.06335**)

Estimating numerical impact (2)

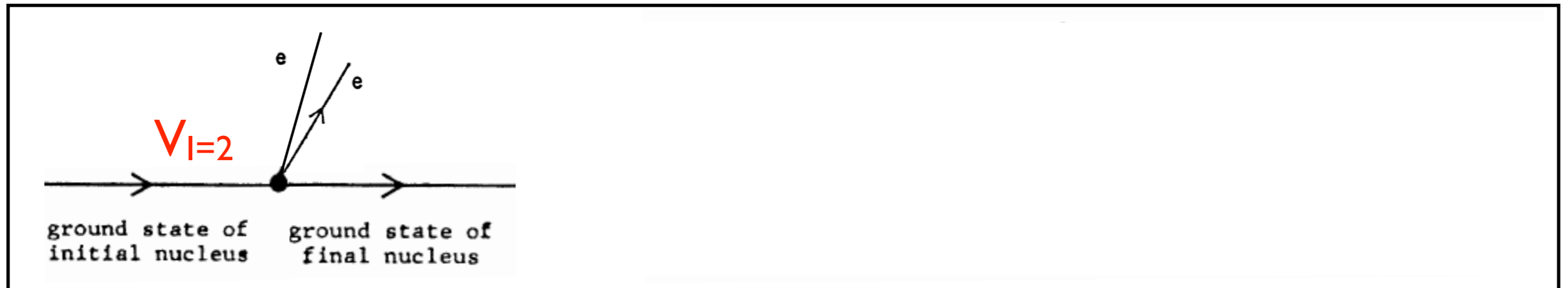


g_v contribution sizable in $\Delta I=2$ transition (*due to node*):
 for $A=12$, $A_{NN}/A_v = 25\%-55\%$

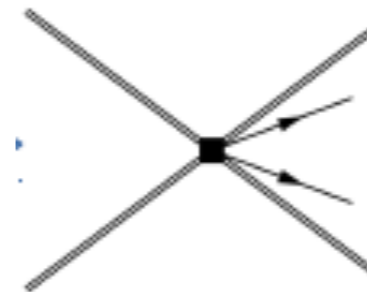
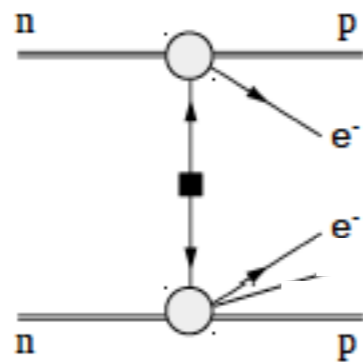
Transitions of interest (${}^{76}\text{Ge} \rightarrow {}^{76}\text{Se}, \dots$)
 have $\Delta I=2$ and node \Rightarrow
 $m_{\beta\beta}$ phenomenology can be significantly affected!

Anatomy of $0\nu\beta\beta$ amplitude in χ EFT

Figure adapted from Primakoff-Rosen 1969



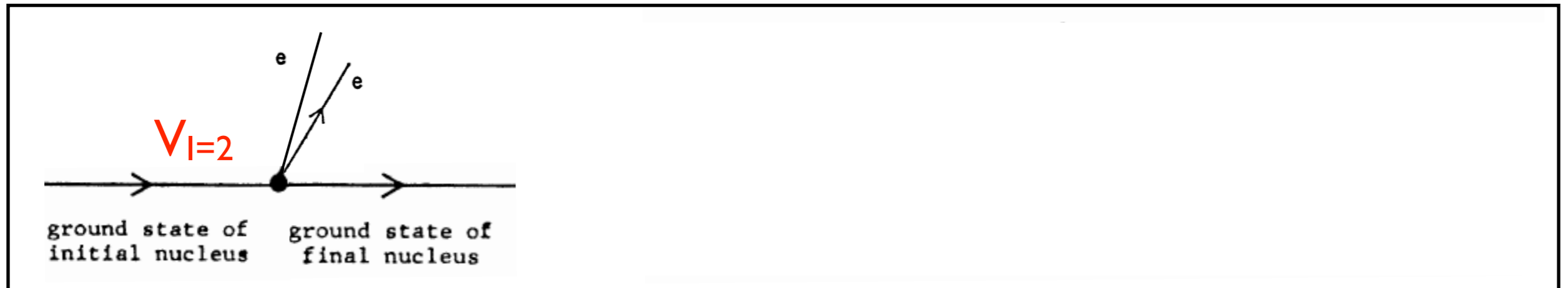
- Leading amplitude controlled by *ground state* matrix element of $V_{v,0}$



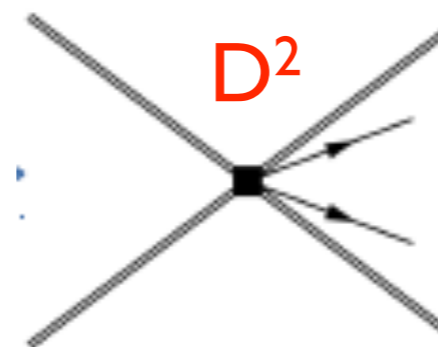
New short range contribution

Anatomy of $0\nu\beta\beta$ amplitude in χ EFT

Figure adapted from Primakoff-Rosen 1969



- NLO: New short range derivative operator $V_{V,I} \sim ND^2N$ NN ?

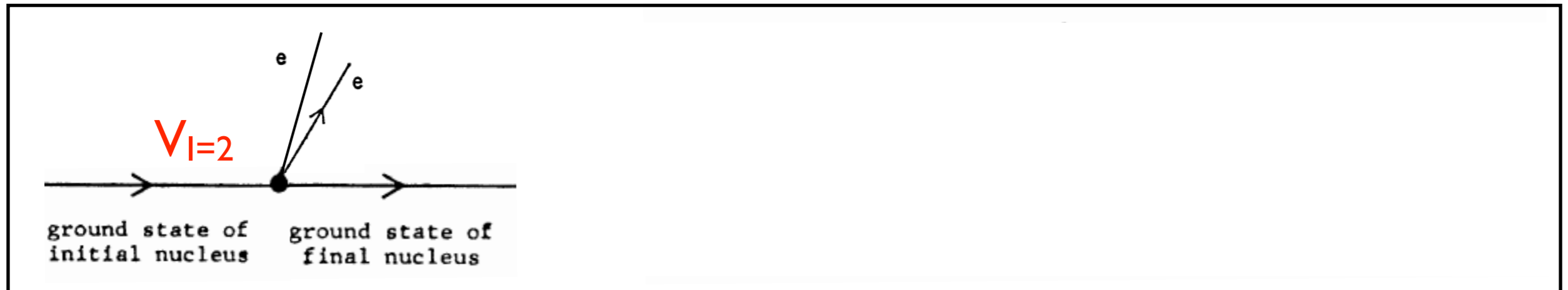


UNDER
INVESTIGATION

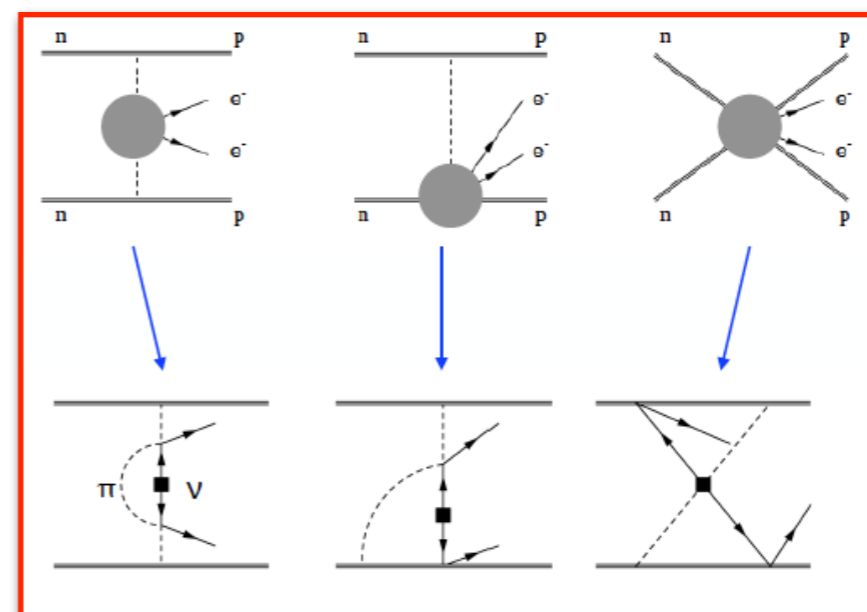
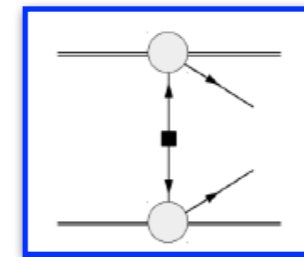
V. Cirigliano, W. Dekens, M. Graesser, E. Mereghetti, S. Pastore, J. de Vries, U. van Kolck

Anatomy of $0\nu\beta\beta$ amplitude in χ EFT

Figure adapted from Primakoff-Rosen 1969



- N2LO (I):
 - Factorizable corrections to 1-body currents (radii, ...)
 - Ground state matrix element of $V_{V,2} \sim V_{V,0} (k_F/4\pi F_\pi)^2$ [π -N loops and contact terms]
 - New non-factorizable terms as important as form-factors**



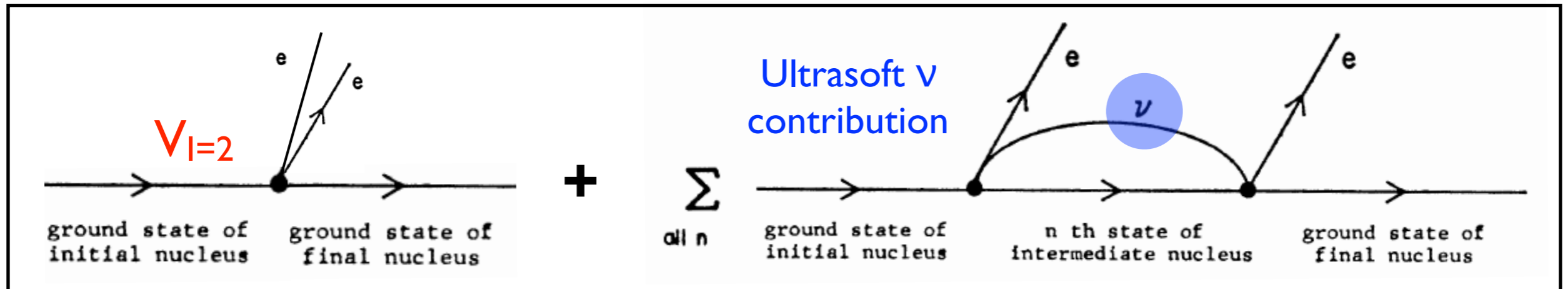
● = one-loop vertex

** S. Pastore, J. Carlson, V. Cirigliano, W. Dekens, E. Mereghetti, R. Wiringa 1710.05026

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

Anatomy of $0\nu\beta\beta$ amplitude in χ EFT

Figure adapted from Primakoff-Rosen 1969



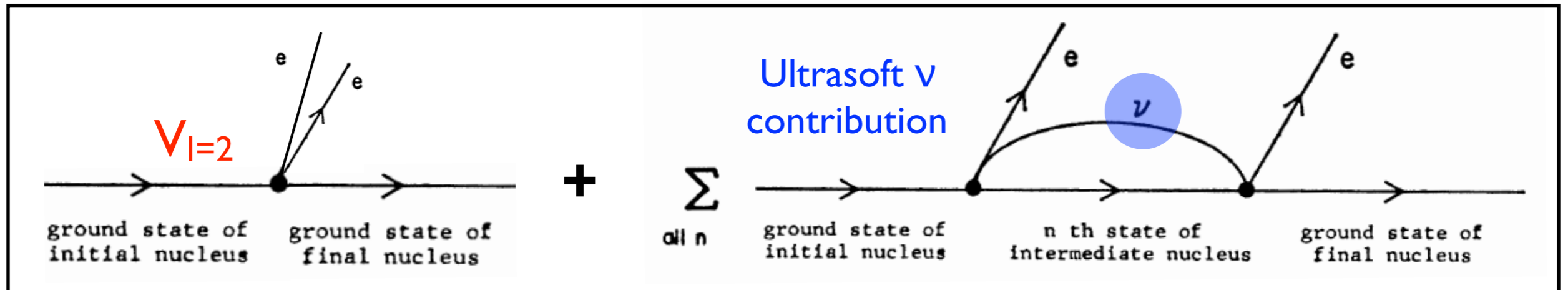
- N2LO (2): ultrasoft ν loop suppressed by $(E_n - E_i)/(4\pi k_F)$

$$T_{\text{usoft}}(\mu_{\text{us}}) = \frac{T_{\text{lept}}}{8\pi^2} \sum_n \langle f | J_\mu | n \rangle \langle n | J^\mu | i \rangle \left\{ (E_2 + E_n - E_i) \left(\log \frac{\mu_{\text{us}}}{2(E_2 + E_n - E_i)} + 1 \right) + 1 \leftrightarrow 2 \right\}$$

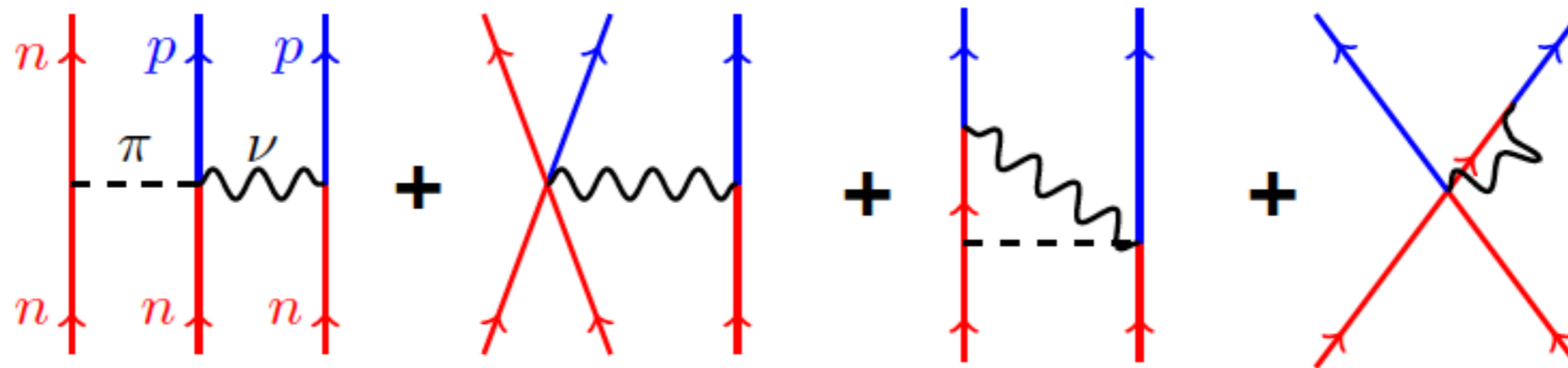
- Ultrasoft neutrinos couple to *nuclear* states: sensitivity to $E_n - E_i$ and $\langle f | J_\mu | n \rangle \langle n | J^\mu | i \rangle$ that also determine $2\nu\beta\beta$ amplitude \rightarrow corrections to closure approximation
- μ_{us} dependence cancels with $V_{\nu,2}$. Non-trivial consistency check!

Anatomy of $0\nu\beta\beta$ amplitude in χ EFT

Figure adapted from Primakoff-Rosen 1969



- Beyond N2LO: “2-body current x 1-body current” starts at N3LO



Wang-Engel-Yao 1805.10276

Conclusions

- Chiral EFT analysis of **light v_M exchange** contribution to $0\nu\beta\beta$
 - **Key new result:** leading order contact $nn \rightarrow pp$ operator. LEC enhanced by $(4\pi)^2$ compared to naive dimensional analysis. **$O(1)$ impact on sensitivity to $m_{\beta\beta}$**
 - At N2LO, identified new non-factorizable potential & corrections to closure approximation due to “ultrasoft” v 's
- **Important aside:** same enhancements affect $nn \rightarrow pp$ contacts induced by dim-9 LNV operators (= short-distance mechanisms)
- Outlook / future work:
 - **Determination of LO coupling g_v :** match to lattice QCD, $I=2$ EM observables, models...

Backup

$0\nu\beta\beta$ potential in pionless EFT

V. Cirigliano, W. Dekens, E. Mereghetti, A. Walker-Loud, 1710.01729

$$V_{\nu,0}^{(a,b)} = \tau^{(a)+}\tau^{(b)+} \left\{ \frac{1}{\mathbf{q}^2} \left(g_V^2 - g_A^2 \boldsymbol{\sigma}^{(a)} \cdot \boldsymbol{\sigma}^{(b)} \right) - \frac{2g_\nu^{NN}}{(4\pi F_0)^2} \mathbf{1}^{(a)} \times \mathbf{1}^{(b)} \right\}$$

$$g_\nu^{NN} = \mathcal{O}\left(\frac{\Lambda_\chi^2}{N^2}\right)$$

- Need leading order counterterm to make the S-matrix element scale-independent



$$\mathcal{A}(nn(^1S_0) \rightarrow pp(^1S_0)) \sim G_F^2 m_{\beta\beta} \left\{ \left(\frac{T}{C_s(\mu)} \right)^2 \left(\left(\frac{m_N C_s(\mu)}{4\pi} \right)^2 (1 + 3g_A^2) I_2 - \frac{2g_\nu^{NN}}{(4\pi F_0)^2} \right) + \dots \right\}$$

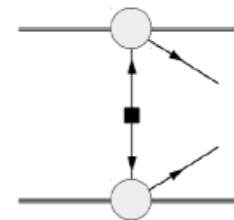
$$g_\nu^{NN}(\mu) = (4\pi F_0)^2 \left(\frac{m_N C_s(\mu)}{4\pi} \right)^2 \tilde{g}_\nu^{NN}(\mu) \quad C_s = C_S - 3C_T = \frac{4\pi}{m_N(a_s^{-1} - \mu)} \quad \frac{d}{d \log \mu} \tilde{g}_\nu^{NN} = \frac{1 + 3g_A^2}{2}$$

Closure approx. and its corrections

- Leading amplitude controlled by *ground state* matrix element of $V_{v,0}$
- Modulo contact term, standard analysis agrees with $V_{v,0}$ if use closure and neglect $\bar{E} - E_i$

$$\sum_n \frac{\langle f | J^\mu(\mathbf{q}) | n \rangle \langle n | J_\mu(-\mathbf{q}) | i \rangle}{|\mathbf{q}|(|\mathbf{q}| + E_n - E_i)} \longrightarrow \frac{\langle f | J^\mu(\mathbf{q}) J_\mu(-\mathbf{q}) | i \rangle}{|\mathbf{q}|(|\mathbf{q}| + \bar{E} - E_i)} \longrightarrow \langle f | \frac{J^\mu(\mathbf{q}) J_\mu(-\mathbf{q})}{|\mathbf{q}|^2} | i \rangle$$

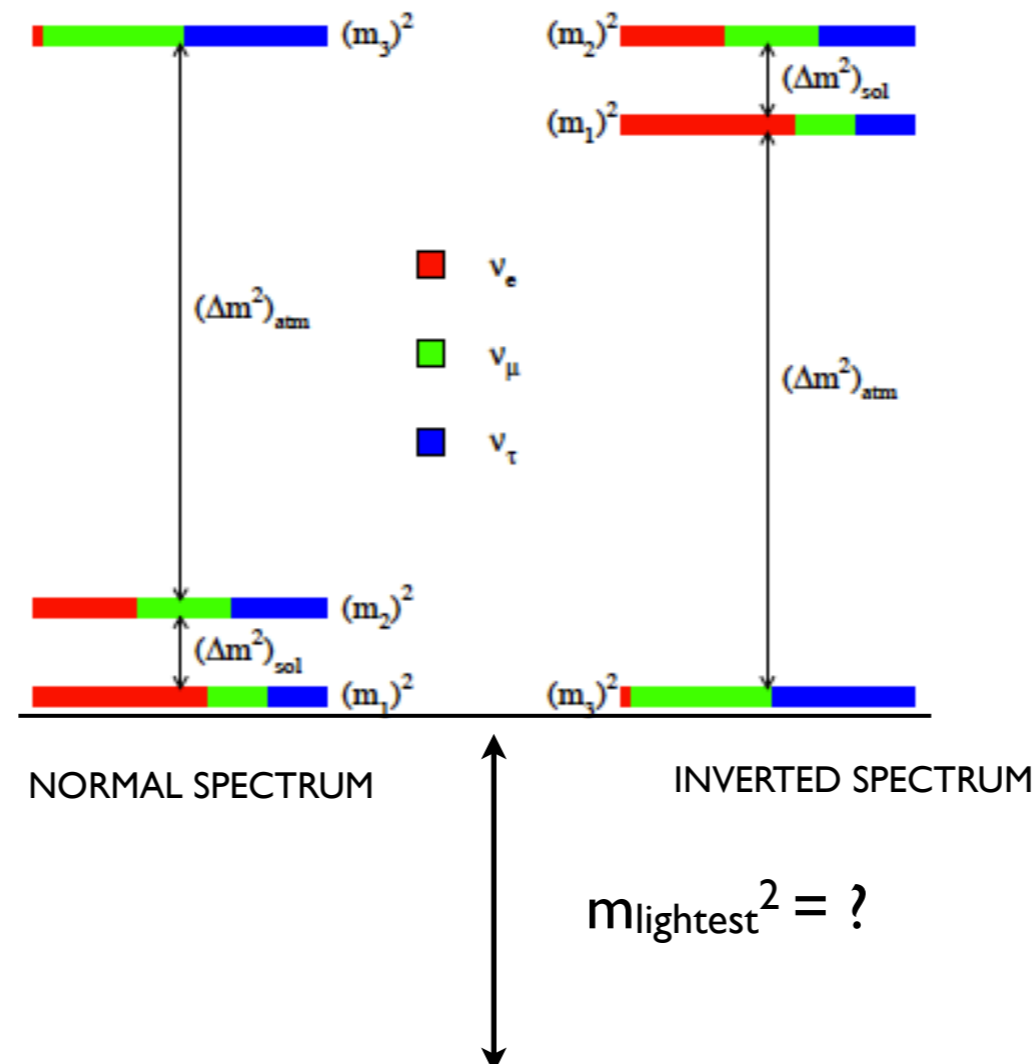
$$|\mathbf{q}| \gg E_n - E_i$$



High-scale seesaw

- Strong correlation of $0\nu\beta\beta$ with neutrino phenomenology: $\Gamma \propto (m_{\beta\beta})^2$

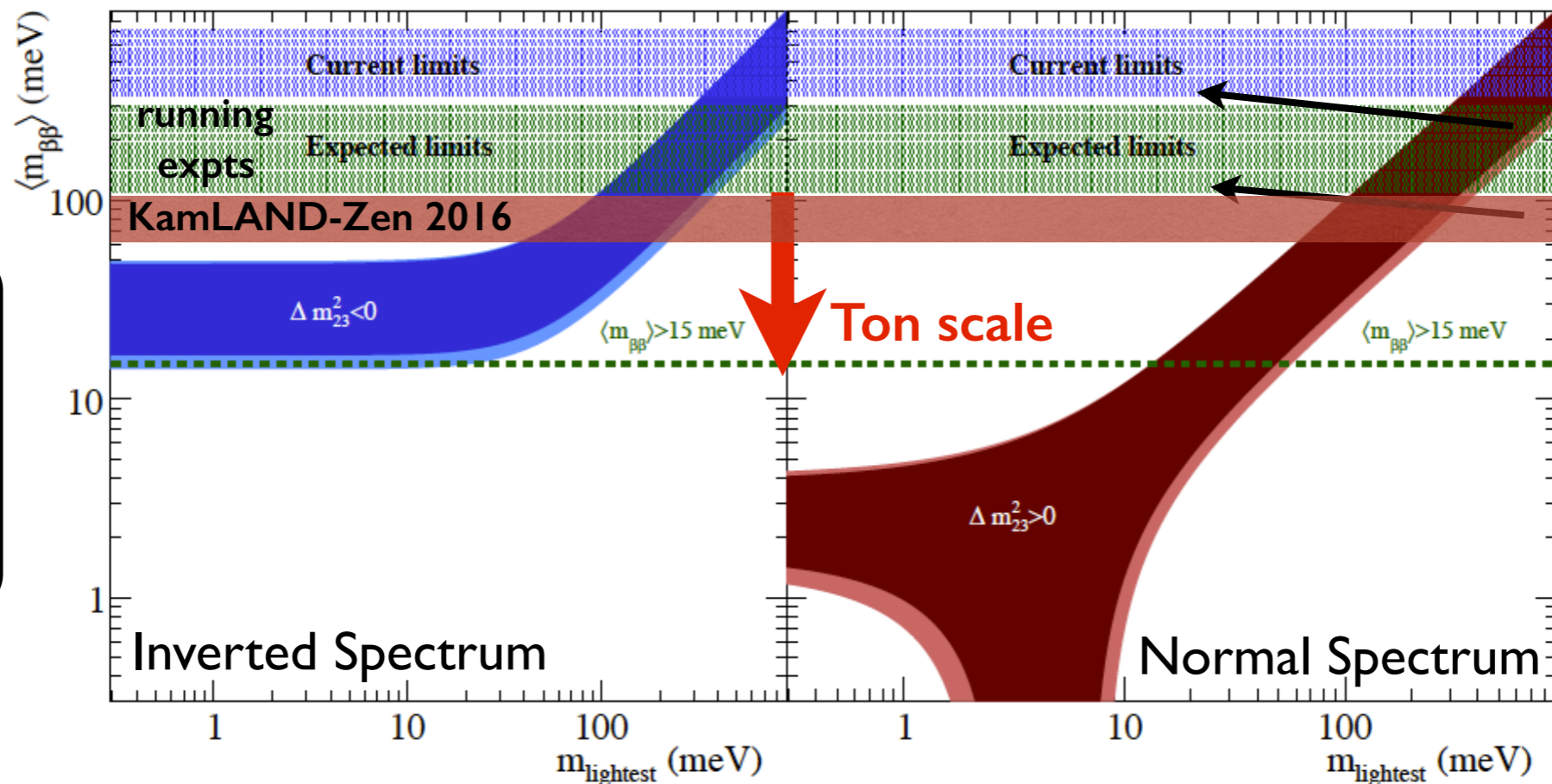
$$\langle m_{\beta\beta} \rangle^2 = \left| \sum_i U_{ei}^2 m_{\nu i} \right|^2$$



High-scale seesaw

- Strong correlation of $0\nu\beta\beta$ with neutrino phenomenology: $\Gamma \propto (m_{\beta\beta})^2$

$$\langle m_{\beta\beta} \rangle^2 = \left| \sum_i U_{ei}^2 m_{\nu i} \right|^2$$



Dark bands:
unknown phases

Light bands:
uncertainty from
oscillation
parameters(90% CL)

Assume most
“pessimistic” values
for nuclear matrix
elements

- Discovery possible for **inverted spectrum** OR **$m_{\text{lightest}} > 50$ meV**

Status of nuclear matrix elements

Engel-Menendez 1610.06548

