

Current status of neutrinoless $\beta\beta$ decay nuclear matrix elements

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Graduate School of Science
University of Tokyo

Center for Nuclear Study (CNS)



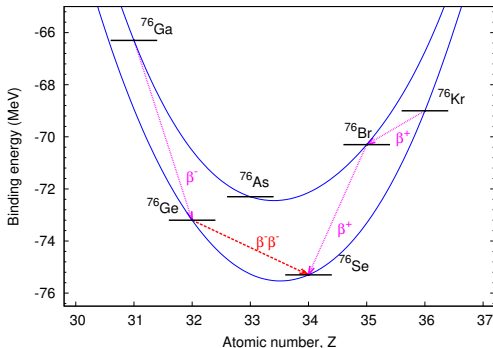
東京大学
THE UNIVERSITY OF TOKYO



Neutrinoless $\beta\beta$ decay

Lepton-number violation, Majorana nature of neutrinos

Second order process only observable in rare cases with β -decay energetically forbidden or hindered by ΔJ



Best limit: ^{76}Ge (GERDA), ^{130}Te (CUORE), ^{136}Xe (EXO, KamLAND-Zen)

Nuclear matrix elements for fundamental physics

Neutrinos, dark matter studied in experiments using nuclei

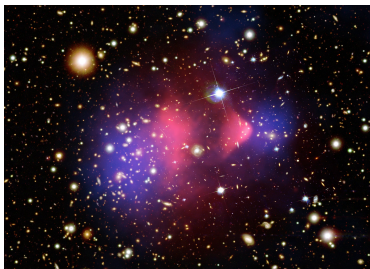
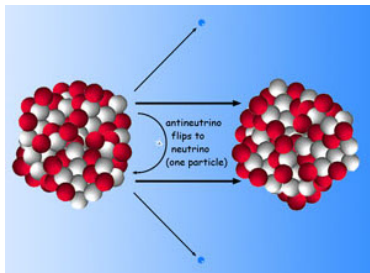
Nuclear matrix elements depend on nuclear structure crucial to anticipate reach and fully exploit experiments

$$0\nu\beta\beta \text{ decay: } \left(T_{1/2}^{0\nu\beta\beta}\right)^{-1} \propto |M^{0\nu\beta\beta}|^2 m_{\beta\beta}^2$$

$$\text{Dark matter: } \frac{d\sigma_{\chi\mathcal{N}}}{dq^2} \propto \left| \sum_i c_i \zeta_i \mathcal{F}_i \right|^2$$

$M^{0\nu\beta\beta}$: Nuclear matrix element

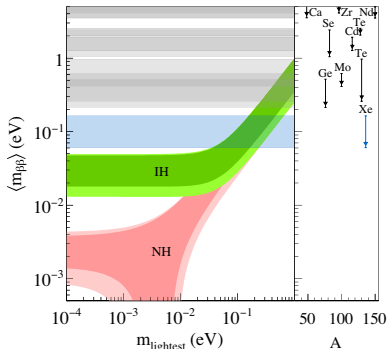
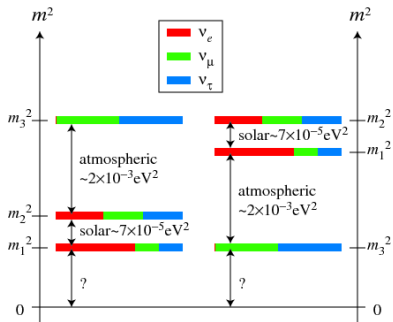
\mathcal{F}_i : Nuclear structure factor



Next generation experiments: inverted hierarchy

The decay lifetime is $T_{1/2}^{0\nu\beta\beta} (0^+ \rightarrow 0^+)^{-1} = G_{01} |M^{0\nu\beta\beta}|^2 m_{\beta\beta}^2$

sensitive to absolute neutrino masses, $m_{\beta\beta} = |\sum U_{ek}^2 m_k|$, and hierarchy



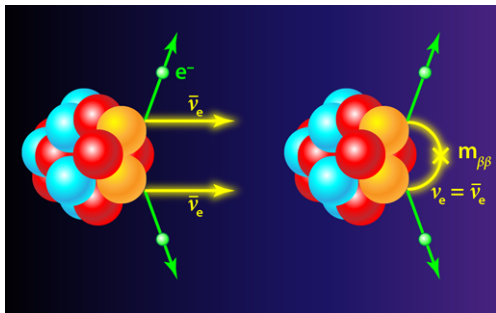
Matrix elements needed to make sure next generation ton-scale experiments fully explore "inverted hierarchy" KamLAND-Zen, PRL117 082503(2016)

Calculating nuclear matrix elements

Nuclear matrix elements needed to study fundamental symmetries

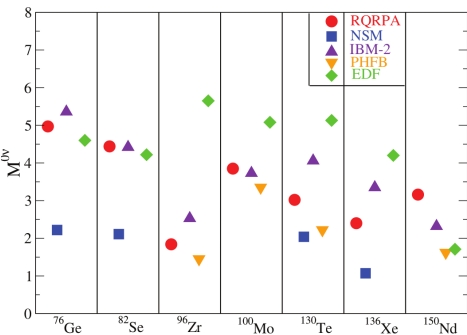
$$\langle \text{Final} | \mathcal{L}_{\text{leptons-nucleons}} | \text{Initial} \rangle = \langle \text{Final} | \int dx j^\mu(x) J_\mu(x) | \text{Initial} \rangle$$

- Nuclear structure calculation of the initial and final states:
Shell model, QRPA, IBM,
Energy-density functional
Ab initio many-body methods
GFMC, Coupled-cluster, IM-SRG...
 - Lepton-nucleus interaction:
Hadronic current in nucleus:
phenomenological,
effective theory of QCD
- V. Cirigliano's talk**

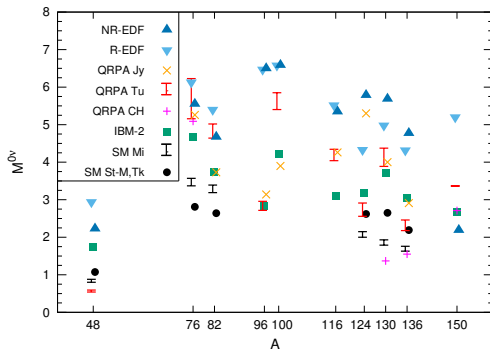


$0\nu\beta\beta$ nuclear matrix elements: last 5 years

Comparison of nuclear matrix element calculations: 2012 vs 2017



Vogel, J. Phys. G 39 124002 (2012)



Engel, JM, Rep.Prog.Phys. 80 046301(2017)

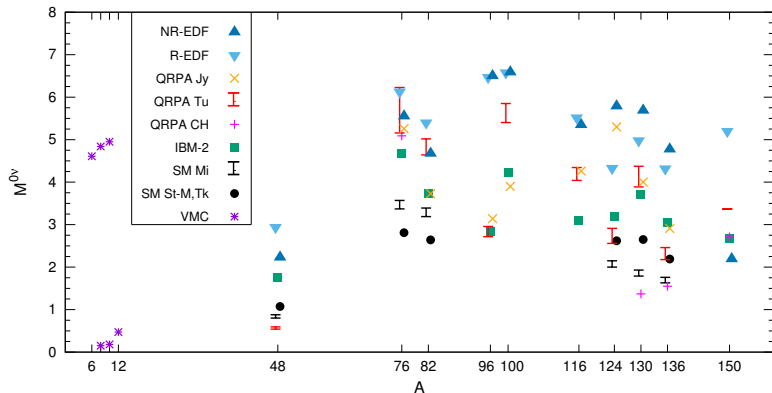
What have we learned in the last 5 years?

$0\nu\beta\beta$ decay nuclear matrix elements

Large difference in nuclear matrix element calculations: factor $\sim 2 - 3$

$$\langle 0_f^+ | \sum_{n,m} \tau_n^- \tau_m^- \sum_X H^X(r) \Omega^X | 0_i^+ \rangle$$

$\Omega^X = \text{Fermi } (\mathbb{1}), \text{GT } (\sigma_n \sigma_m), \text{Tensor}$
 $H(r) = \text{neutrino potential}$

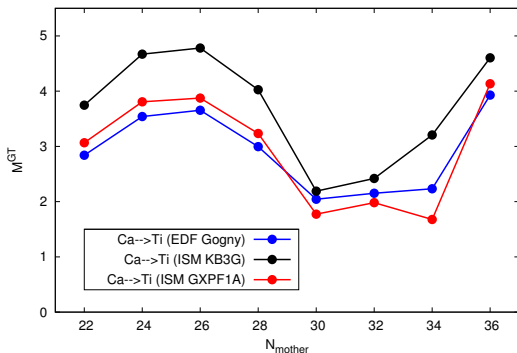


Ab initio Quantum Monte Carlo $0\nu\beta\beta$: Pastore et al. PRC97 014606(2018)

$0\nu\beta\beta$ decay without correlations

Non-realistic spherical (uncorrelated) mother and daughter nuclei:

- Shell model (SM): zero seniority, neutron and proton $J = 0$ pairs
- Energy density functional (EDF): only spherical contributions



In contrast to full (correlated) calculation SM and EDF NMEs agree!

NME scale set by pairing interaction

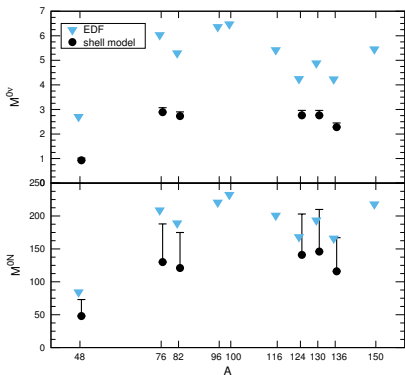
JM, Rodríguez, Martínez-Pinedo, Poves PRC90 024311(2014)

NME follows generalized seniority model:

$$M_{GT}^{0\nu\beta\beta} \simeq \alpha_\pi \alpha_\nu \sqrt{N_\pi + 1} \sqrt{\Omega_\pi - N_\pi} \sqrt{N_\nu} \sqrt{\Omega_\nu - N_\nu + 1}, \text{ Barea, Iachello PRC79 044301(2009)}$$

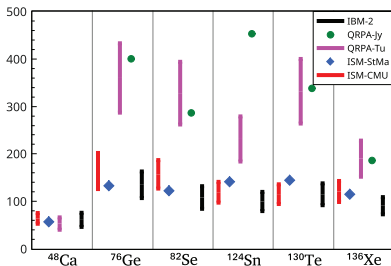
Heavy-neutrino exchange nuclear matrix elements

Contrary to light-neutrino-exchange, for heavy-neutrino-exchange decay shell model, IBM, and EDF matrix elements agree reasonably!



Song et al. PRC95 024305 (2017)

JM, JPG 45 014003 (2018)



Neacsu et al. PRC100 052503 (2015)

Longer-range nuclear correlations drive light-neutrino exchange diffs.

Heavy ν 's: short-range correlations

Cruz-Torres et al. arXiv:1710:07966

Heavy-neutrino exchange and correlations

Compared to
light-neutrino exchange

heavy neutrino exchange
dominated by
shorter internucleon range,
larger momentum transfers

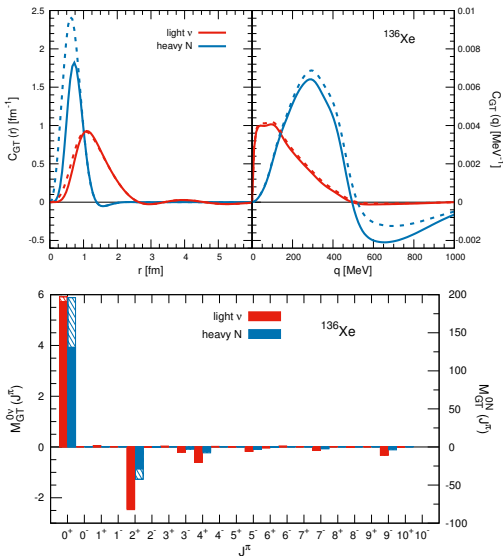
heavy neutrino exchange
contribution
from $J > 0$ pairs smaller:
pairing most relevant

⇒

Long-range correlations
(except pairing)
not under control

JM, JPG 45 014003 (2018)

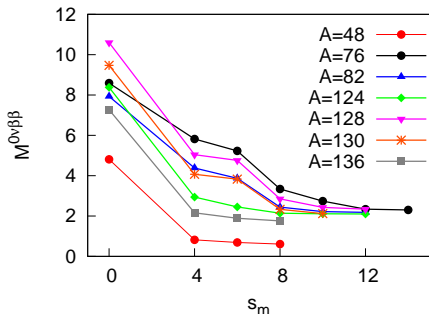
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Pairing correlations and $0\nu\beta\beta$ decay

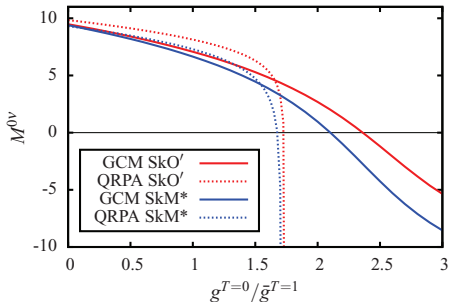
$0\nu\beta\beta$ decay favoured by proton-proton, neutron-neutron pairing, but it is disfavored by proton-neutron pairing

Ideal case: superfluid nuclei reduced with high-seniorities



Caurier et al. PRL100 052503 (2008)

Addition of isoscalar pairing reduces matrix element value



Hinohara, Engel PRC90 031301 (2014)

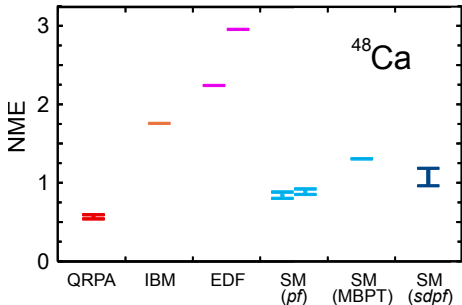
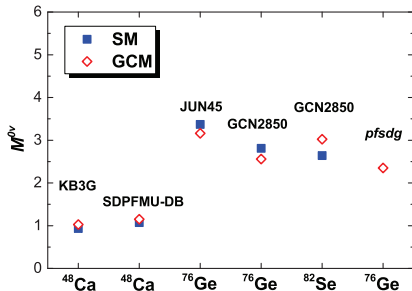
Related to approximate $SU(4)$ symmetry of the $\sum H(r)\sigma_i\sigma_j\tau_i\tau_j$ operator

Shell model matrix elements in two shells

$^{48}\text{Ca} \rightarrow ^{48}\text{Ti}$ $0\nu\beta\beta$ decay

Enlarge configuration space
from pf to $sdpf$, 4 to 7 orbitals

Test excitation energy of 0_2^+ in
 ^{48}Ca off by 1.3MeV in pf shell



Nuclear matrix element
increases moderately 30%

Iwata et al. PRL116 112502 (2016)

Likewise, very mild effect
found in GCM calculations of ^{76}Ge

Jiao et al. PRC96 054310 (2017)

Ab initio many-body methods

Oxygen dripline using chiral NN+3N forces correctly reproduced
ab-initio calculations treating explicitly all nucleons
excellent agreement between different approaches

No-core shell model
(Importance-truncated)

In-medium SRG

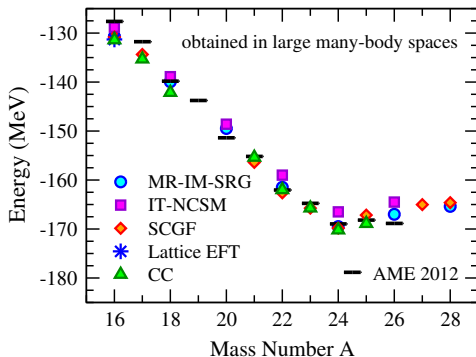
Hergert et al. PRL110 242501(2013)

Self-consistent Green's
function

Cipollone et al. PRL111 062501(2013)

Coupled-clusters

Jansen et al. PRL113 142502(2014)

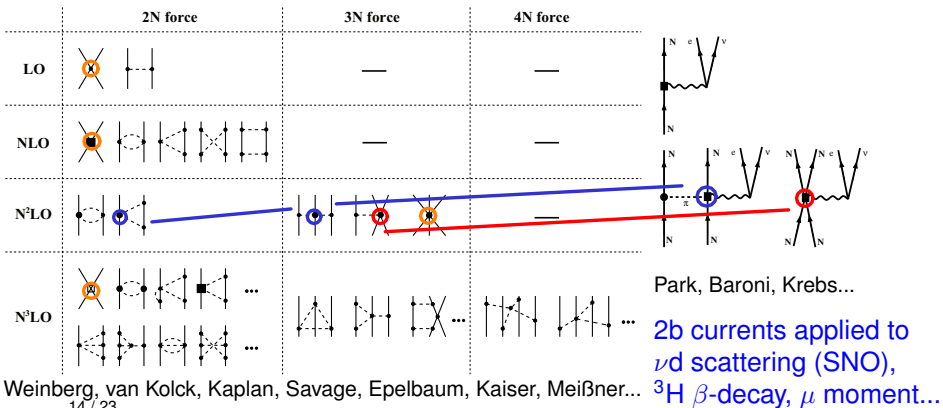


Chiral effective field theory

Chiral EFT: low energy approach to QCD, nuclear structure energies

Approximate chiral symmetry: pion exchanges, contact interactions

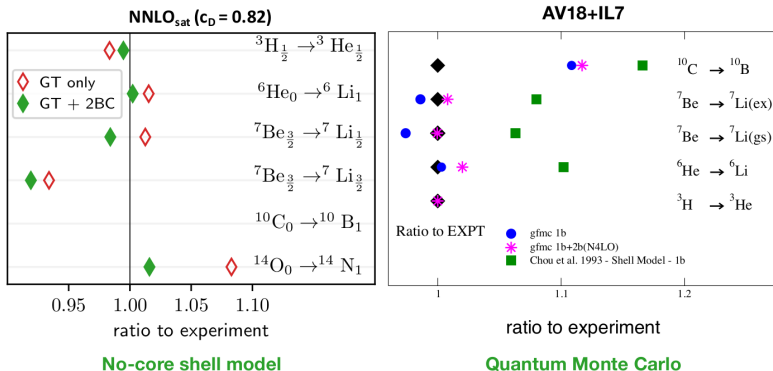
Systematic expansion: nuclear forces and electroweak currents



β decay in very light nuclei: GFMC vs NCSM

Quantum Monte Carlo, No Core Shell Model β decays in $A \leq 10$

Pastore et al. PRC97 022501 (2018), G. Hagen et al., INT-18-1a program



Very good agreement to experiment, except ${}^{10}\text{C}$ (structure)

Impact of 2b currents small (few %), disagreement on sign

β decay in medium-mass nuclei: IMSRG

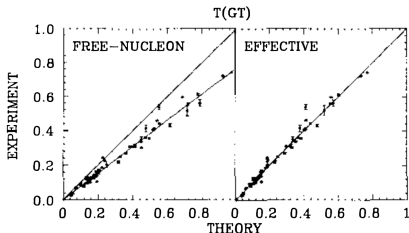


“Quenching” of g_A in Gamow-Teller Decays

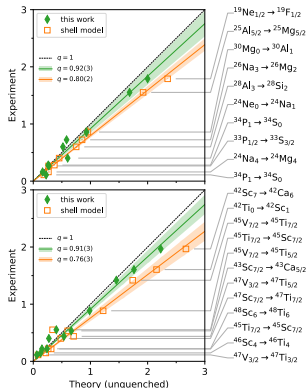
VS-IMSRG calculations of GT transitions in sd, pf shells

Minor effect from consistent effective operator

Significant effect from neglected 2-body currents



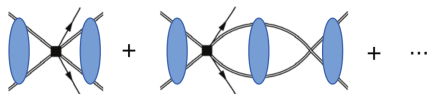
Ab initio calculations explain data with unquenched g_A



From J. Holt, INT-18-1a program

Open questions: transition operator

Contact light-neutrino operator

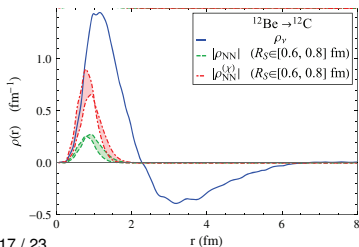


Cirigliano et al. PRL120 202001(2018)

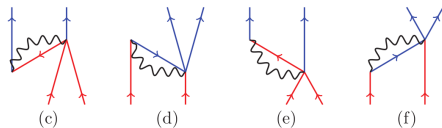
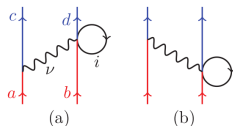
Unknown coupling value

V. Cirigliano's talk

Short-range character



Two-body currents in $\beta\beta$ decay



Estimated effect $\sim 10\%$

Wang et al. arXiv:1805:10276

compared to $\sim 20\%$
in single- β decay (“quenching”)

JM et al. PRL107 062501(2011)

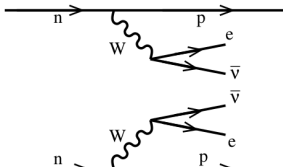
Test of nuclear structure

Test of $0\nu\beta\beta$ decay: comparison of predicted $2\nu\beta\beta$ decay vs data, momentum transfers $q \sim 100$ MeV: μ -capture, inelastic ν scattering

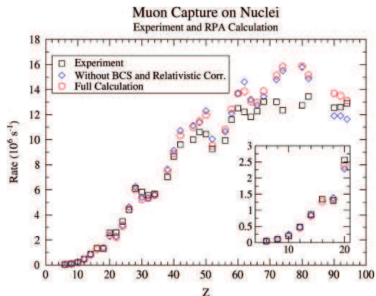
Shell model

reproduce $2\nu\beta\beta$ data including "quenching" common to β decays in same mass region

Shell model prediction previous to ^{48}Ca measurement!



$$M^{2\nu\beta\beta} = \sum_k \frac{\langle 0_f^+ | \sum_n \sigma_n \tau_n^- | 1_k^+ \rangle \langle 1_k^+ | \sum_m \sigma_m \tau_m^- | 0_i^+ \rangle}{E_k - (M_i + M_f)/2}$$



μ -capture, ν -nucleus scattering
many multipoles (J values), like $0\nu\beta\beta$ decay

Double Gamow-Teller strength distribution

Measurement of Double Gamow-Teller (DGT) resonance
in double charge-exchange reactions $^{48}\text{Ca}(pp,nn)^{48}\text{Ti}$ proposed in 80's

Auerbach, Muto, Vogel... 1980's, 90's

Recent experimental plans in RCNP, RIKEN (^{48}Ca), INFN Catania

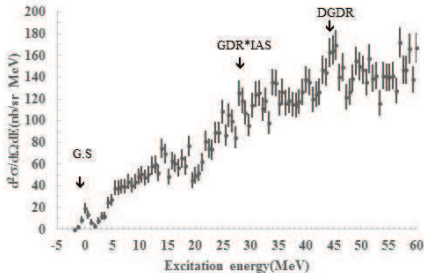
Takaki et al. JPS Conf. Proc. 6 020038 (2015)

Capuzzello et al. EPJA 51 145 (2015), Takahisa, Ejiri et al. arXiv:1703.08264

Promising connection to $\beta\beta$ decay,
two-particle-exchange process,
especially the (tiny) transition
to ground state of final state

Two-nucleon transfers related to
 $0\nu\beta\beta$ decay matrix elements

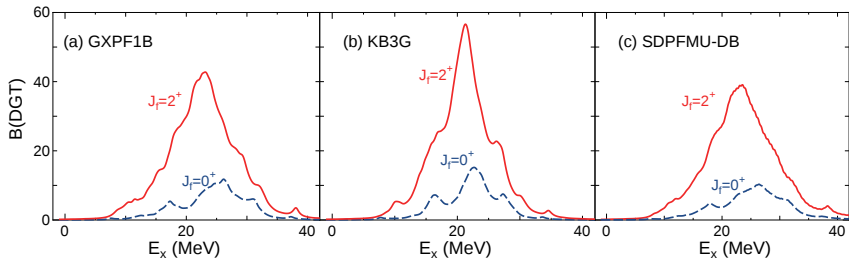
Brown et al. PRL113 262501 (2014)



^{48}Ca Double Gamow-Teller distribution

Calculate with shell model ^{48}Ca 0_{gs}^+ Double Gamow-Teller distribution

$$B(\text{DGT}^-; \lambda; i \rightarrow f) = \frac{1}{2J_i + 1} \left| \left\langle {}^{48}\text{Ti} \left\| \left[\sum_i \sigma_i \tau_i^- \times \sum_j \sigma_j \tau_j^- \right]^{(\lambda)} \right\| \left| {}^{48}\text{Ca}_{\text{gs}} \right\rangle \right|^2$$

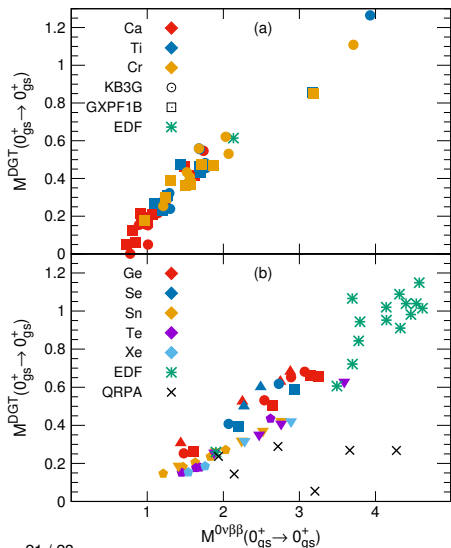


Shell model calculation with Lanczos strength function method

Double GT resonances in one and two shells rather similar result

Shimizu, JM, Yako, PRL120 142502 (2018)

DGT and $0\nu\beta\beta$ decay: heavy nuclei



DGT transition to ground state

$$M^{\text{DGT}} = \sqrt{B(\text{DGT}_{-}; 0; 0_{\text{gs}}^+ \rightarrow 0_{\text{gs}}^+)}$$

very good linear correlation
with $0\nu\beta\beta$ decay
nuclear matrix elements

Correlation holds
across wide range of nuclei,
from Ca to Ge and Xe

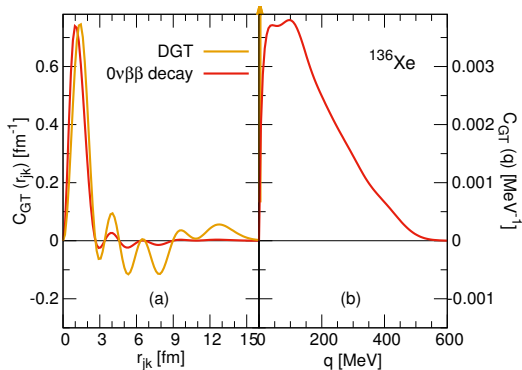
Common to shell model and
energy-density functional theory
 $0 \lesssim M^{0\nu\beta\beta} \lesssim 5$
disagreement to QRPA

Shimizu, JM, Yako,
PRL120 142502 (2018)

Short-range character of DGT, $0\nu\beta\beta$ decay

Correlation between DGT and $0\nu\beta\beta$ decay matrix elements explained by transition involving low-energy states combined with dominance of short distances between exchanged/decaying neutrons

Bogner et al. PRC86 064304 (2012)



$0\nu\beta\beta$ decay matrix element limited to shorter range

Short-range part dominant in double GT matrix element due to partial cancellation of mid- and long-range parts

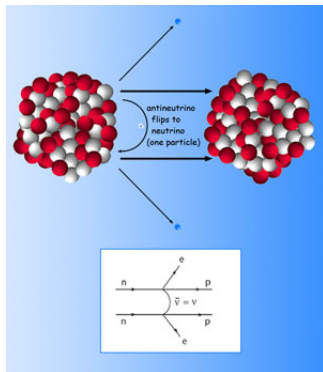
Long-range part dominant in QRPA DGT matrix elements

Shimizu, JM, Yako,
PRL120 142502 (2018)

Summary

Nuclear matrix elements are key for the design of next-generation tonne-scale $0\nu\beta\beta$ decay experiments and for fully exploiting the experimental results

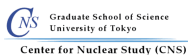
- Present matrix element calculations disagree
Need improved calculations, guidance from other nuclear experiments
- Ab initio matrix elements in light nuclei
ab initio matrix elements in $\beta\beta$ emitters soon!
- Double Gamow-Teller transitions pursued in RIKEN, INFN LNS, RCNP Osaka can provide very useful insight on value of $0\nu\beta\beta$ decay matrix elements



Collaborators



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